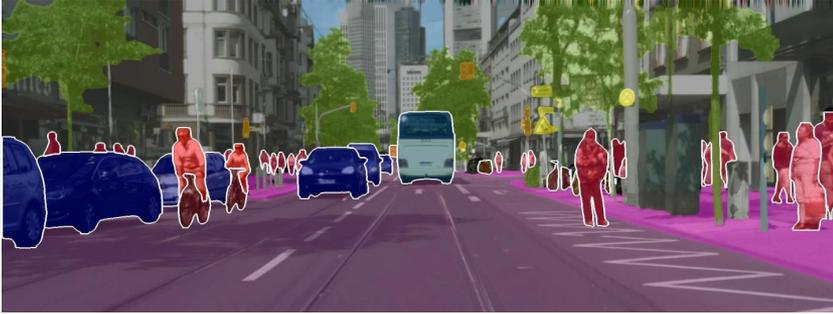
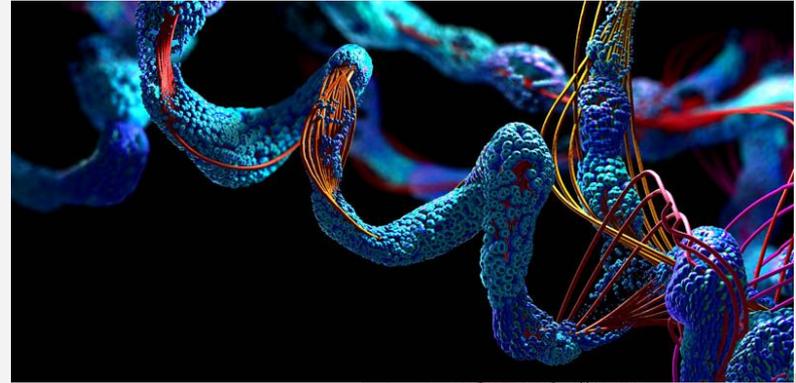


Sequential and Generative Modeling

Oct 29, 2025



eureka!ert



AWS - BERT



NASA



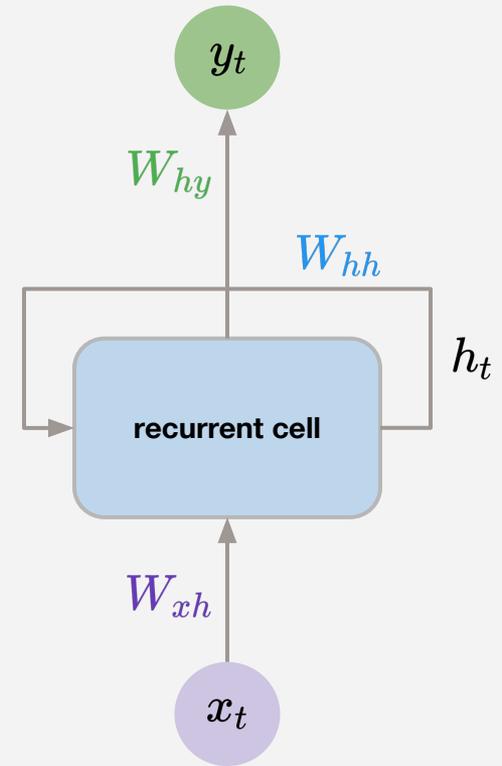
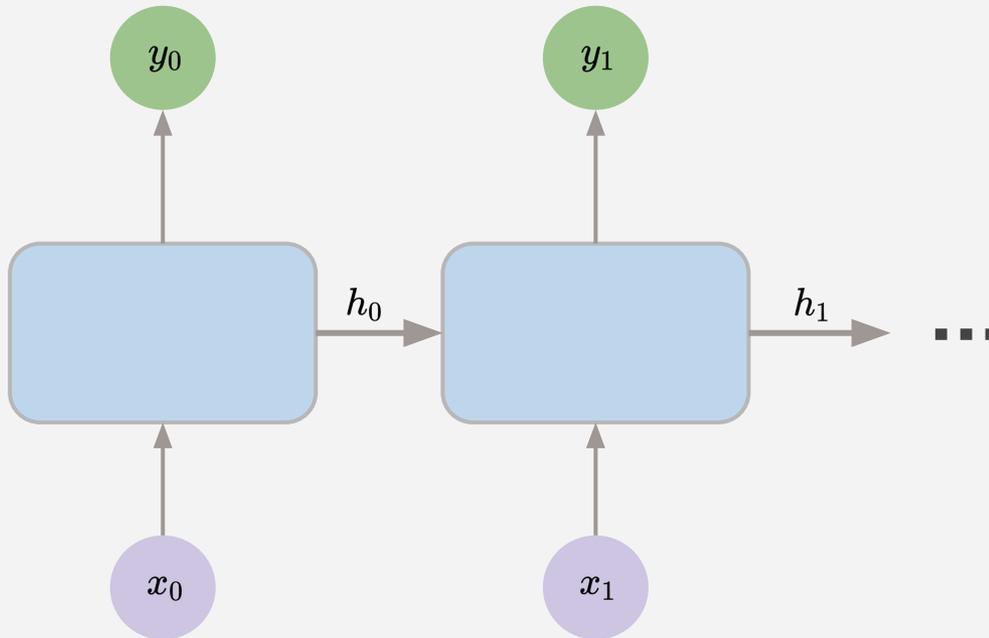
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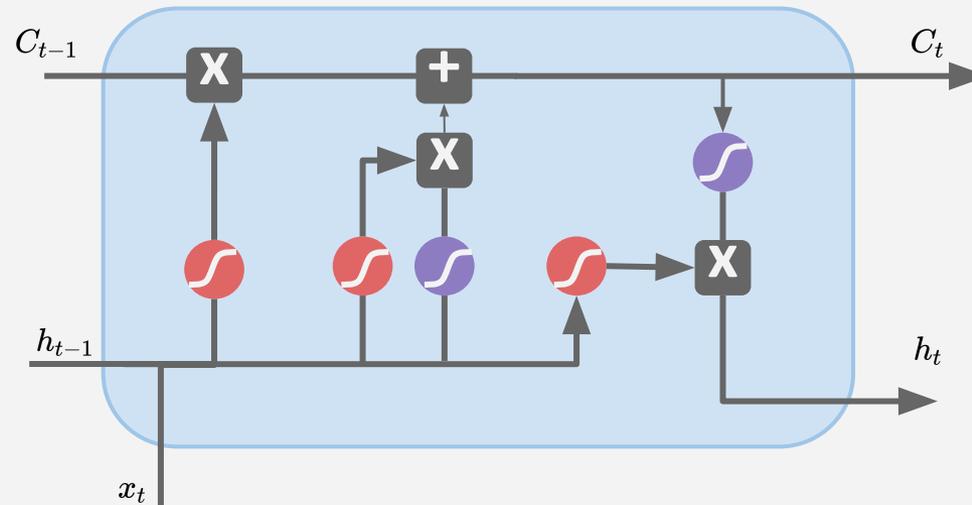
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Sequences in the Wild

Review: RNNs



Review: LSTMs



1. Maintains a persistent cell state - robust to gradient updates
2. Gates to regulate information
 - a. **Forget gate** to remove unnecessary information from the cell state
 - b. **Input gate** to selectively use the current input and hidden state information
 - c. **Output gate** to propagate the modified cell state to the next cell
3. Gates are parameterized

Backpropagation through time will update gradients to **control gates** for **long-term persistence**

Attention Intuition

Attend to the most important parts of an input



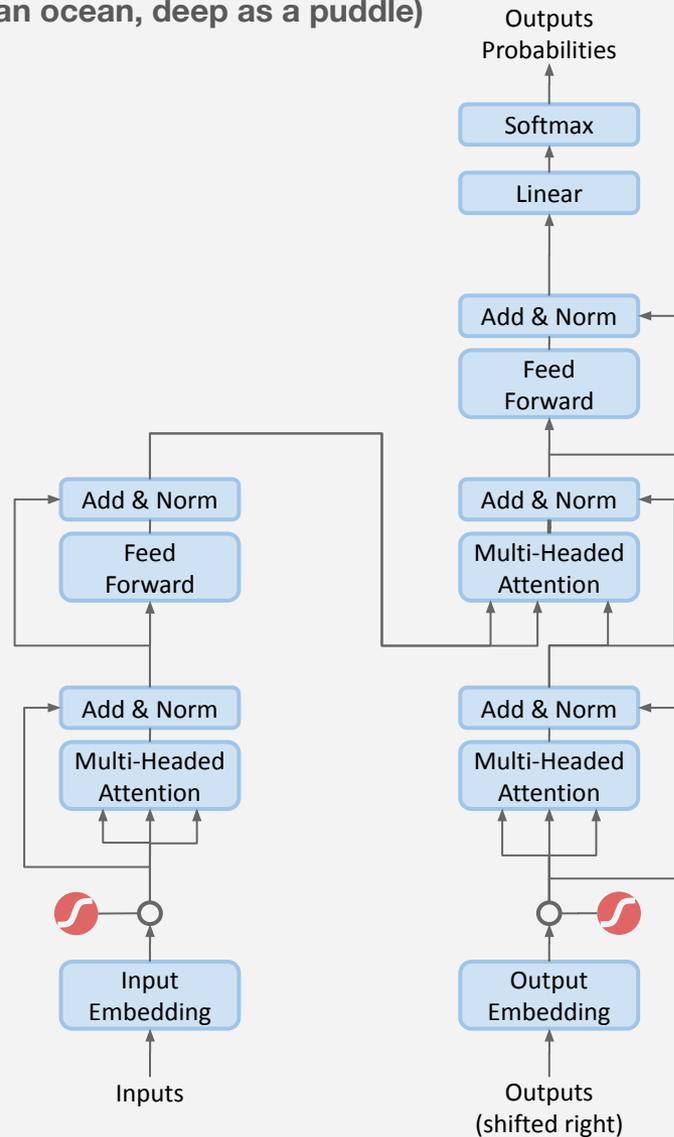
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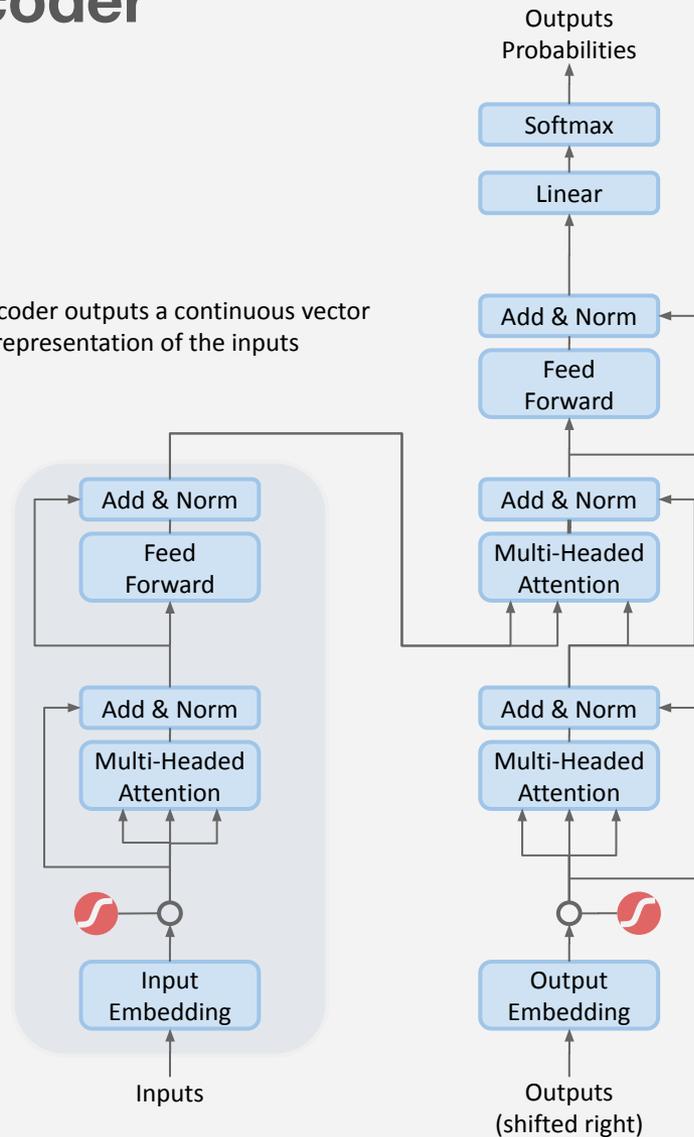
1. Identify which parts to attend } Search
2. Extract parts with high attention } Feature Extraction
3. Condition output on extracted parts } Linear Feedforward

Transformer (Wide as an ocean, deep as a puddle)

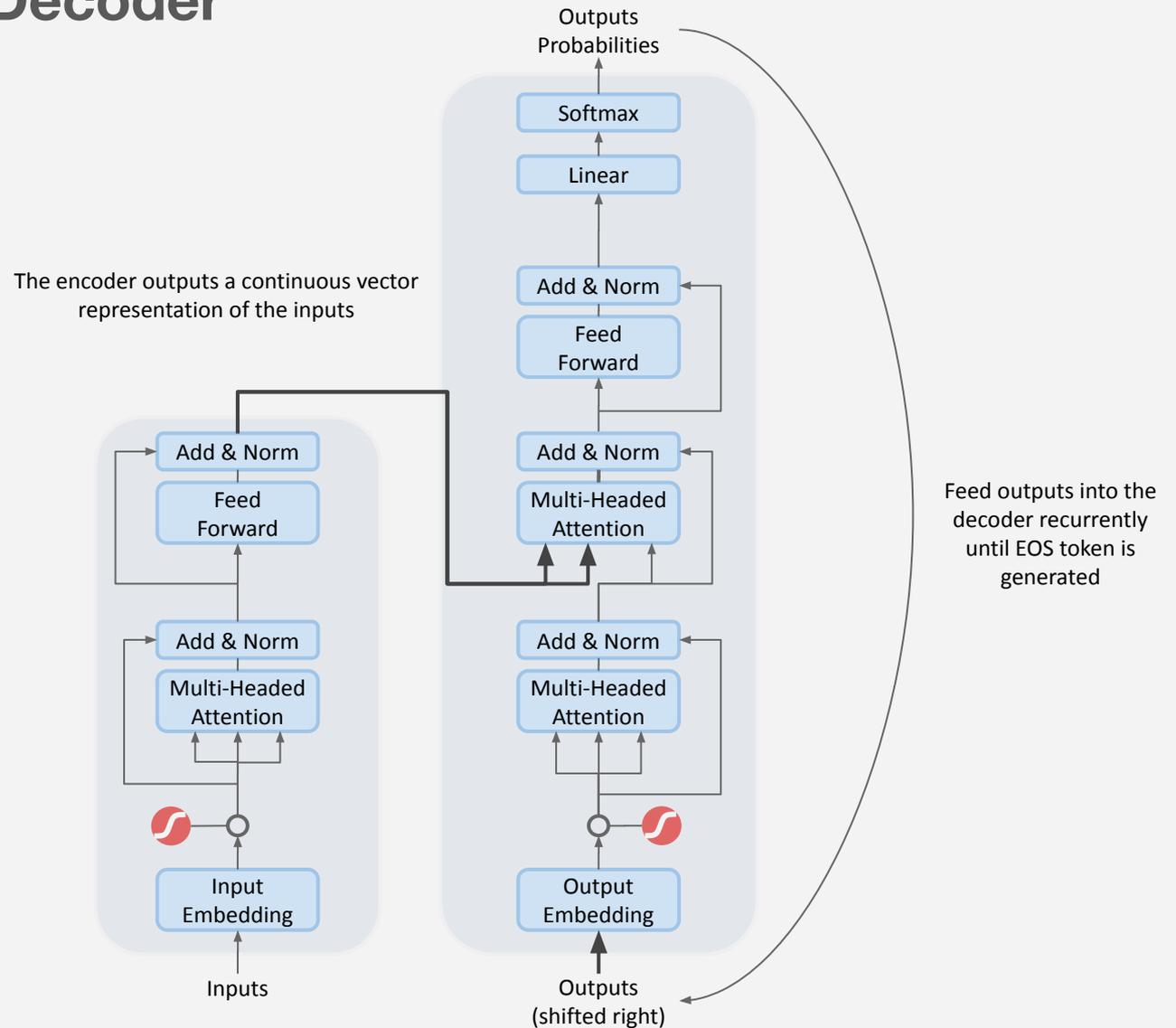


Transformer: Encoder

The encoder outputs a continuous vector representation of the inputs



Transformer: Decoder

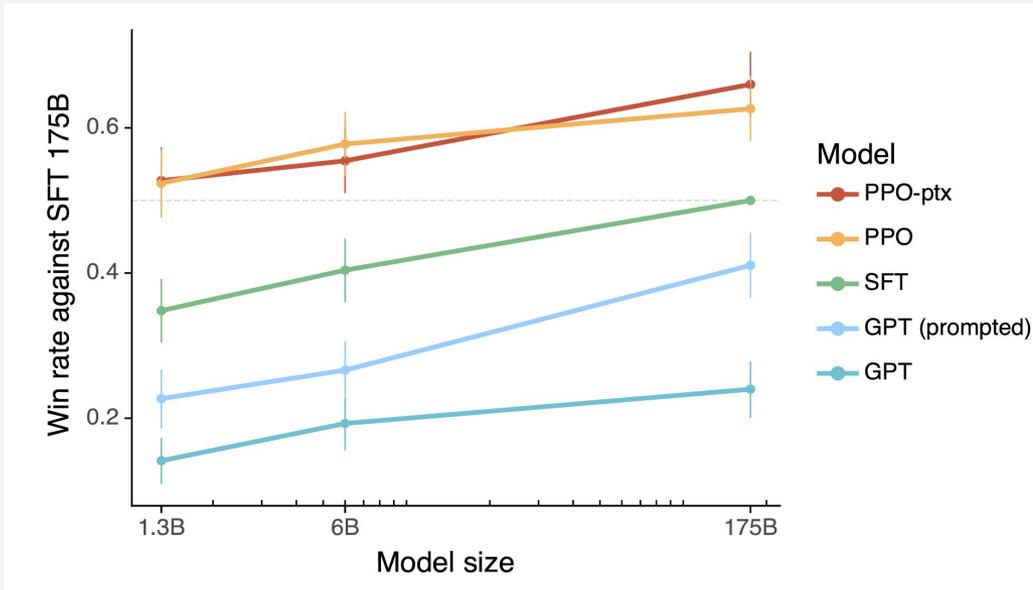


What is the Model Aligned To?

- Follows human instructions?
- Guardrails?
- Contexts?

Ouyang, Long, Jeffrey Wu, Xu Jiang, Diogo Almeida, Carroll Wainwright, Pamela Mishkin, Chong Zhang et al. "Training language models to follow instructions with human feedback." *Advances in neural information processing systems* 35 (2022): 27730-27744.

RLHF Leads to Massive Performance Gains



1.5B parameter RLHF model preferred over model 100x the size

→ Authors conclude **investing in RLHF fine-tuning is more cost effective than continuing to scale**

Quoting the DeepSeek Paper

“Behaviors such as reflection, where the model revisits and reevaluates its previous steps, and the exploration of alternative approaches to problem-solving arise spontaneously. These behaviors are not explicitly programmed but instead **emerge as a result of the model’s interaction with the reinforcement learning environment**”

“...captivating example of how reinforcement learning can lead to **unexpected and sophisticated outcomes**”

“...rather than explicitly teaching the model on how to solve a problem, **we simply provide it with the right incentives, and it autonomously develops advanced problem-solving strategies.**”

Guo, Daya, Dejian Yang, Haowei Zhang, Junxiao Song, Ruoyu Zhang, Runxin Xu, Qihao Zhu et al. "Deepseek-r1: Incentivizing reasoning capability in llms via reinforcement learning." arXiv preprint arXiv:2501.12948 (2025).

Quotes from the DeepSeek Paper

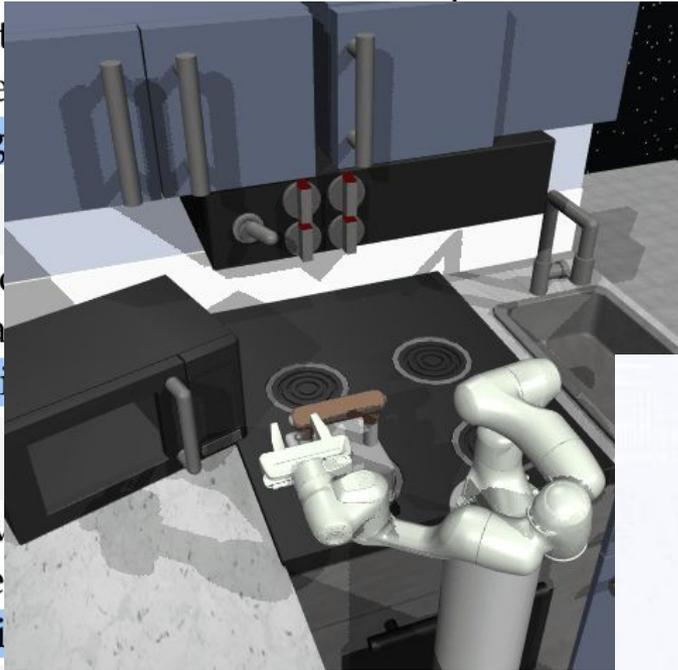
behaviors as the test-time computation increases. Behaviors such as reflection—where the model revisits and reevaluates its previous steps—and the exploration of alternative approaches to problem-solving arise spontaneously. These behaviors are not explicitly programmed but instead emerge as a result of the model's interaction with the reinforcement learning environment. This

approach. This behavior is not only a testament to the model's growing reasoning abilities but also a captivating example of how reinforcement learning can lead to unexpected and sophisticated outcomes.

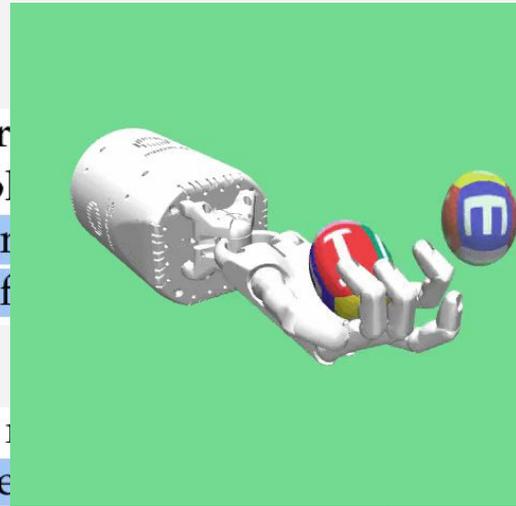
observing its behavior. It underscores the power and beauty of reinforcement learning: rather than explicitly teaching the model on how to solve a problem, we simply provide it with the right incentives, and it autonomously develops advanced problem-solving strategies. The

Quotes from the DeepSeek Paper

behaviors as the test-time computation increases. Behavior revisits problems—and the exploratory behaviors are not emergent with the reinforcement learning.



statement to the reinforcement learning.



the model approaches to output instead of a single token. This

abilities detected and

approach but a sophisticated

observed than expected right i



rather than the . The

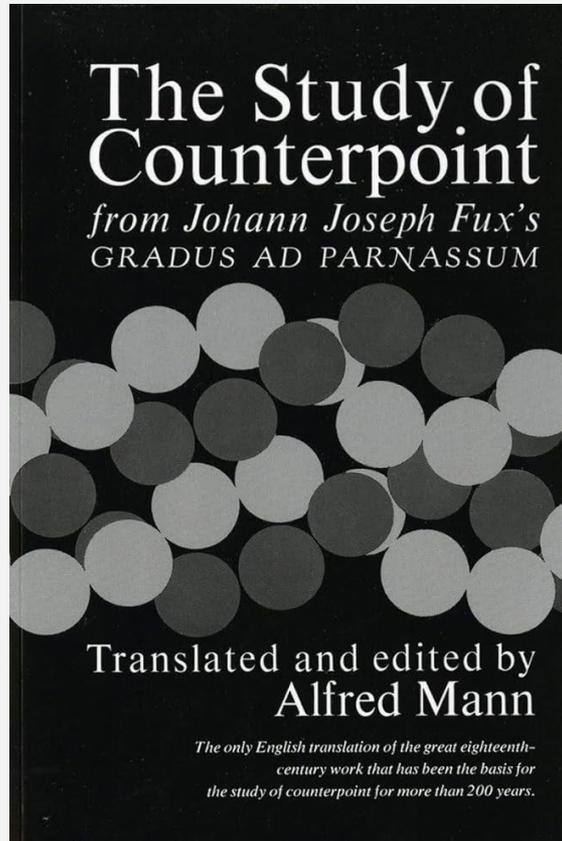
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Music Generation



Jaques, Natasha, Shixiang Gu, Richard E. Turner, and Douglas Eck. "Tuning recurrent neural networks with reinforcement learning." (2017).

Using RL to Enforce Advice from Music Theory

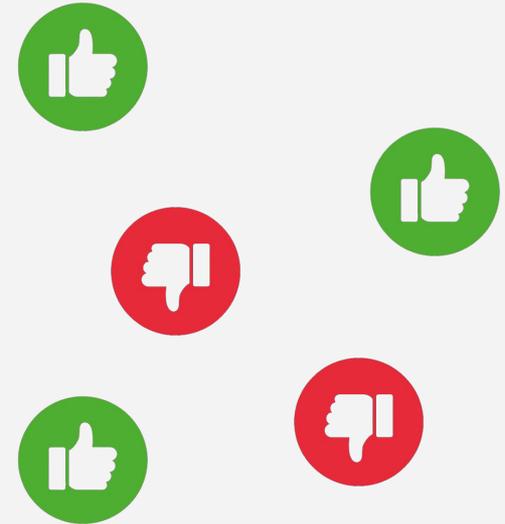
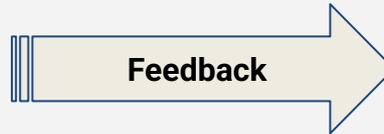
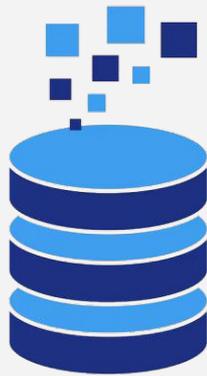


First species counterpoint

The simplest method of writing counterpoint, this outlines the harmonic “skeleton” for a phrase.

- **Note against note:** for every note in the **cantus firmus** (c.f.), or the voice that is given, write a corresponding note
- **Consonance only:** every interval between the counterpoint and cantus firmus must be a perfect or imperfect consonance
- **No voice crossing:** the written counterpoint should be entirely above or below the cantus firmus (c.f.)
 - Voice crossing is allowed only for “exceptionally pleasing lines”
- **Start and end in the right mode (key):** if writing above the c.f., the last note should be the tonic, meaning the last interval should be (1) unison or (8) octave. If writing below the c.f., both the first and last intervals should be tonic (1 or 8).
 - Perfect consonances are preferred for openings and cadences, imperfect consonances for the middle of phrases
 - Avoid unisons in the middle of phrases
 - The last interval (cadence) should be approached stepwise in contrary motion.
- Avoid skips greater than a (5) fifth

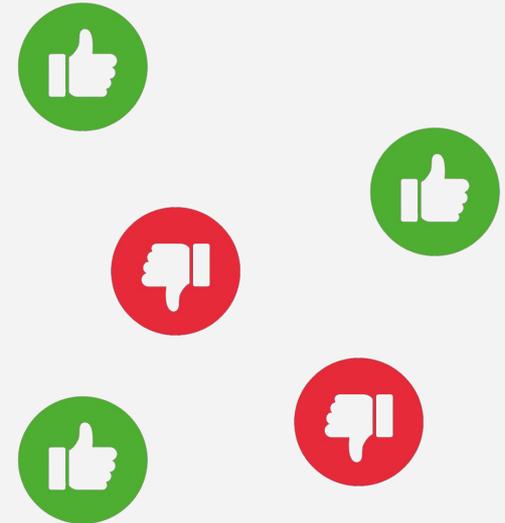
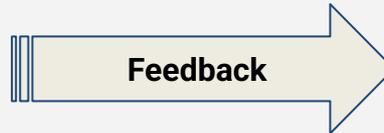
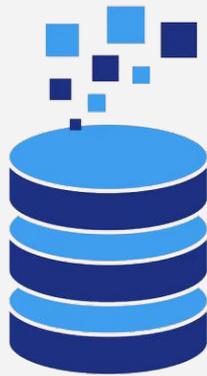
RL Fine-Tuning for Music



Pre-train on data
(→ music as a sequence)

Keep training with RL
(→ learn “rules” of music theory)

RL Fine-Tuning for Translation



Pre-train on data
(→ learn a language)

Keep training with RL
(→ improve BLEU score)

Ranzato, Marc'Aurelio, Sumit Chopra, Michael Auli, and Wojciech Zaremba. "Sequence level training with recurrent neural networks." arXiv preprint arXiv:1511.06732 (2015).

Problems with Naive RL Fine-Tuning

- **Catastrophic forgetting**



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Problems with Naive RL Fine-Tuning

- **Catastrophic forgetting**
- **RL will trivially exploit the reward**
- **Imperfect reward functions**
 - Can we create a proxy?



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Music Generation + RL Fine-Tuning

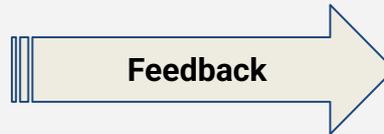


Jaques, Natasha, Shixiang Gu, Richard E. Turner, and Douglas Eck. "Tuning recurrent neural networks with reinforcement learning." (2017).

Fine-Tuning a LLM with RL



Pre-train on data



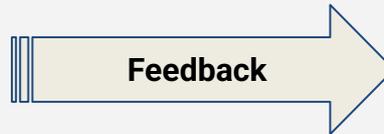
Keep training with RL

Jaques, Natasha, Shixiang Gu, Dzmitry Bahdanau, José Miguel Hernández-Lobato, Richard E. Turner, and Douglas Eck. "Sequence tutor: Conservative fine-tuning of sequence generation models with kl-control." In International Conference on Machine Learning, pp. 1645-1654. PMLR, 2017.

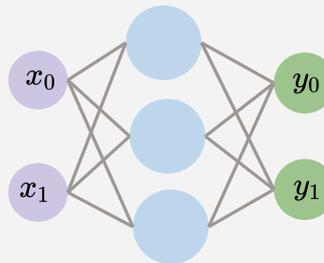
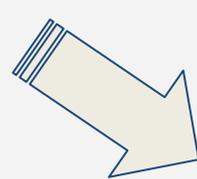
Fine-Tuning a LLM with RL



Pre-train on data



Keep training with RL

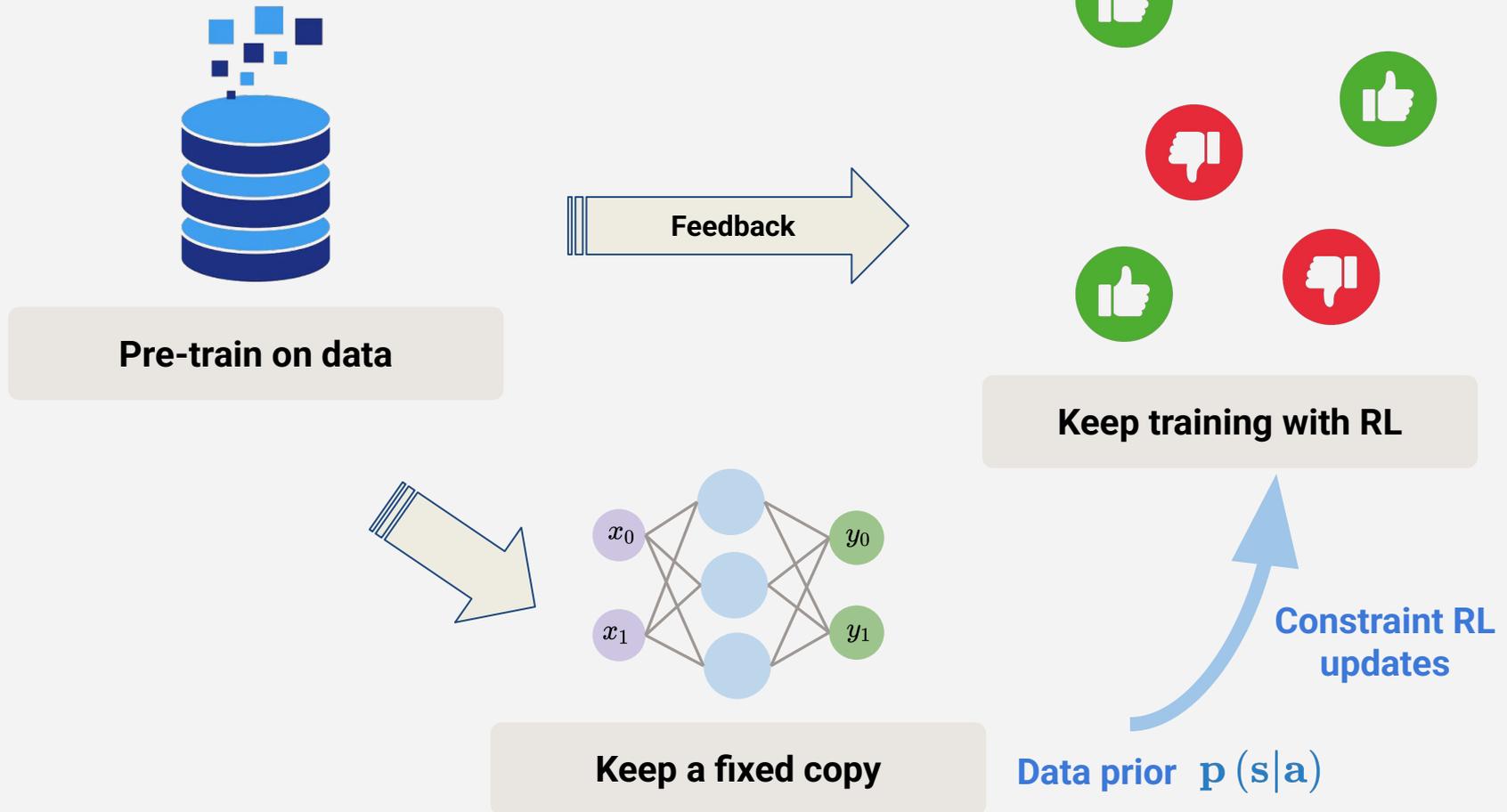


Keep a fixed copy

Data prior $p(s|a)$

Jaques, Natasha, Shixiang Gu, Dzmitry Bahdanau, José Miguel Hernández-Lobato, Richard E. Turner, and Douglas Eck. "Sequence tutor: Conservative fine-tuning of sequence generation models with kl-control." In International Conference on Machine Learning, pp. 1645-1654. PMLR, 2017.

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Fine-Tuning a LLM with RL

- **KL-control from pre-trained data prior** $p(s|a)$

$$L(q) = \mathbb{E}_{q(\tau)} [r(\tau)]/c - D_{KL} [q(\tau) || p(\tau)]$$

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RL Policy



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RL Policy

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RL Policy

Pre-trained prior

$$Q^\pi(s_t, a_t) = \mathbb{E}_\pi \left[\sum_{t'=t}^T r(s_{t'}, a_{t'})/c - \log \pi(a_{t'}|s_{t'}) + \log p(a_{t'}|s_{t'}) \right]$$

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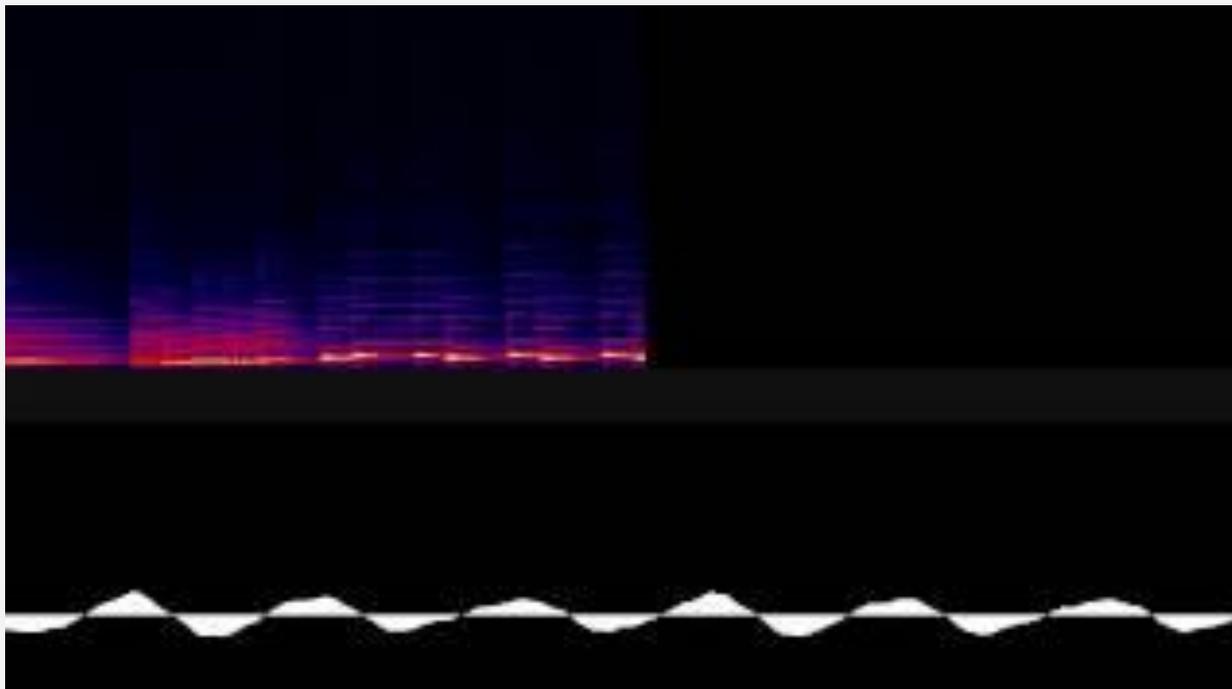
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Music Generation with Sequence Tutor



Jaques, Natasha, Shixiang Gu, Richard E. Turner, and Douglas Eck. "Tuning recurrent neural networks with reinforcement learning." (2017).

What is RLHF

What is RLHF

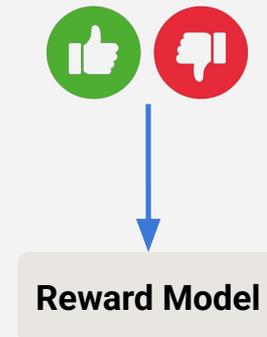
1. Collect human feedback data



Christiano, Paul F., Jan Leike, Tom Brown, Miljan Martic, Shane Legg, and Dario Amodei. "Deep reinforcement learning from human preferences." Advances in neural information processing systems 30 (2017).

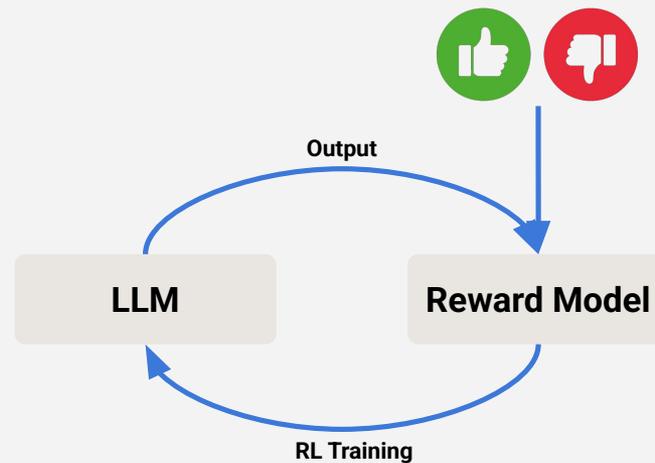
What is RLHF

1. Collect human feedback data
2. Train a **reward model** to predict human feedback on novel samples



What is RLHF

1. Collect human feedback data
2. Train a **reward model** to predict human feedback on novel samples
3. **Fine-tune with RL** using RM



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Reward Model

Humans rate which of the two model outputs they prefer.

$$p_{\phi}(s_A \succ s_B) = \frac{e^{r_{\phi}(s_A)}}{e^{r_{\phi}(s_A)} + e^{r_{\phi}(s_B)}}$$

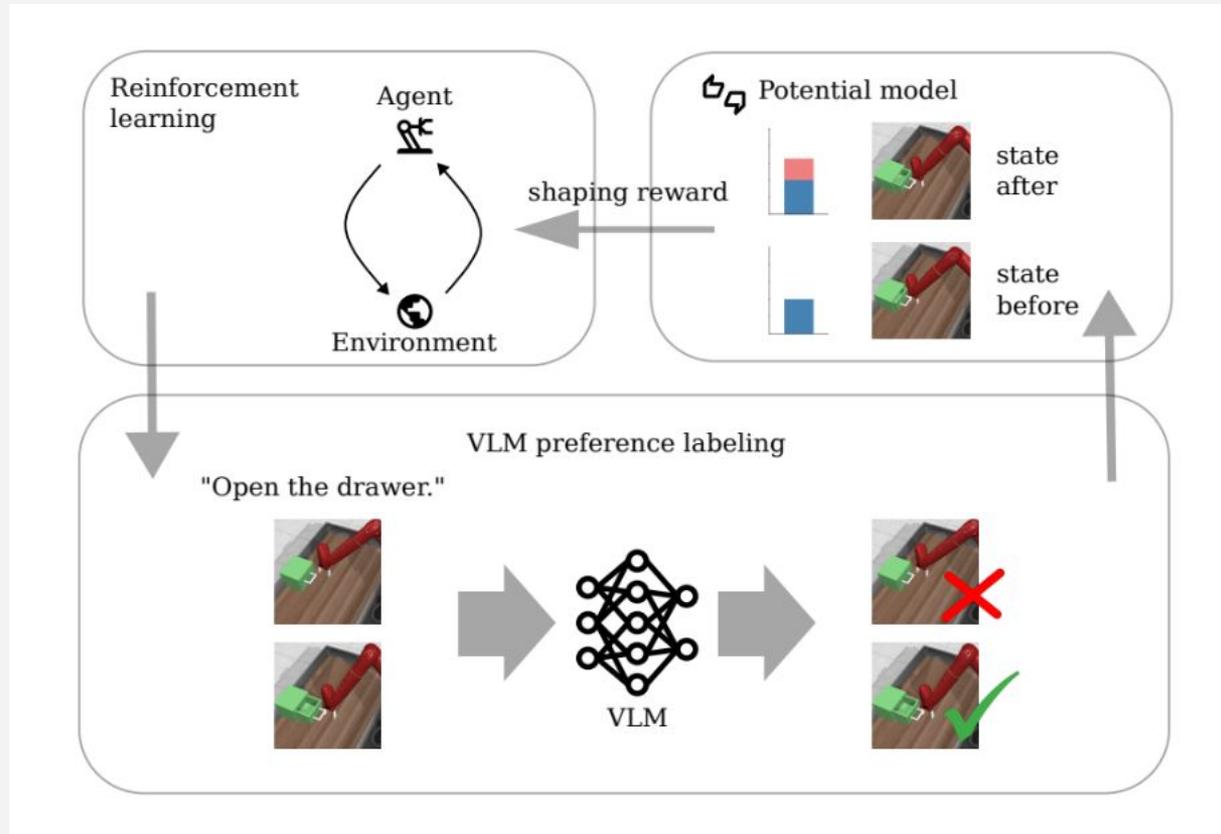
Bradley-Terry-Luce (BTL) preference model

Bradley, Ralph Allan, and Milton E. Terry. "Rank analysis of incomplete block designs: I. the method of paired comparisons." *Biometrika* 39, no. 3/4 (1952): 324-345.

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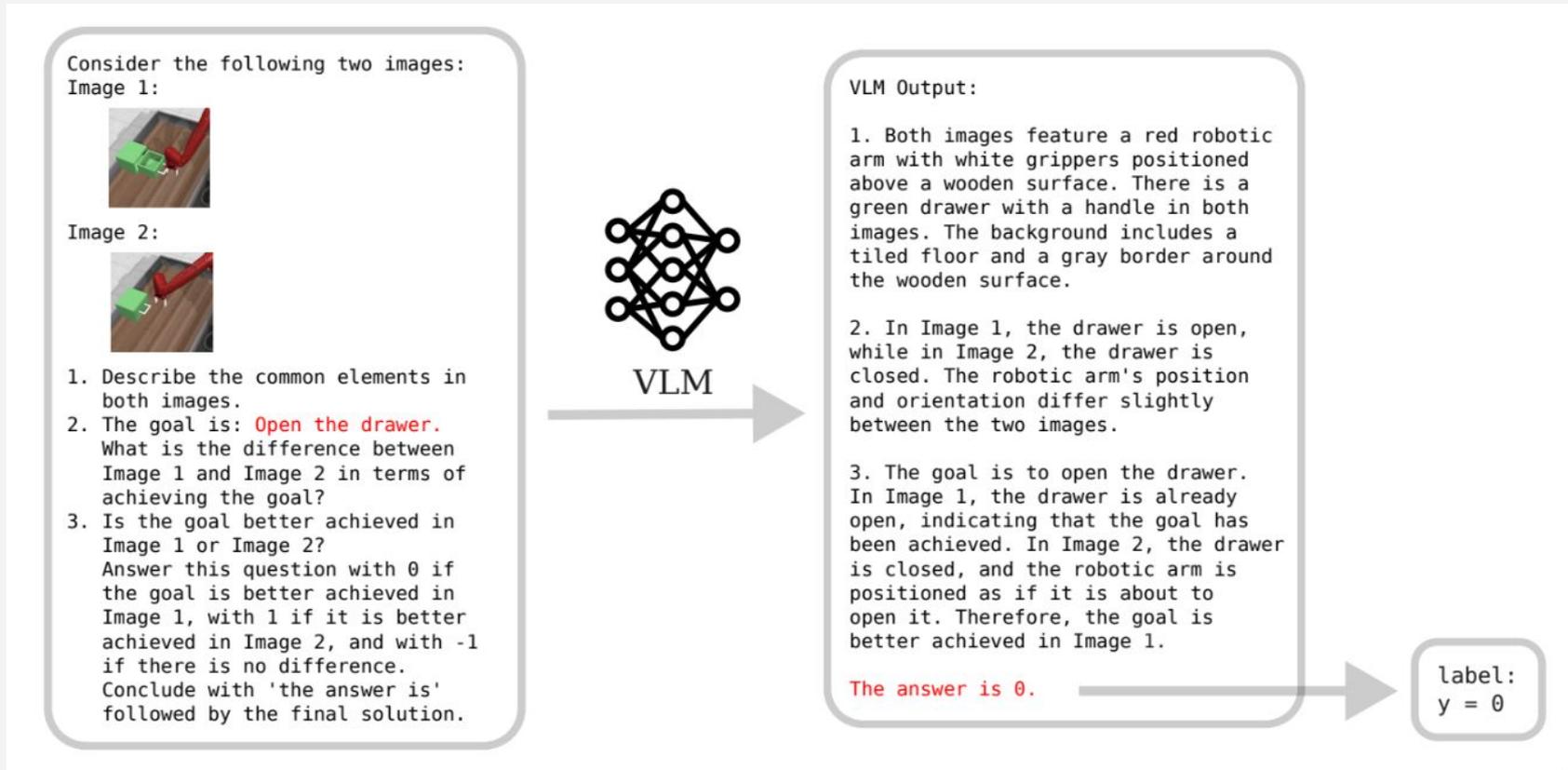
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Aligned To?

- Small set of english-speaking raters trained to have high inter-rater agreement with **OpenAI researchers**
- Values and preferences for labeling decided by OpenAI researchers
- Training data from OpenAI customers

Pluralistic Alignment



Is it ok for governments to moderate the social media content available to public?

Pluralistic Human Values



Overton



Many think that it's not okay for the government to moderate content as it endangers liberty, while others deem it acceptable for prevention of terrorism. A few, on the other hand, think it's necessary for sovereignty.

Steerable



- It is ok for the government to moderate content for terrorism and threats.
- or
- It is not ok to moderate any content as it endangers liberty.
- or
- It is ok for the government to moderate content that endangers its sovereignty.

Distributional



Divergent Preferences

Language

- conform to writing style
- preferences for verbosity

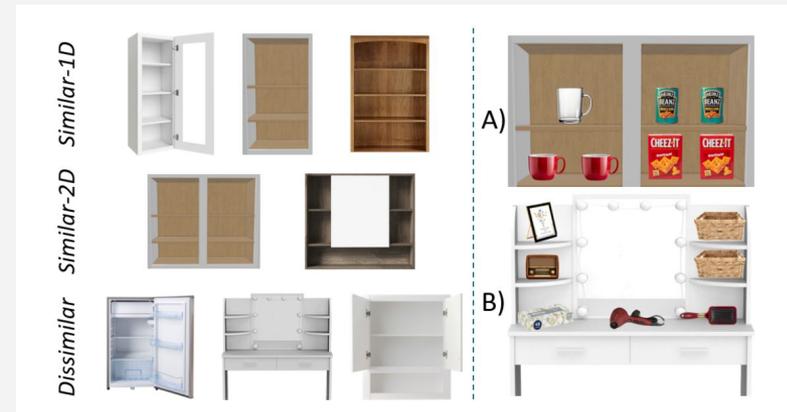
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Robotics

- Personalization

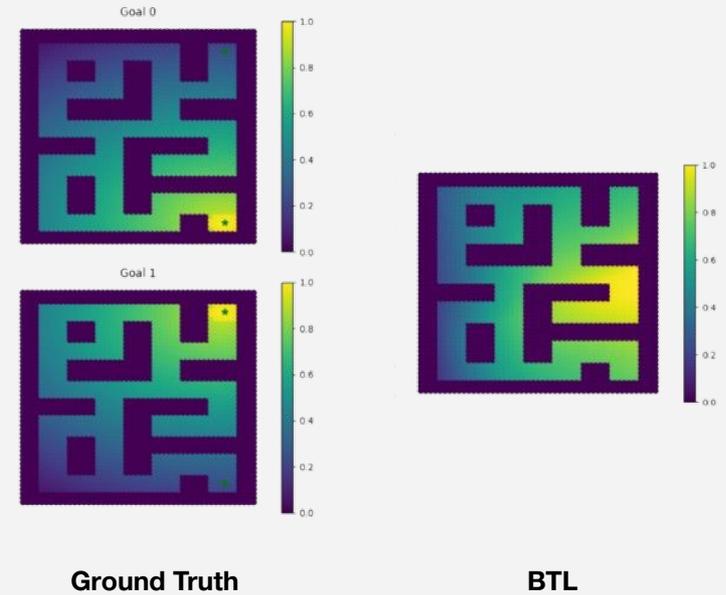


Can the BTL Model Consolidate Diverse Feedback?

- **No.**

“RLHF will ignore the preferences of minority groups if the majority population has a weak preference for an outcome that will severely disadvantage a minority group”

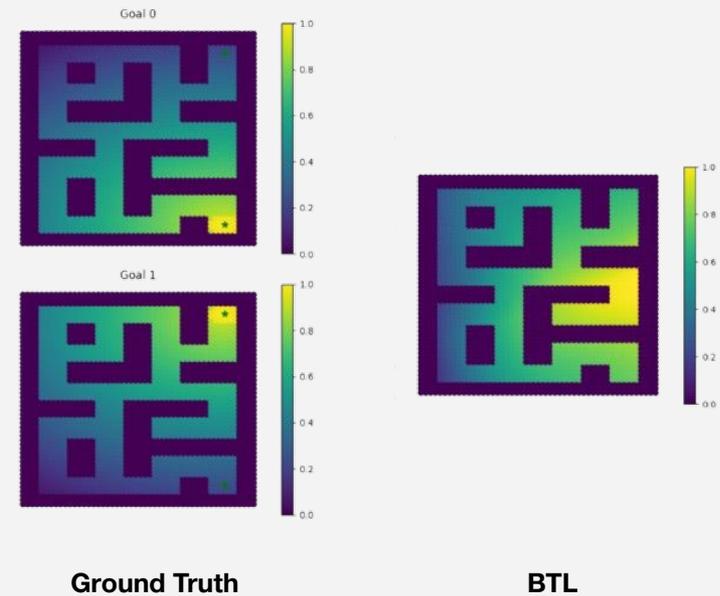
Divergent Preferences with BTL



Poddar, Sriyash, Yanming Wan, Hamish Ivison, Abhishek Gupta, and Natasha Jaques. "Personalizing reinforcement learning from human feedback with variational preference learning." Advances in Neural Information Processing Systems 37 (2024): 52516-52544.

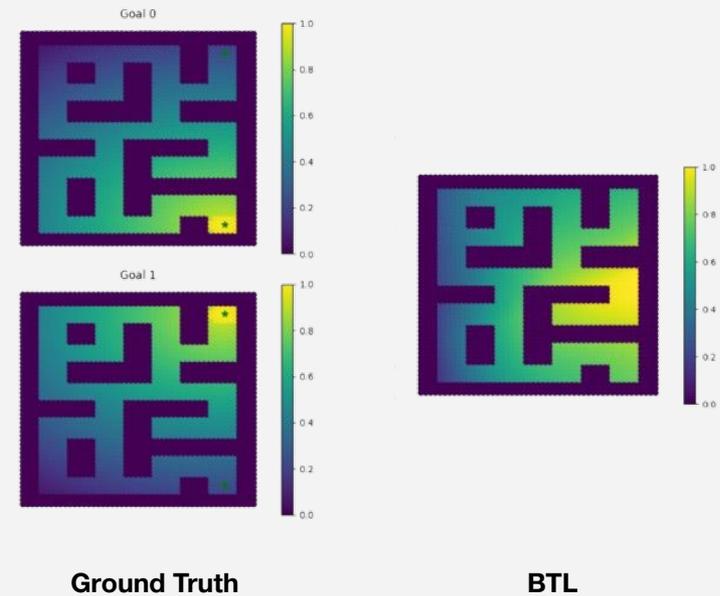
Divergent Preferences with BTL

- Maximizing likelihood under BTL results in a reward function that **averages modes**



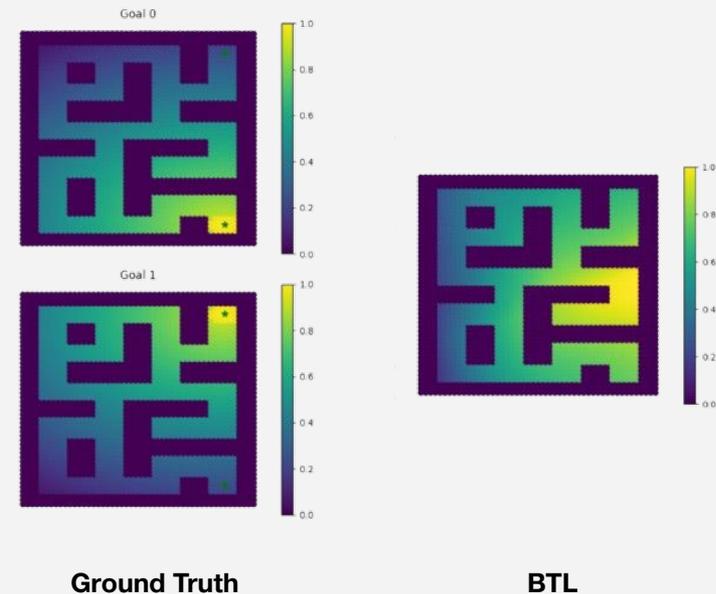
Divergent Preferences with BTL

- Maximizing likelihood under BTL results in a reward function that **averages modes**
- Can be **inaccurate for all users!**



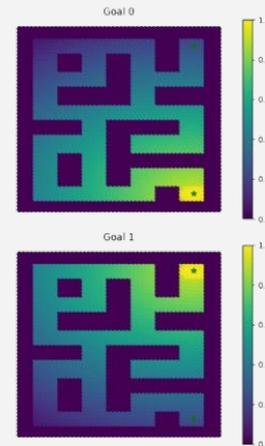
Divergent Preferences with BTL

- Maximizing likelihood under BTL results in a reward function that **averages modes**
- Can be **inaccurate for all users!**
- To get good performance, we need to **account for divergent preferences**

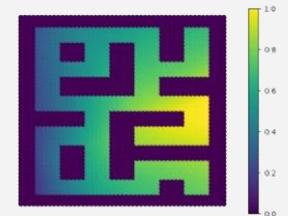


Divergent Preferences with BTL

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Ground Truth



BTL

Accommodating Divergent Preferences

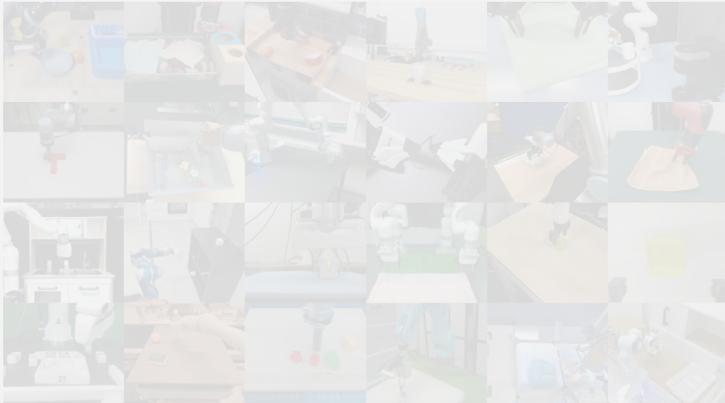


London, Alex John, and Hoda Heidari. "Beneficent intelligence: a capability approach to modeling benefit, assistance, and associated moral failures through AI systems." *Minds and Machines* 34, no. 4 (2024): 41.

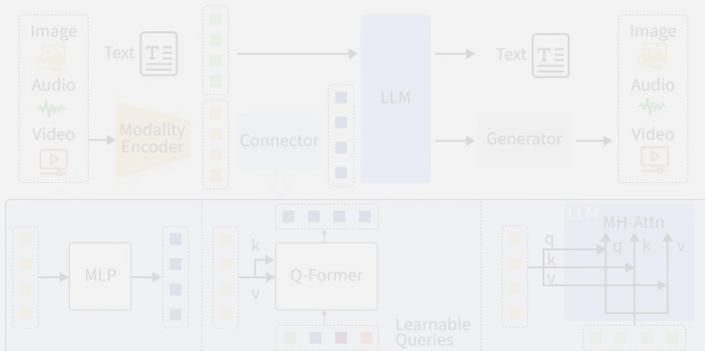
<https://ai-caring.org/>

The Anatomy of Foundation Model Training

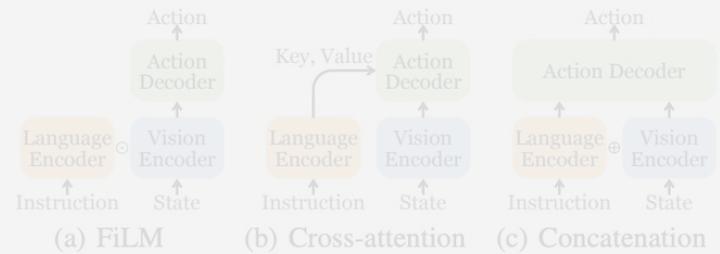
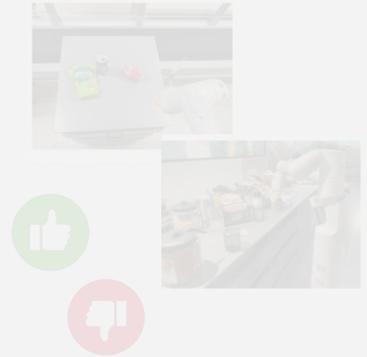
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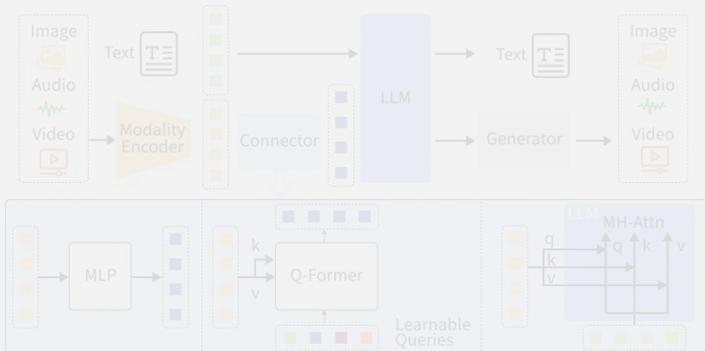
Brohan, Anthony, Noah Brown, Justice Carbajal, Yevgen Chebotar, Joseph Dabis, Chelsea Finn, Keerthana Gopalakrishnan et al. "Rt-1: Robotics transformer for real-world control at scale." arXiv preprint arXiv:2212.06817 (2022).

The Anatomy of Foundation Model Training

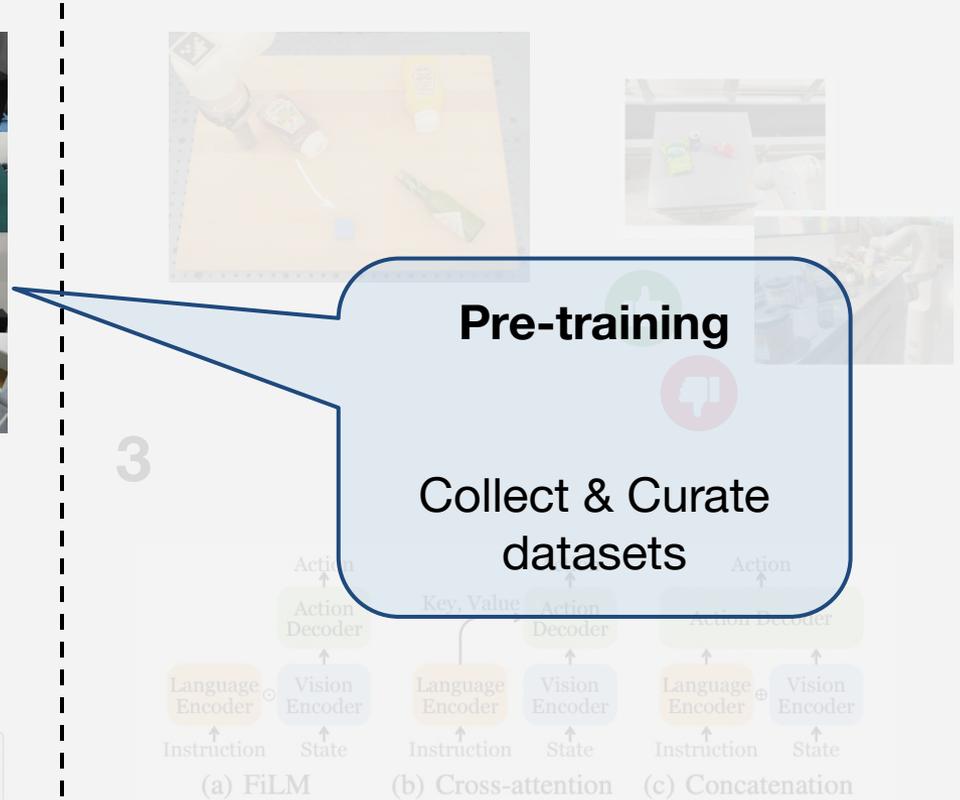
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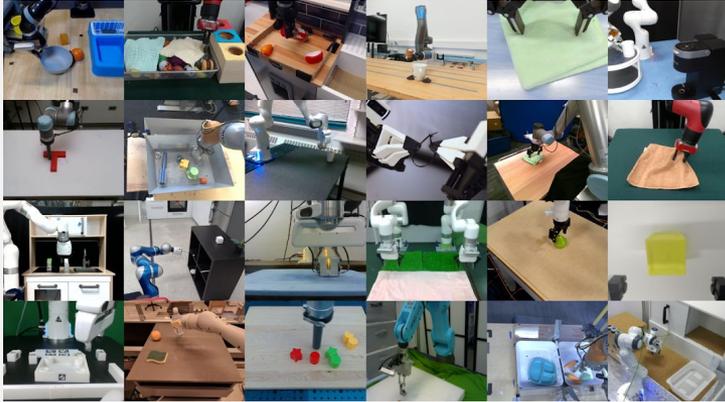
3



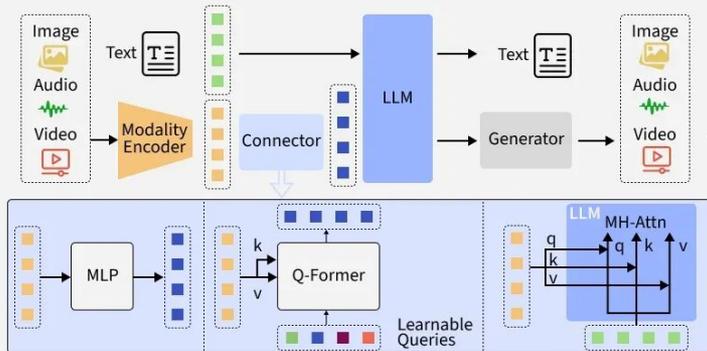
Brohan, Anthony, Noah Brown, Justice Carbajal, Yevgen Chebotar, Joseph Dabis, Chelsea Finn, Keerthana Gopalakrishnan et al. "Rt-1: Robotics transformer for real-world control at scale." arXiv preprint arXiv:2212.06817 (2022).

The Anatomy of Foundation Model Training

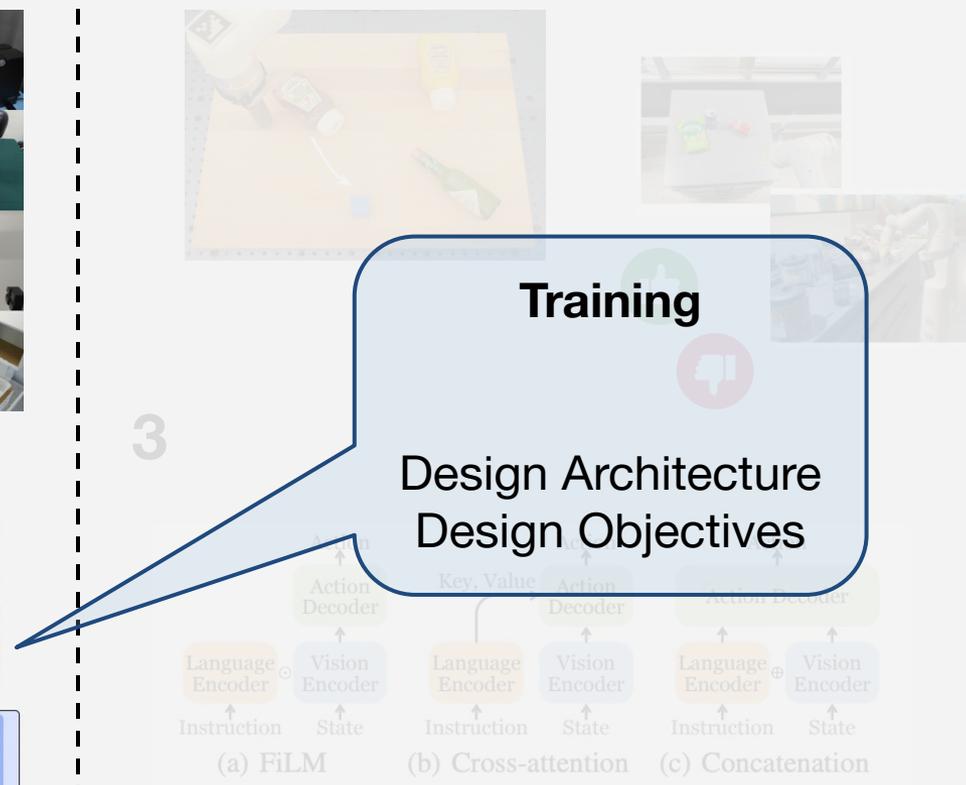
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2



3



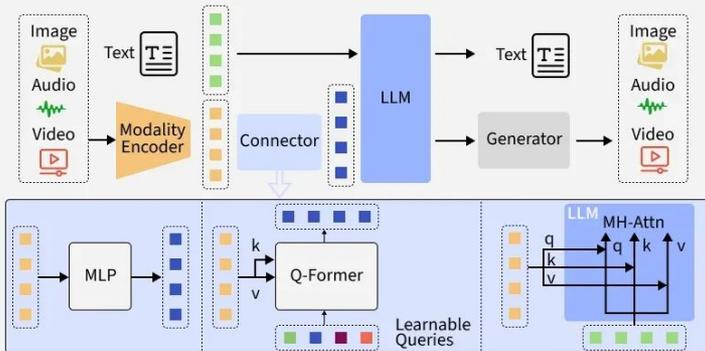
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The Anatomy of Foundation Model Training

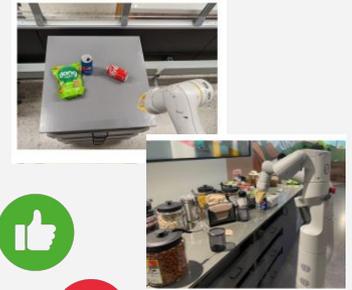
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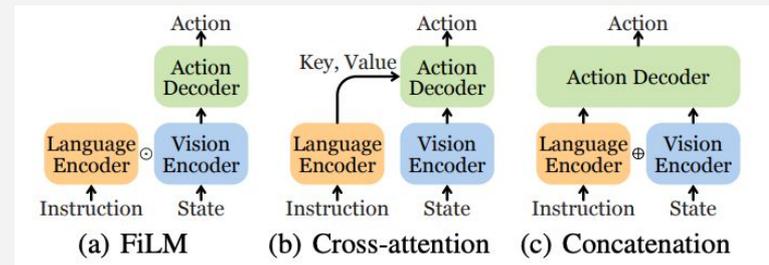
2



SFT Datasets
RLHF



3



Post-Training
Fine-Tuning
Alignment

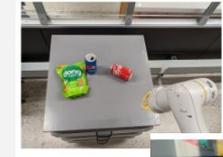
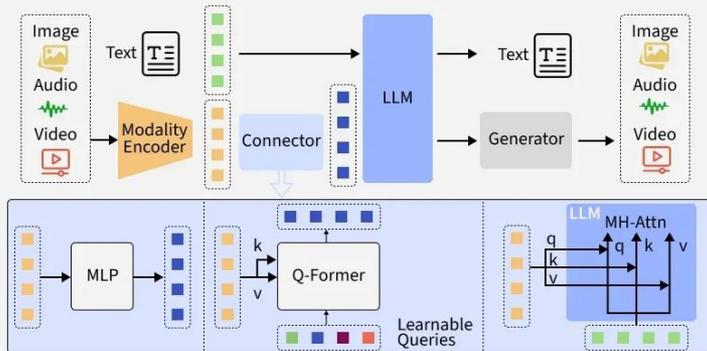
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The Anatomy of Foundation Model Training

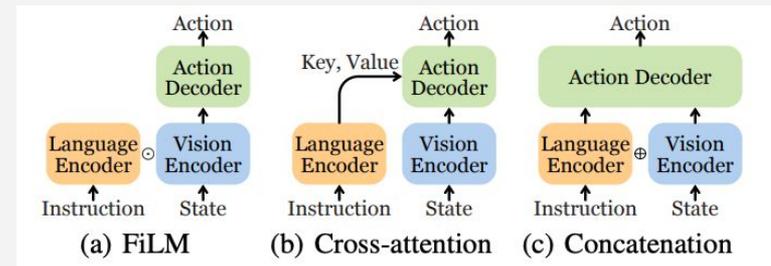
1



2



3



Brohan, Anthony, Noah Brown, Justice Carbajal, Yevgen Chebotar, Joseph Dabis, Chelsea Finn, Keerthana Gopalakrishnan et al. "Rt-1: Robotics transformer for real-world control at scale." arXiv preprint arXiv:2212.06817 (2022).

Robotics Transformer



Brohan, Anthony, Noah Brown, Justice Carbajal, Yevgen Chebotar, Joseph Dabis, Chelsea Finn, Keerthana Gopalakrishnan et al. "Rt-1: Robotics transformer for real-world control at scale." arXiv preprint arXiv:2212.06817 (2022).

Generative Modeling

Supervised vs Unsupervised

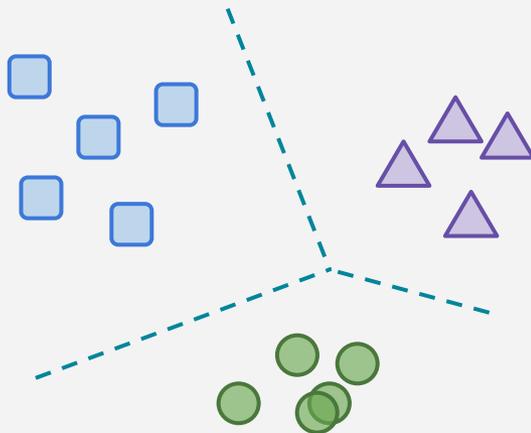
Supervised Learning

Data: (x, y)

x is data, y is label

Goal: Learn a function that maps

$$x \rightarrow y$$



Unsupervised Learning

Data: x

x is data, no labels

Goal: Learn the hidden or underlying structure of the data x

Supervised vs Unsupervised

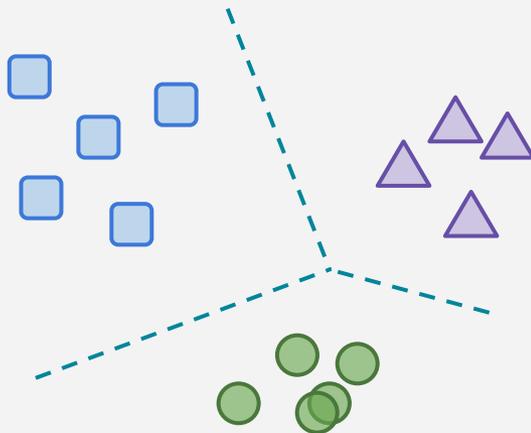
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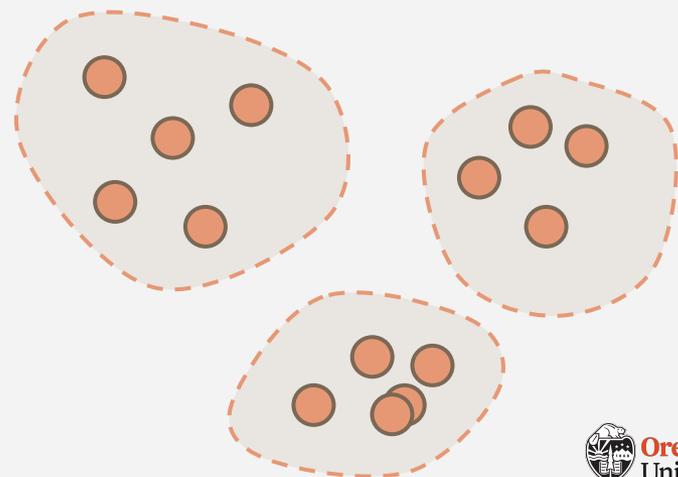


Unsupervised Learning

Data: x

x is data, no labels

Goal: Learn the hidden or underlying structure of the data x



Generative Modeling

Goal: Learn a model that represents a target distribution

Data: Samples from the target distribution

Generative Modeling

Goal: Learn a model that represents a target distribution

Data: Samples from the target distribution

Density Estimation

Generative Modeling

Goal: Learn a model that represents a target distribution

Data: Samples from the target distribution

Density Estimation

samples

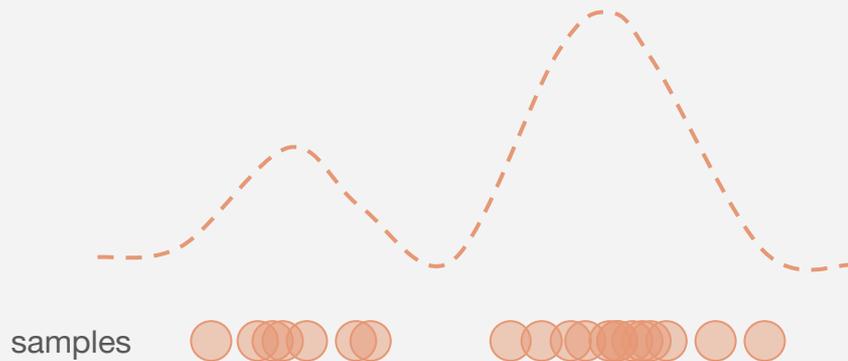


Generative Modeling

Goal: Learn a model that represents a target distribution

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Density Estimation

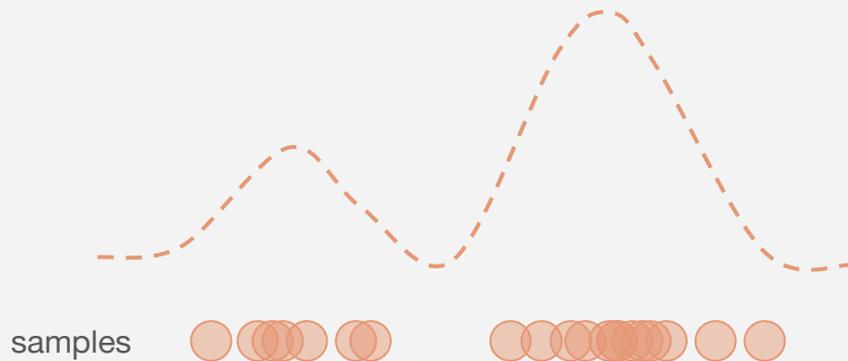


Generative Modeling

Goal: Learn a model that represents a target distribution

Data: Samples from the target distribution

Density Estimation



Sample Generation



Input samples

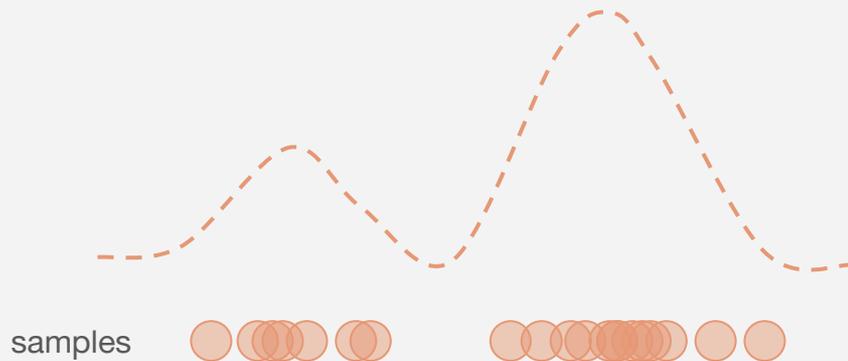
Training data $\sim P_{data}(x)$

Generative Modeling

Goal: Learn a model that represents a target distribution

Data: Samples from the target distribution

Density Estimation



Sample Generation



Input samples



Generated samples

Training data $\sim P_{data}(x)$

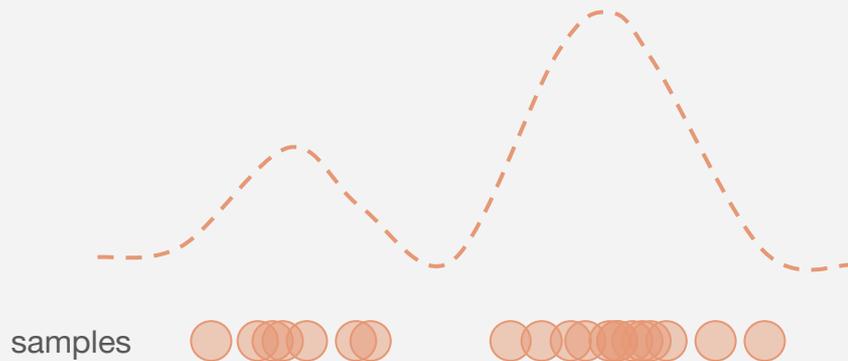
Generated $\sim P_{model}(x)$

Generative Modeling

Goal: Learn a model that represents a target distribution

Data: Samples from the target distribution

Density Estimation



Sample Generation



Input samples



Generated samples

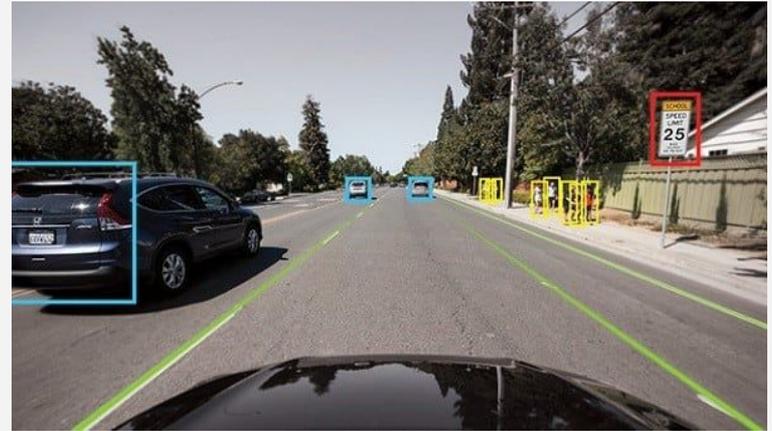
Training data $\sim P_{data}(x)$

Generated $\sim P_{model}(x)$

How can we learn $P_{model}(x)$ similar to $P_{data}(x)$?

Outlier Detection

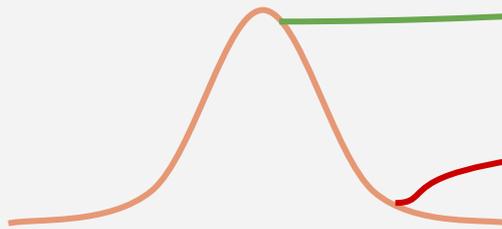
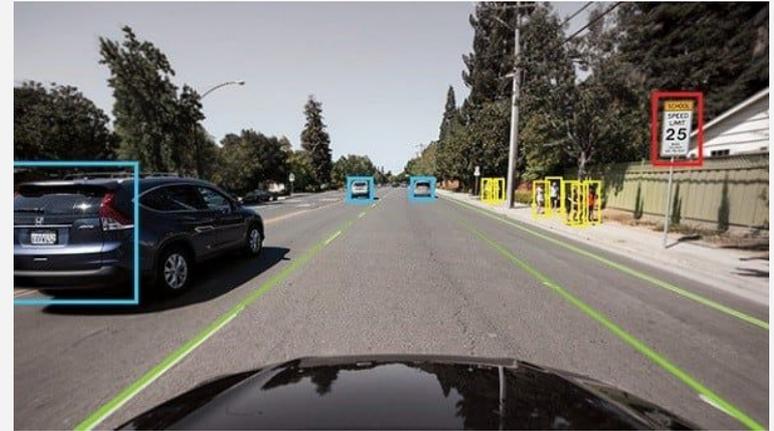
How can we detect when we encounter something new or rare?



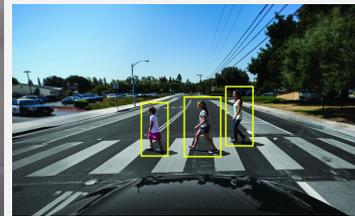
Outlier Detection

How can we detect when we encounter something new or rare?

Strategy: Leverage generative models, detect outliers in the distribution



Harsh Conditions



Pedestrians



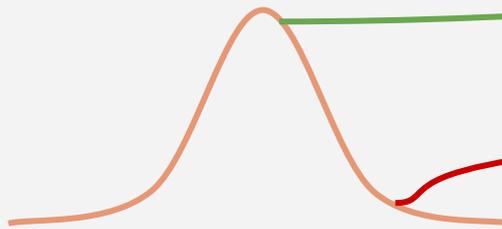
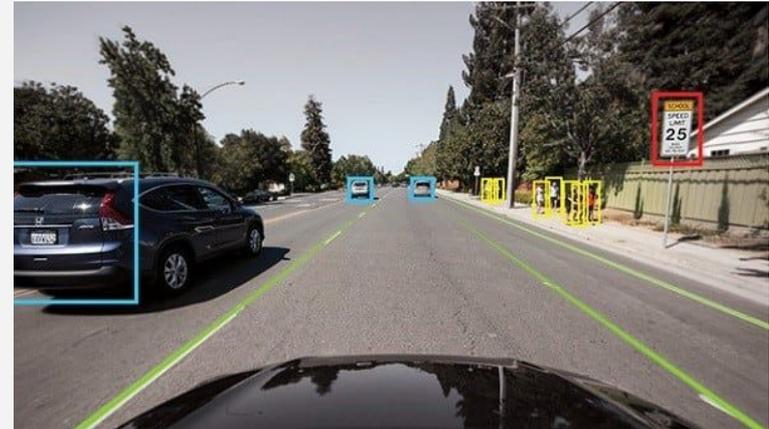
Edge Cases?

Outlier Detection

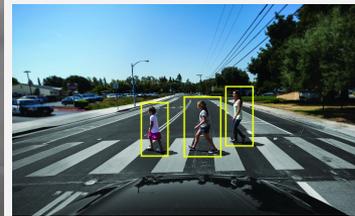
How can we detect when we encounter something new or rare?

Strategy: Leverage generative models, detect outliers in the distribution

Goal: Use outliers during training to improve!



Harsh Conditions



Pedestrians



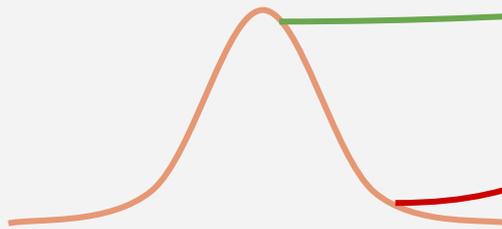
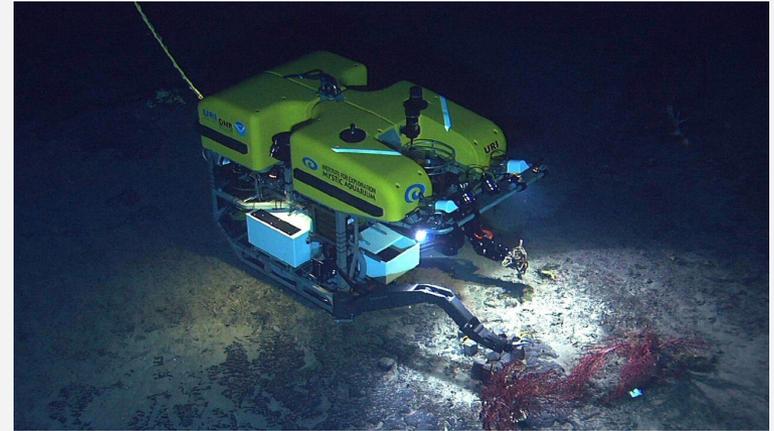
Edge Cases?

Outlier Detection

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Harsh Conditions



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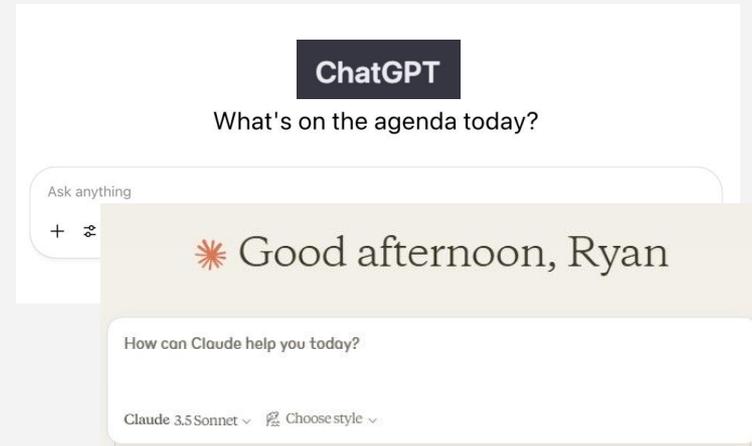
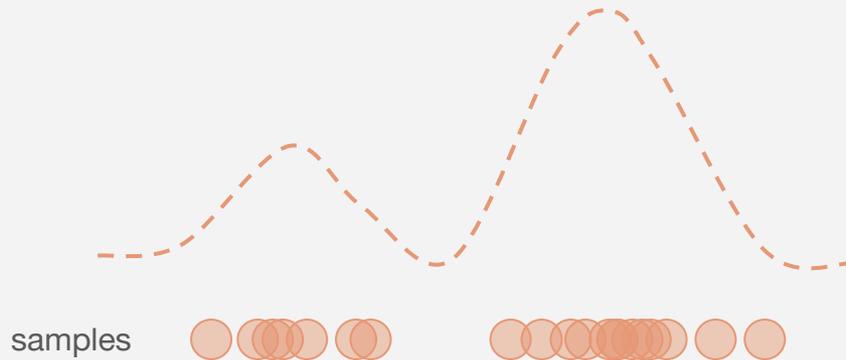


Edge Cases?

Generative Models

Generative models learn probability distributions

Sampling from the learnt distribution produces new data instances.



Natural Language

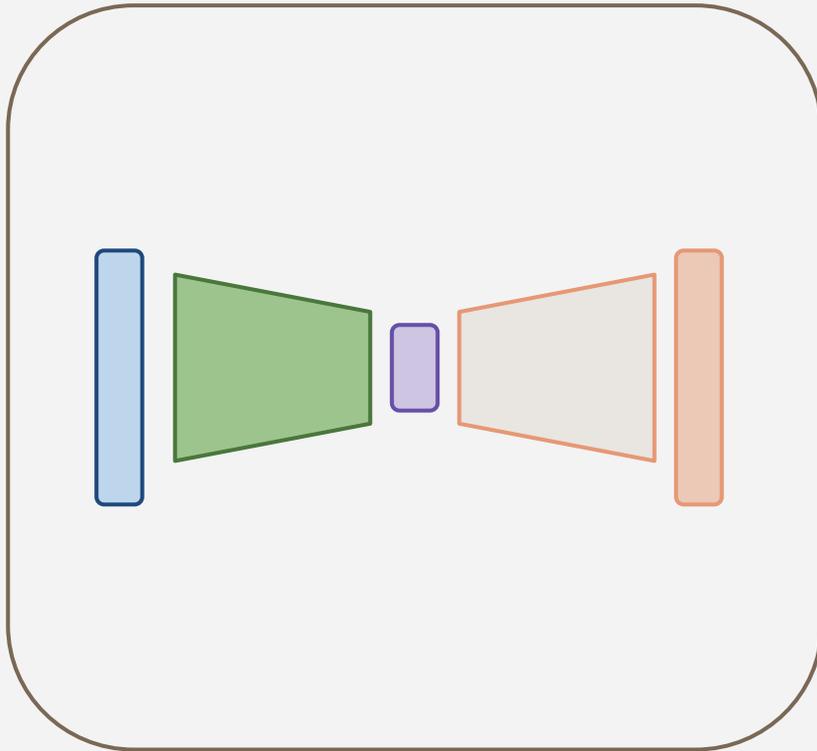


Vision / Action

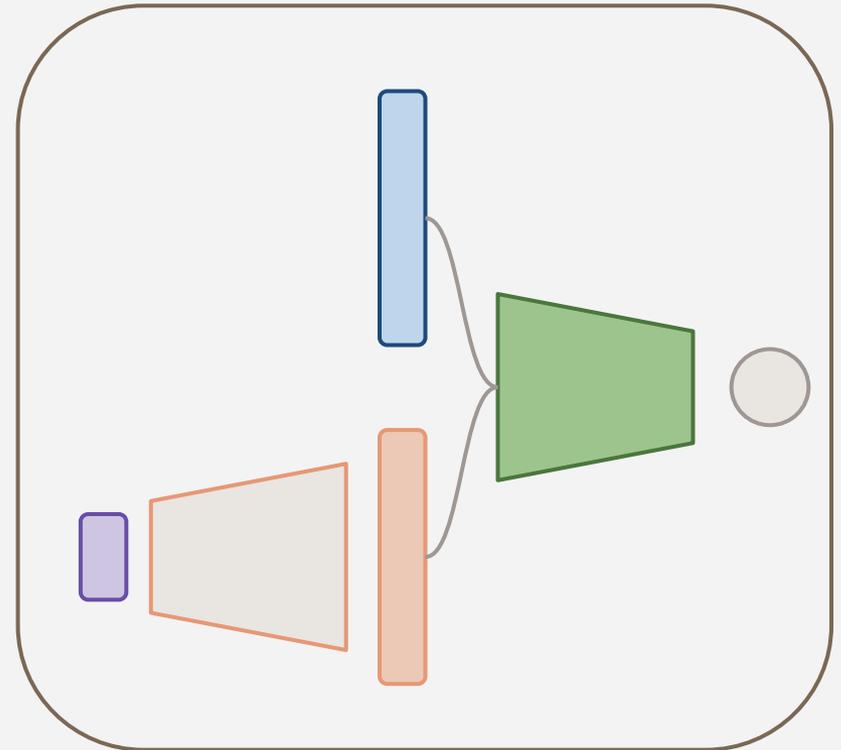


Images

Latent Variable Models

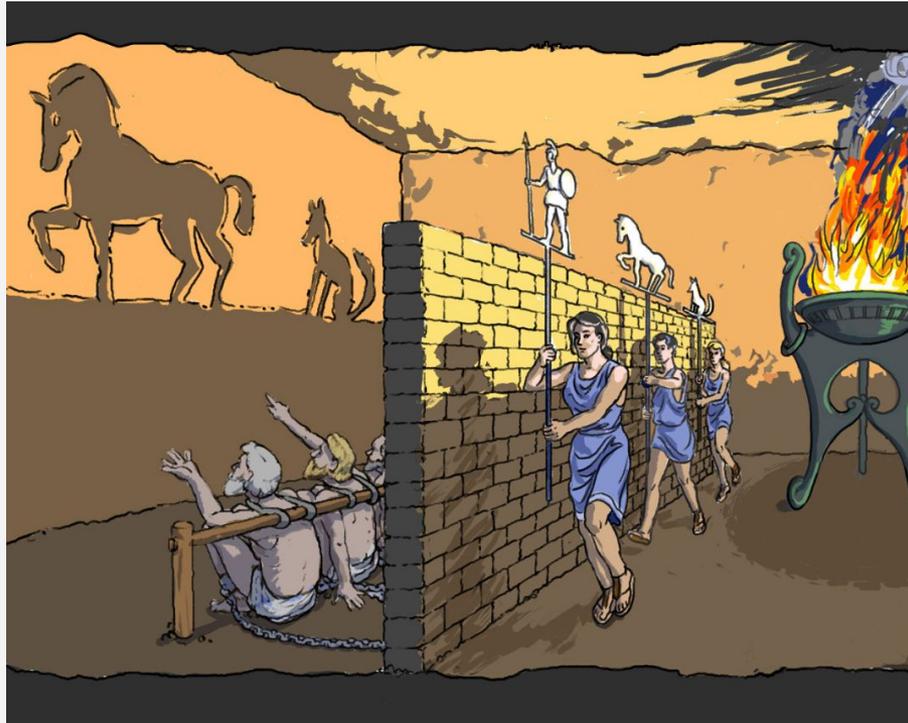


Autoencoders



Generative Adversarial Networks (GANs)

Latent Variables



The Allegory of the Cave

Latent Variables

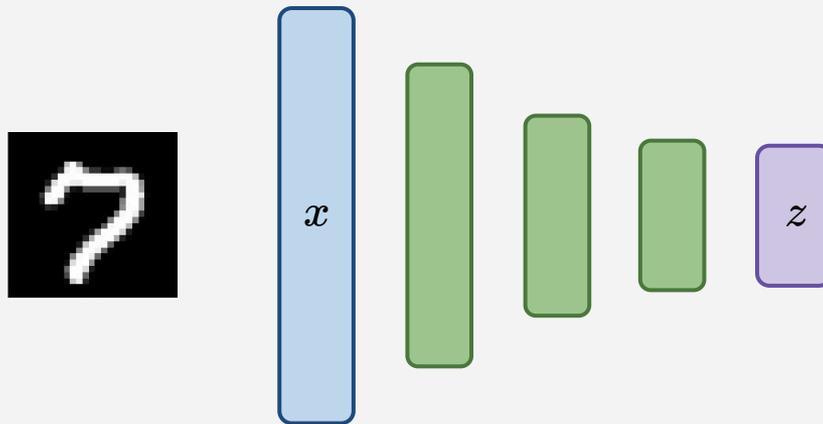


Can we learn the true **explanatory factors** from merely observed data?

Autoencoders

Autoencoders

Unsupervised approach to learn a **lower-dimensional feature** representation from unlabeled training data

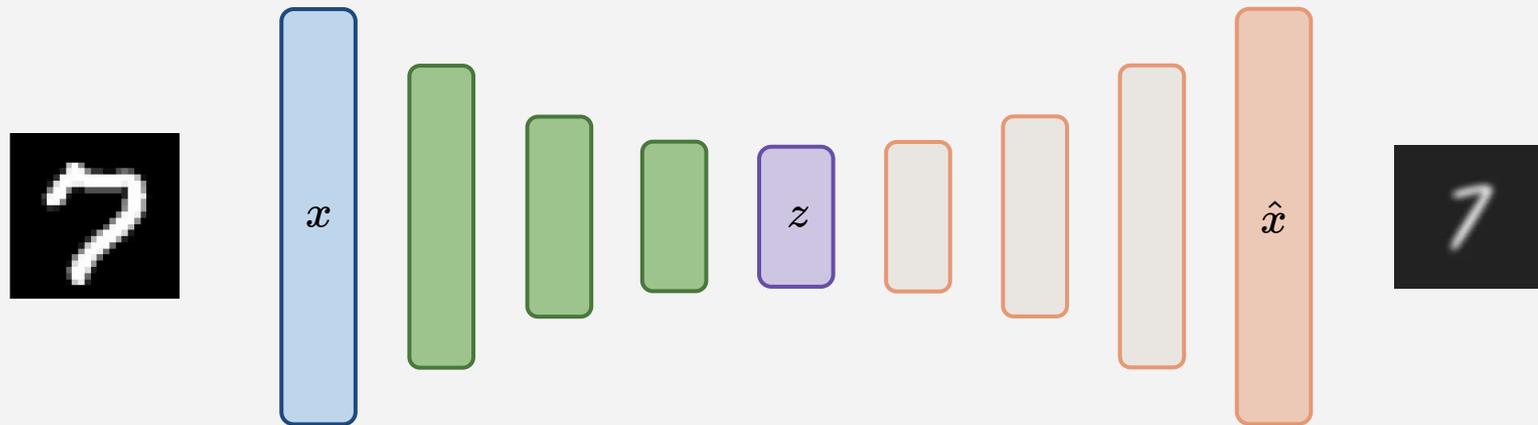


“Encoder” learns to map data x to a low-dimensional latent space z

Autoencoders

How can we learn this latent space?

Train the model to learn features that **reconstruct the original data**

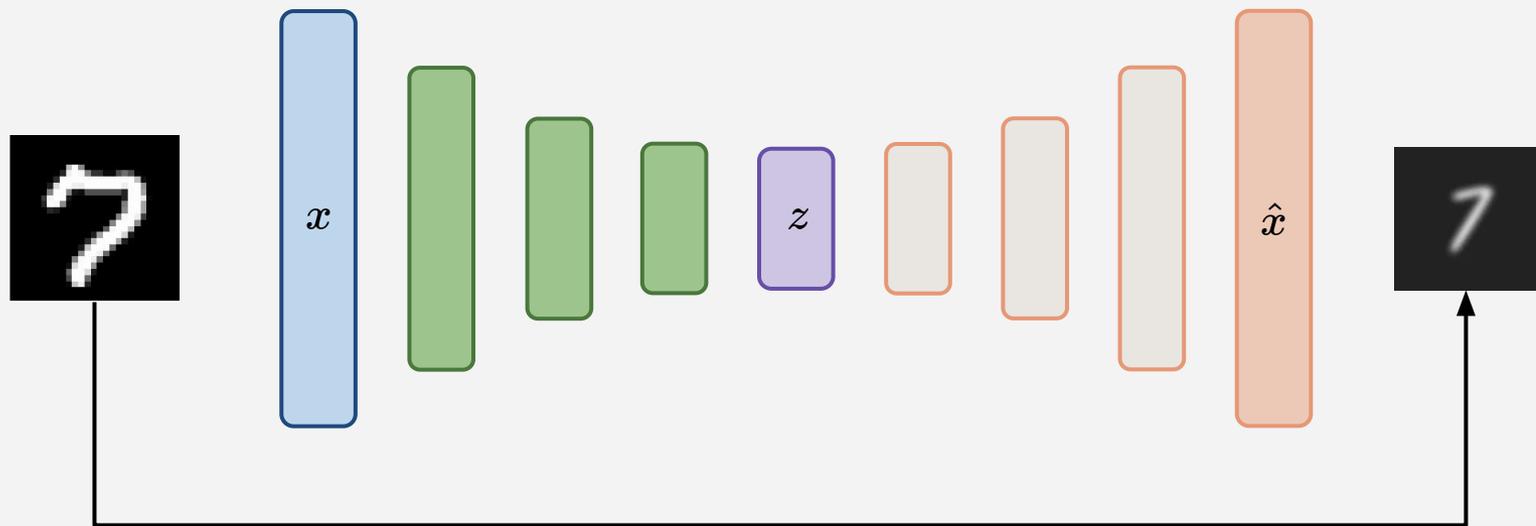


“Decoder” learns to map back from latent space z to a reconstructed observation \hat{x}

Autoencoders

How can we learn this latent space?

Train the model the learn features that **reconstruct the original data**



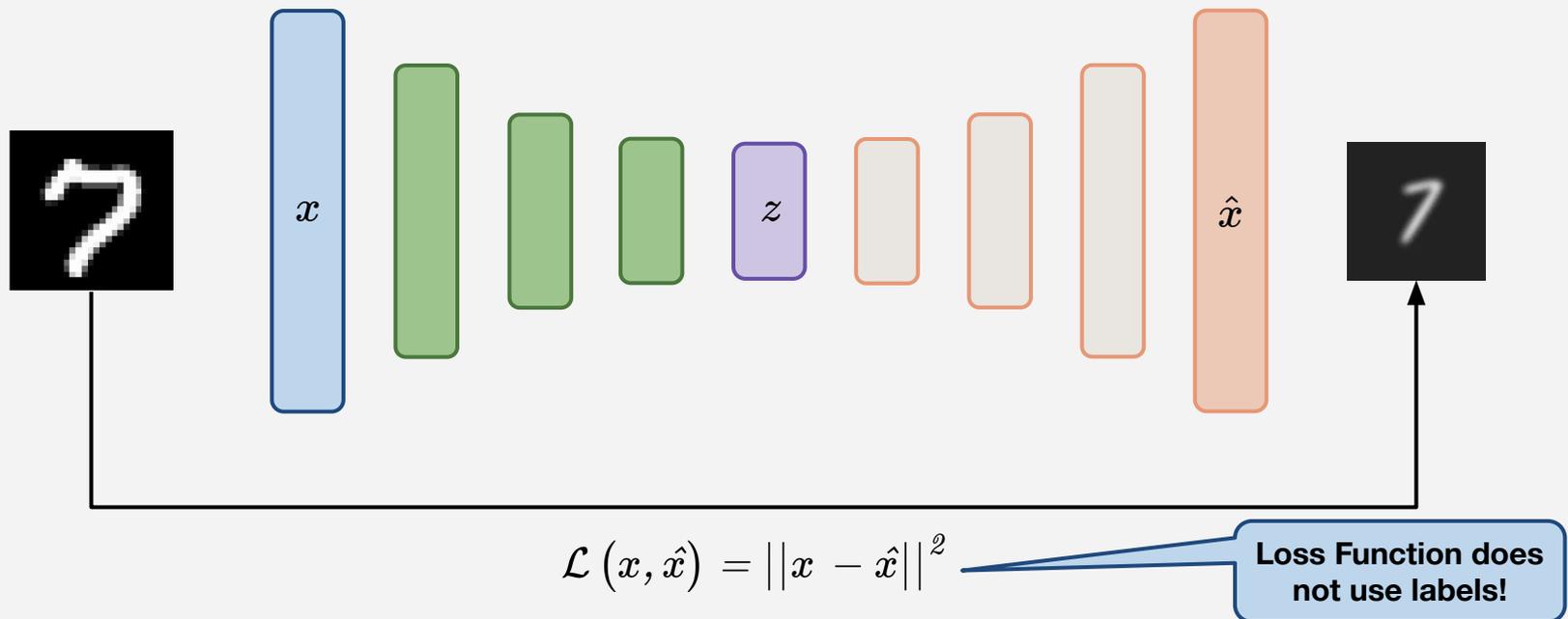
$$\mathcal{L}(x, \hat{x}) = ||x - \hat{x}||^2$$

“Decoder” learns to map back from latent space z to a reconstructed observation \hat{x}

Autoencoders

How can we learn this latent space?

Train the model the learn features that **reconstruct the original data**

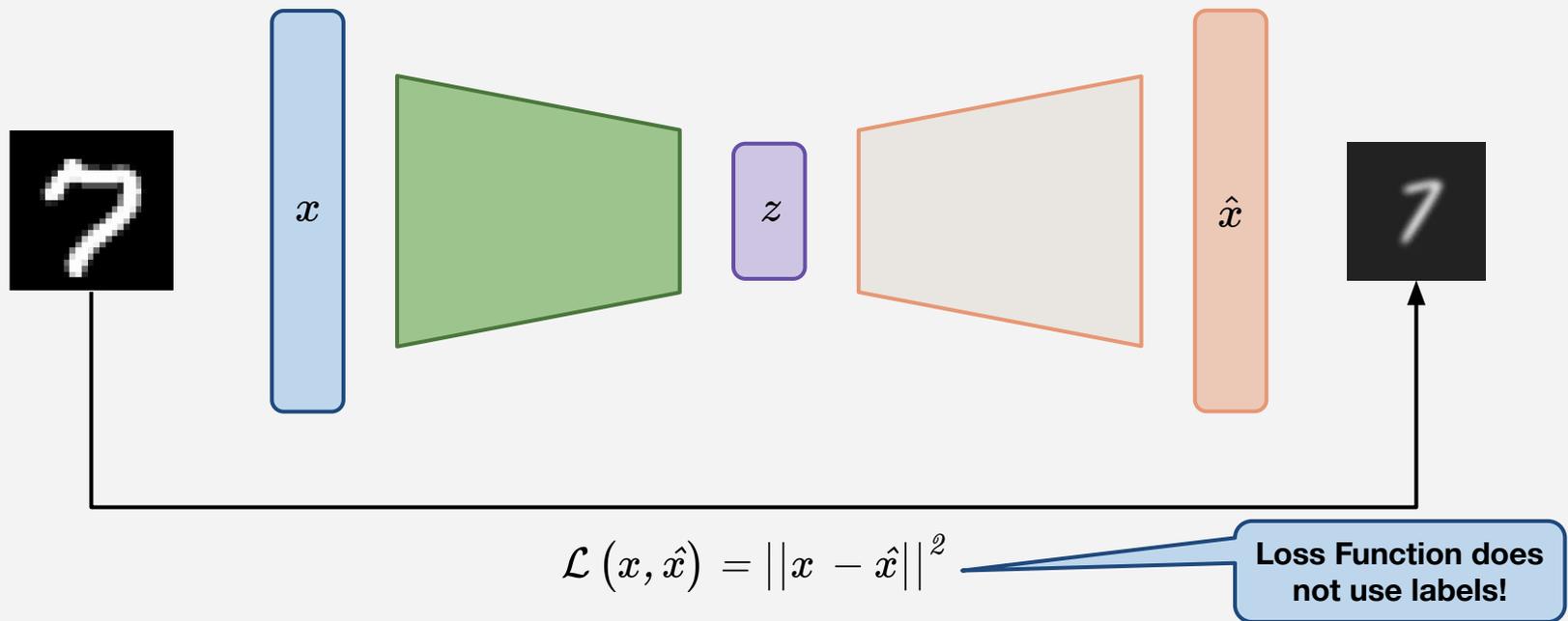


“Decoder” learns to map back from latent space z to a reconstructed observation \hat{x}

Autoencoders

How can we learn this latent space?

Train the model the learn features that **reconstruct the original data**



“Decoder” learns to map back from latent space z to a reconstructed observation \hat{x}

Reconstruction Quality

Autoencoding is a form of **compression**

Smaller latent space will force a larger training bottleneck



2D Latent Space



5D Latent Space

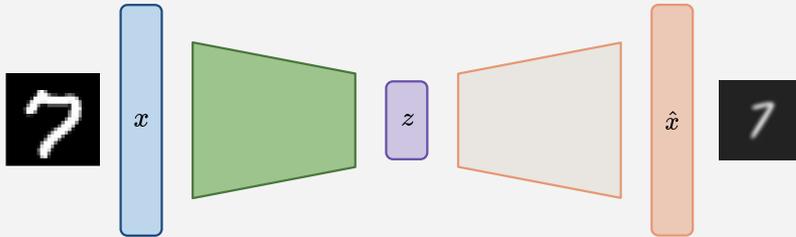


Ground Truth

Autoencoders for Representation Learning

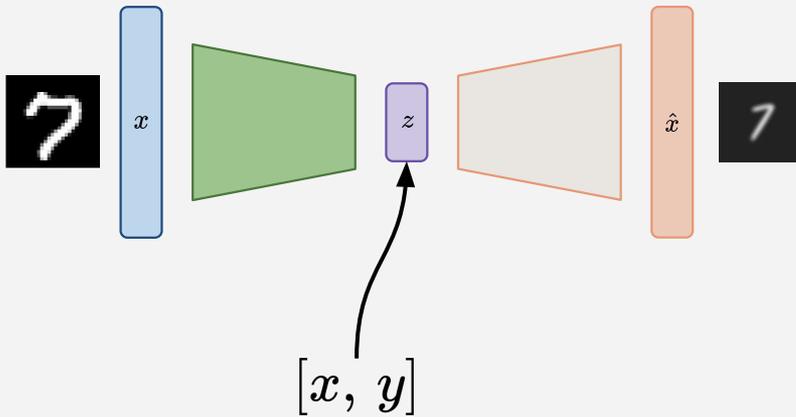
- **Bottleneck hidden layer** forces network to learn a compressed latent representation
- **Reconstruction loss** forces the latent representation to capture (“encode”) information about the data
- **Autoencoding** = **Automatically encoding** data; “Auto” = **self**-encoding (without labels)

Autoencoders for Representation Learning



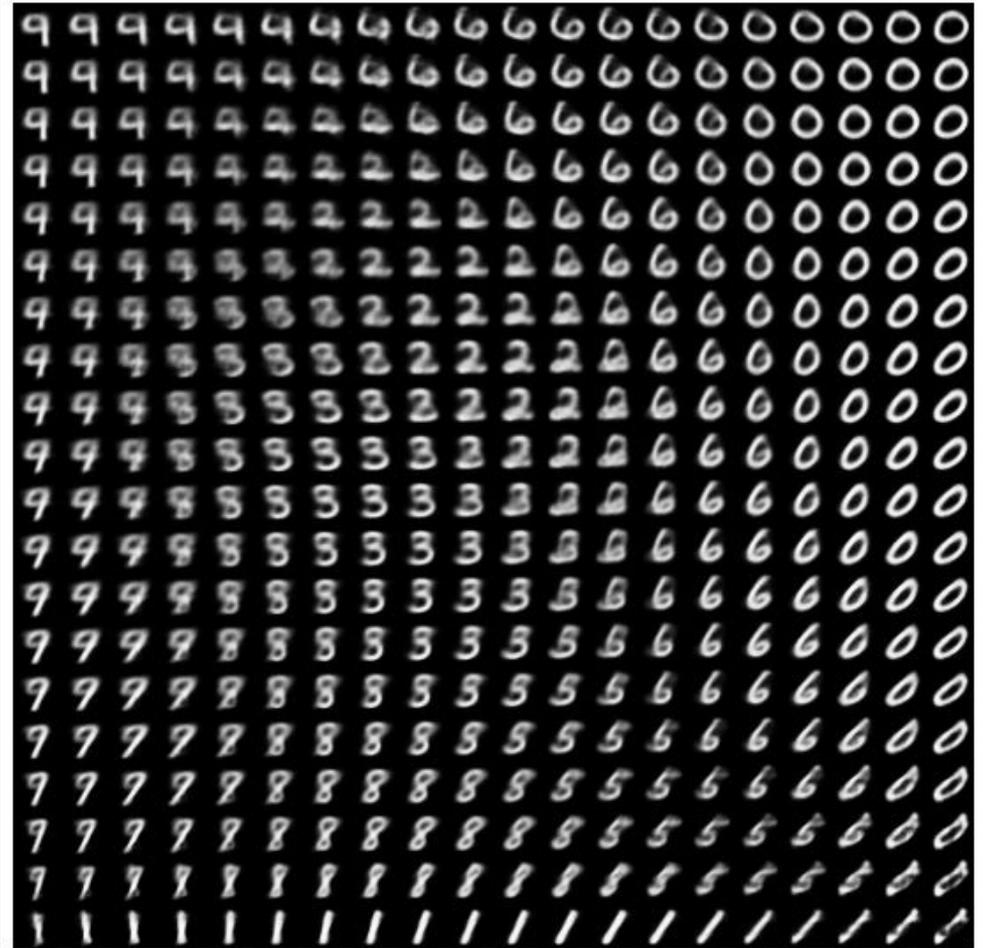
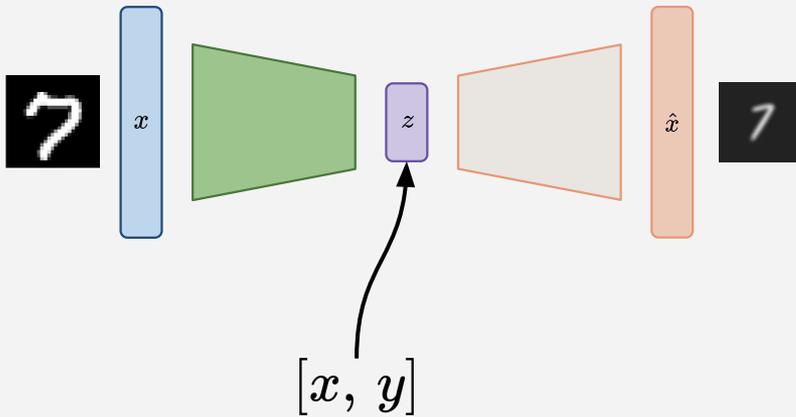
Kingma, Diederik P., and Max Welling. "Auto-encoding variational bayes." arXiv preprint arXiv:1312.6114 (2013).

Autoencoders for Representation Learning



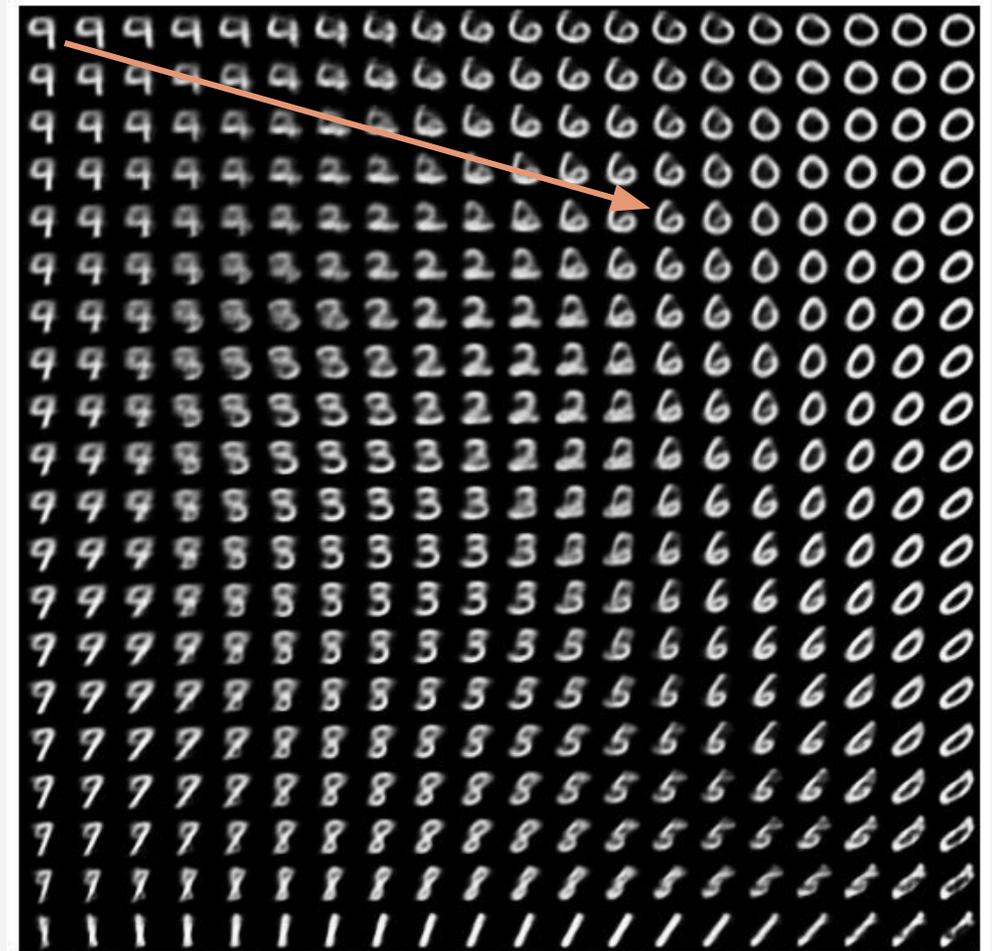
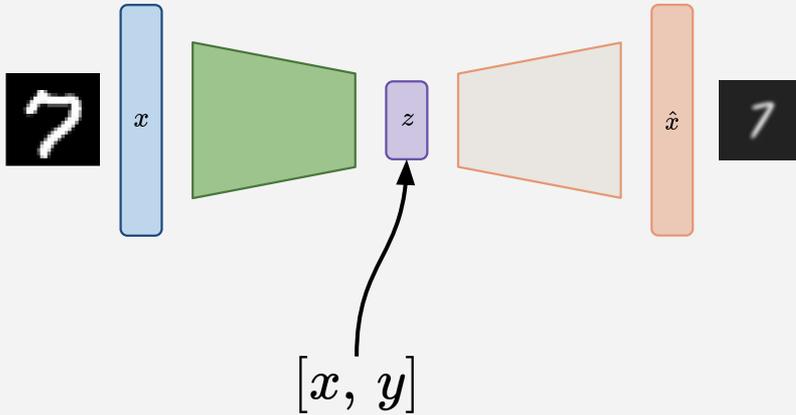
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Autoencoders for Representation Learning

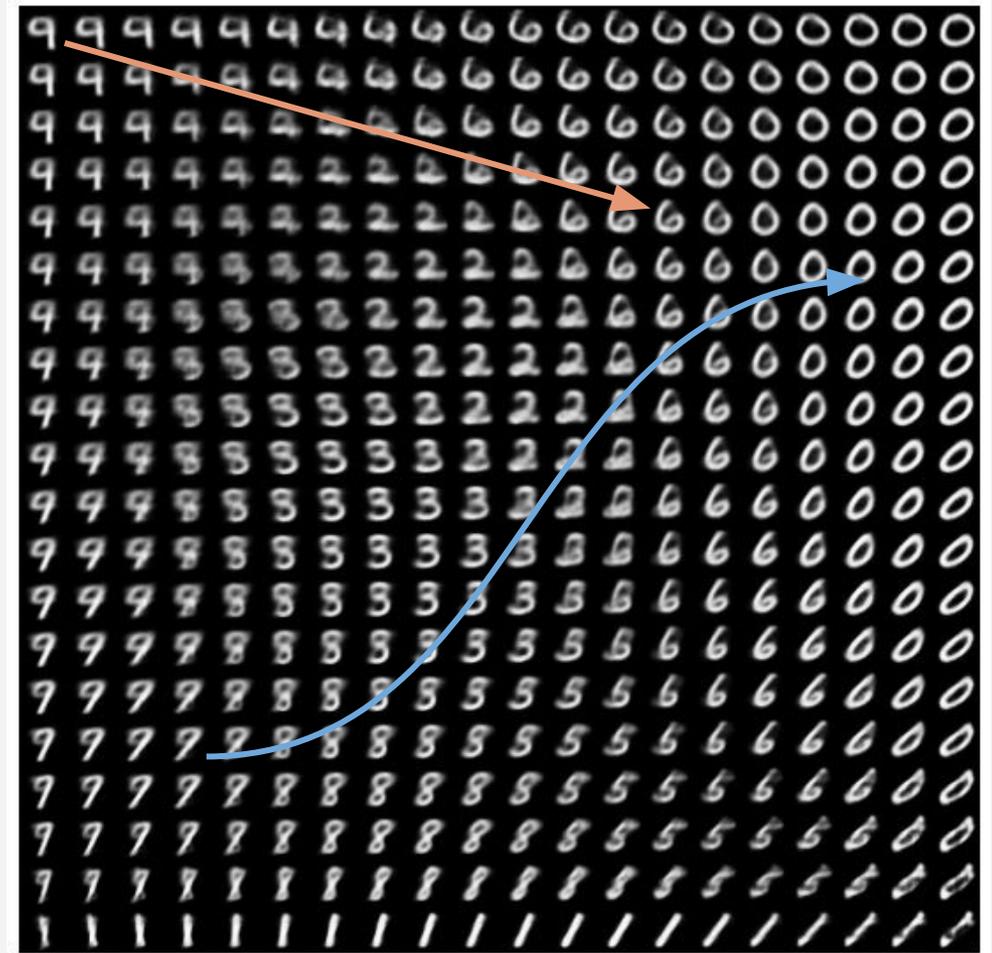
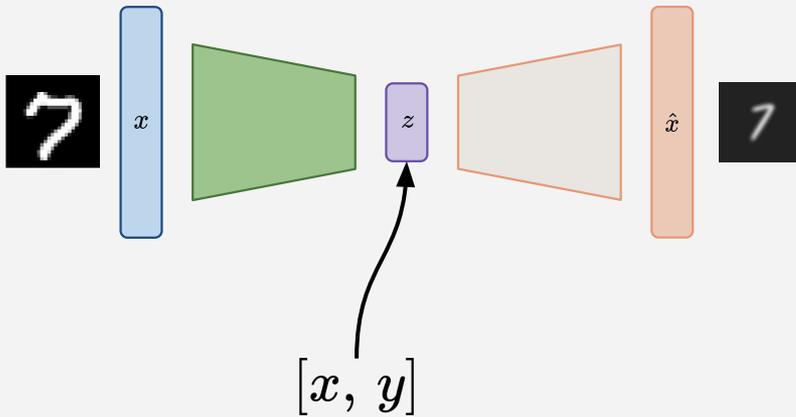


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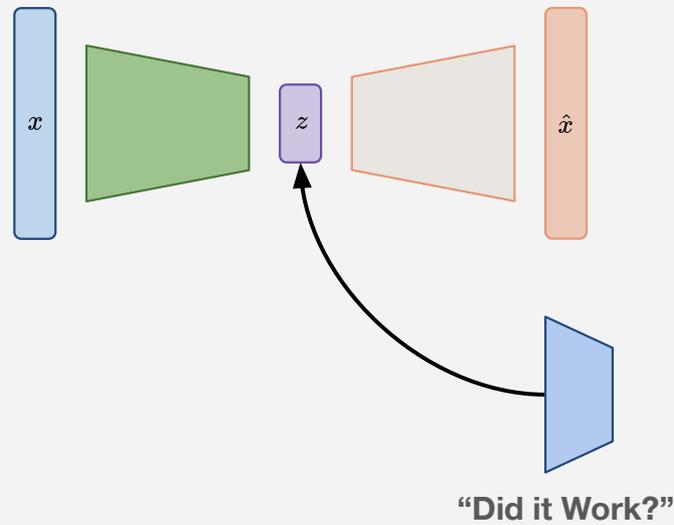
Autoencoders for Representation Learning



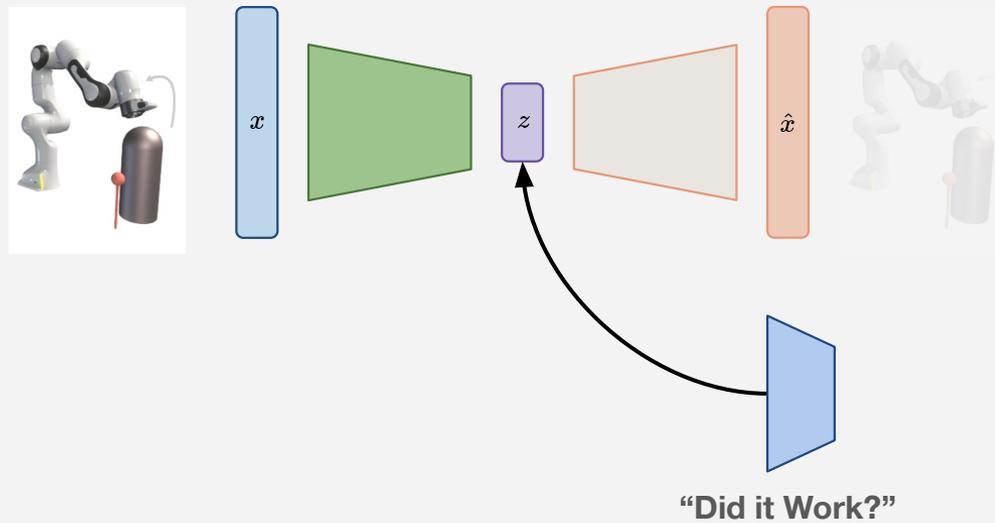
Autoencoders for Representation Learning



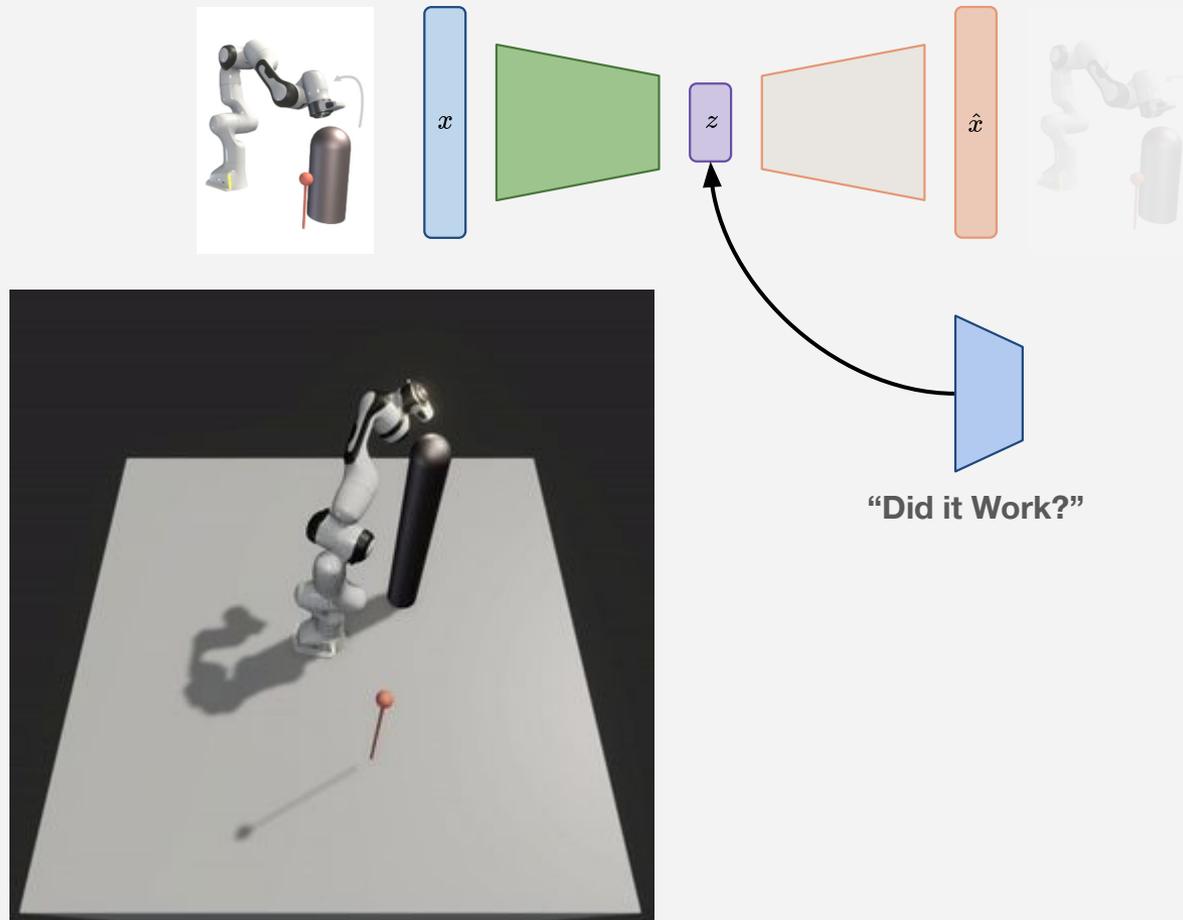
Walks in the Latent Space



Walks in the Latent Space

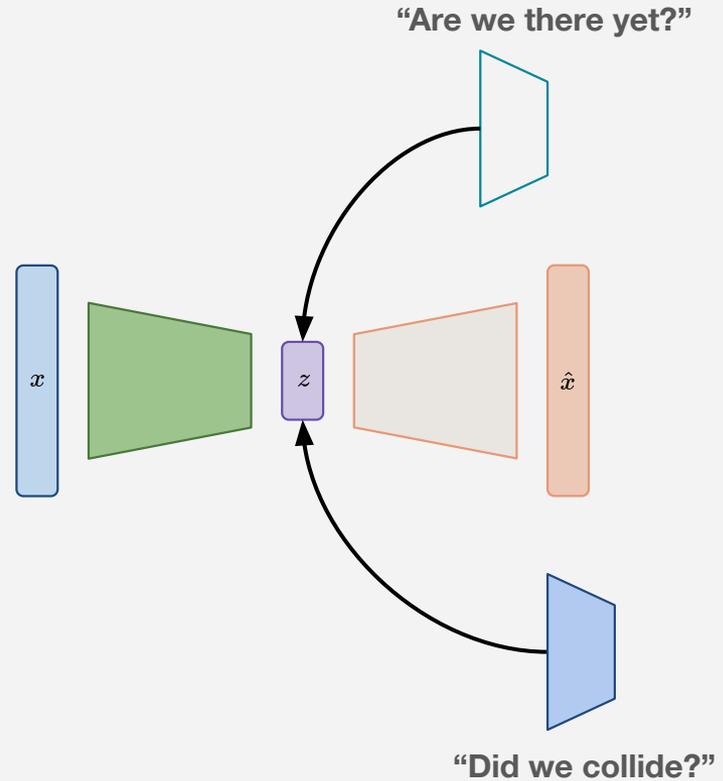
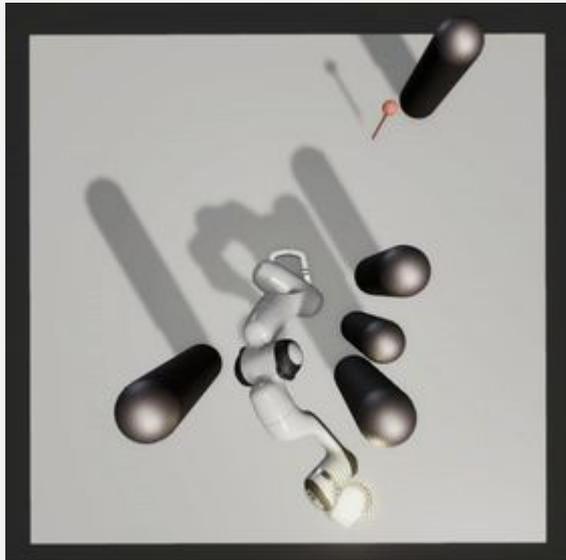


Walks in the Latent Space



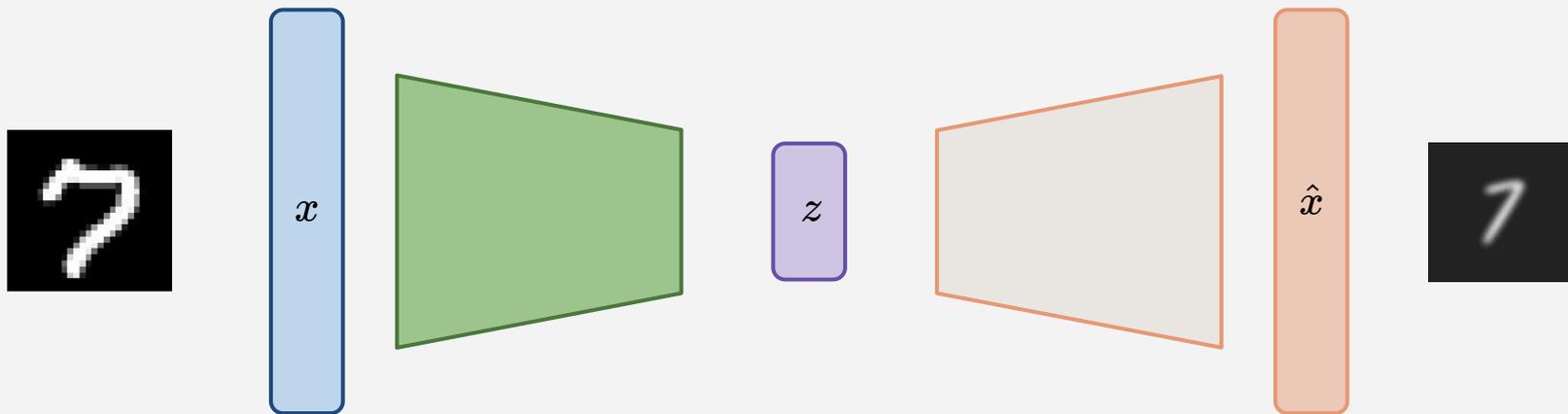
Hung, Chia-Man, Shaohong Zhong, Walter Goodwin, Oiwi Parker Jones, Martin Engelcke, Ioannis Havoutis, and Ingmar Posner. "Reaching through latent space: From joint statistics to path planning in manipulation." IEEE Robotics and Automation Letters 7, no. 2 (2022): 5334-5341.

Walks in the Latent Space

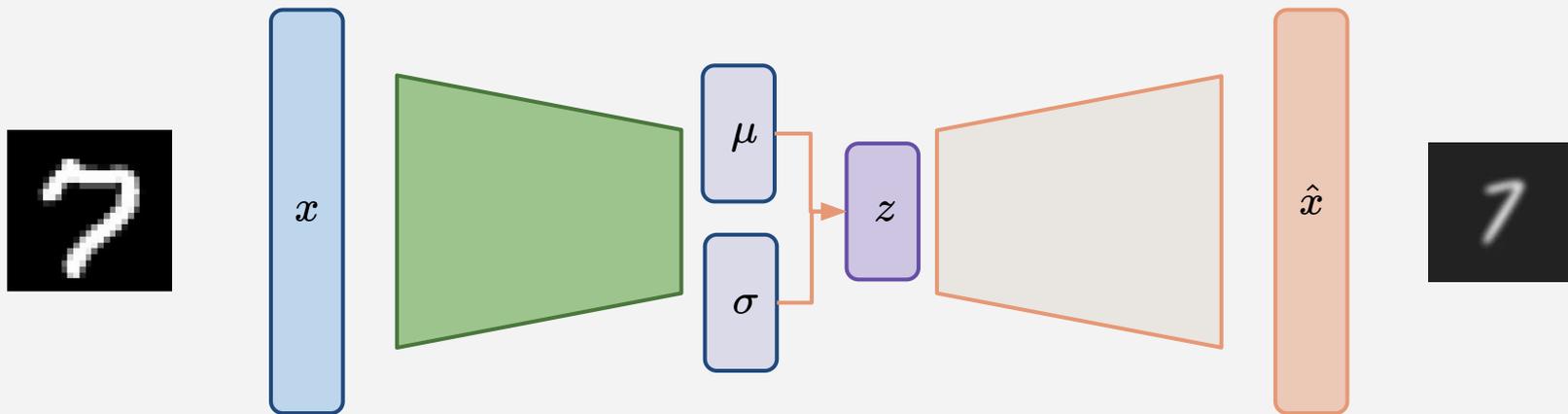


Variational Autoencoders (VAEs)

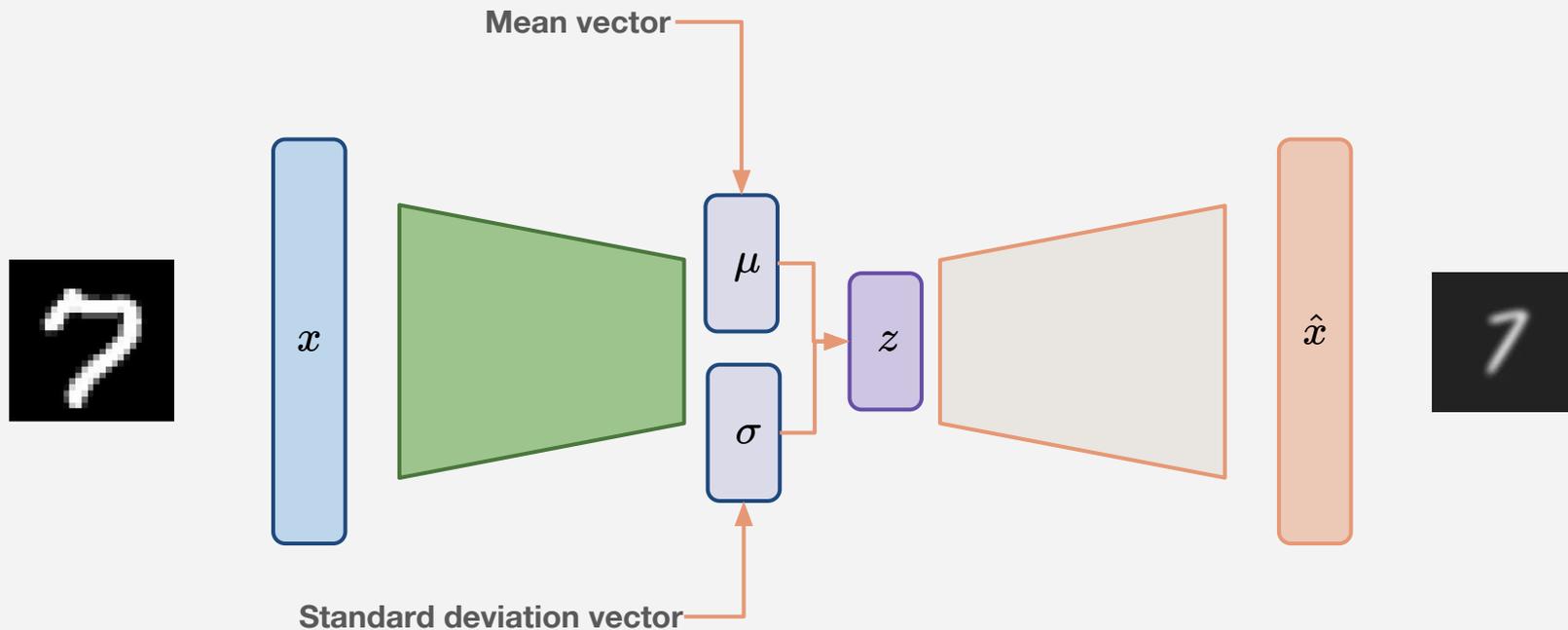
Autoencoder



Variational Autoencoder (VAE) : Key Difference



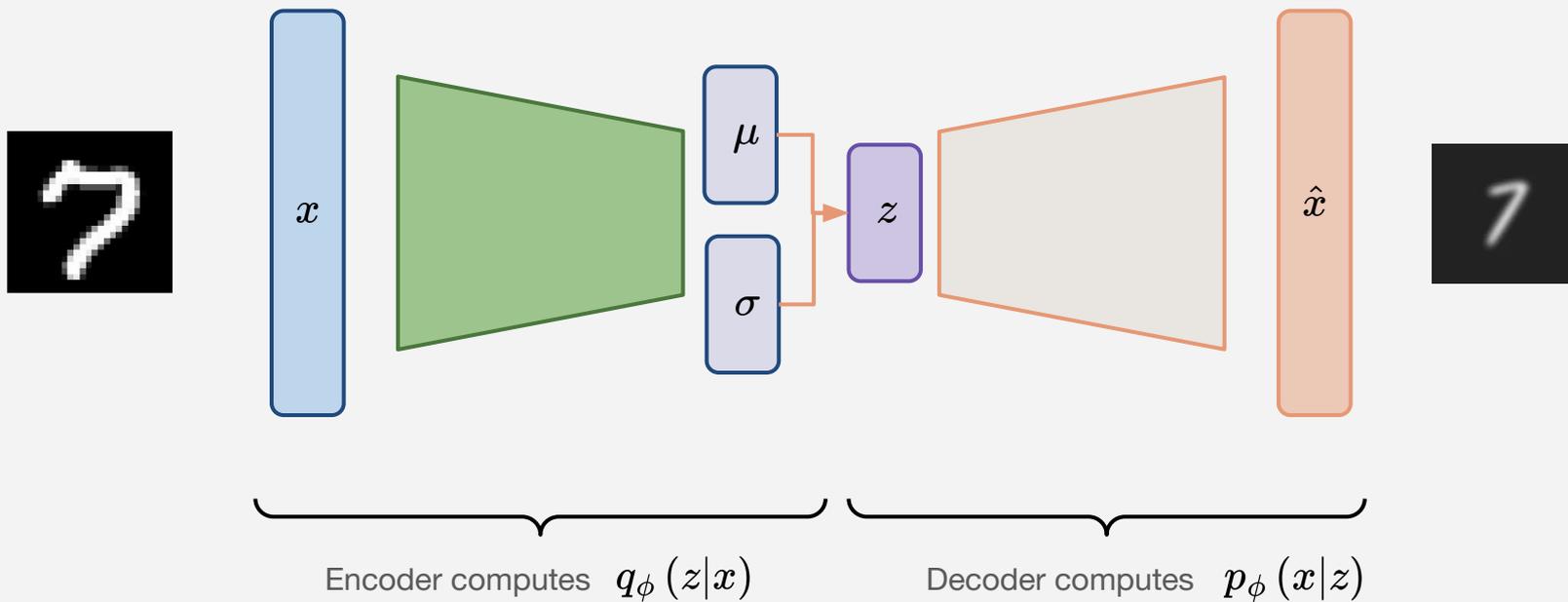
VAE : Key Difference



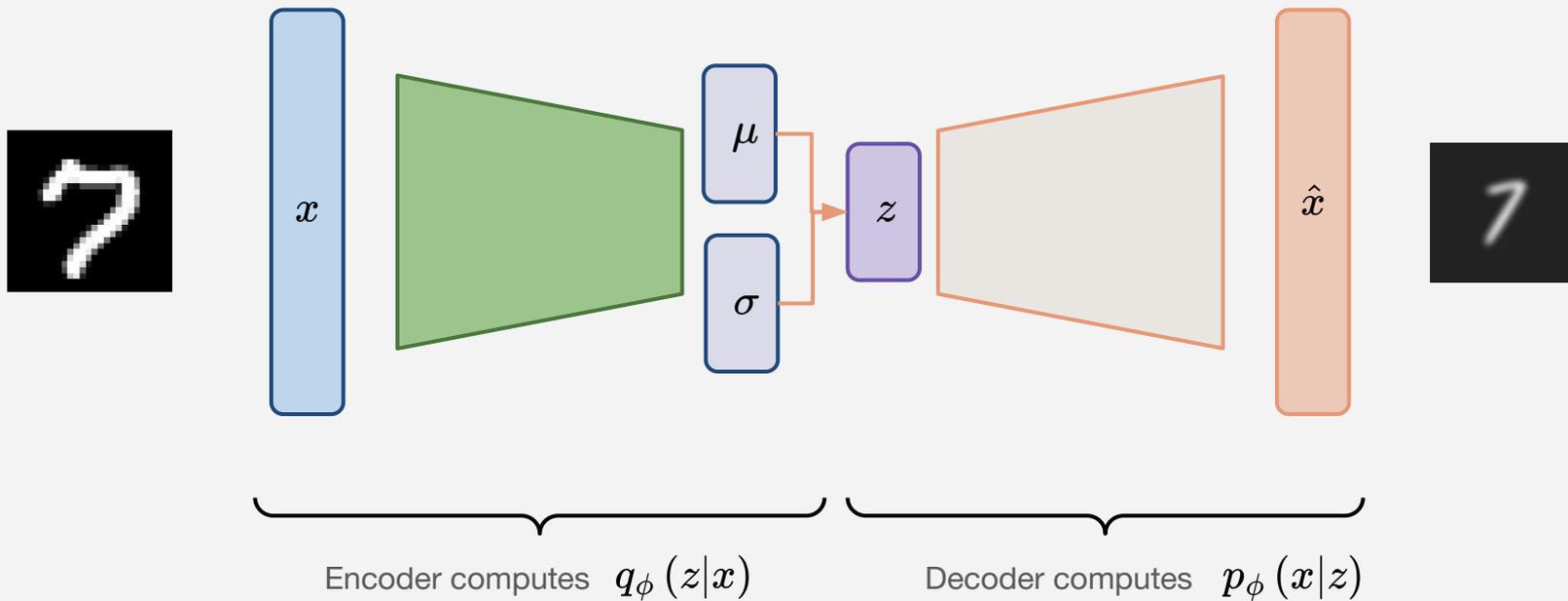
Variational Autoencoders are a probabilistic twist on autoencoders

Sample from the mean and standard deviation to compute latent space

VAE Optimization

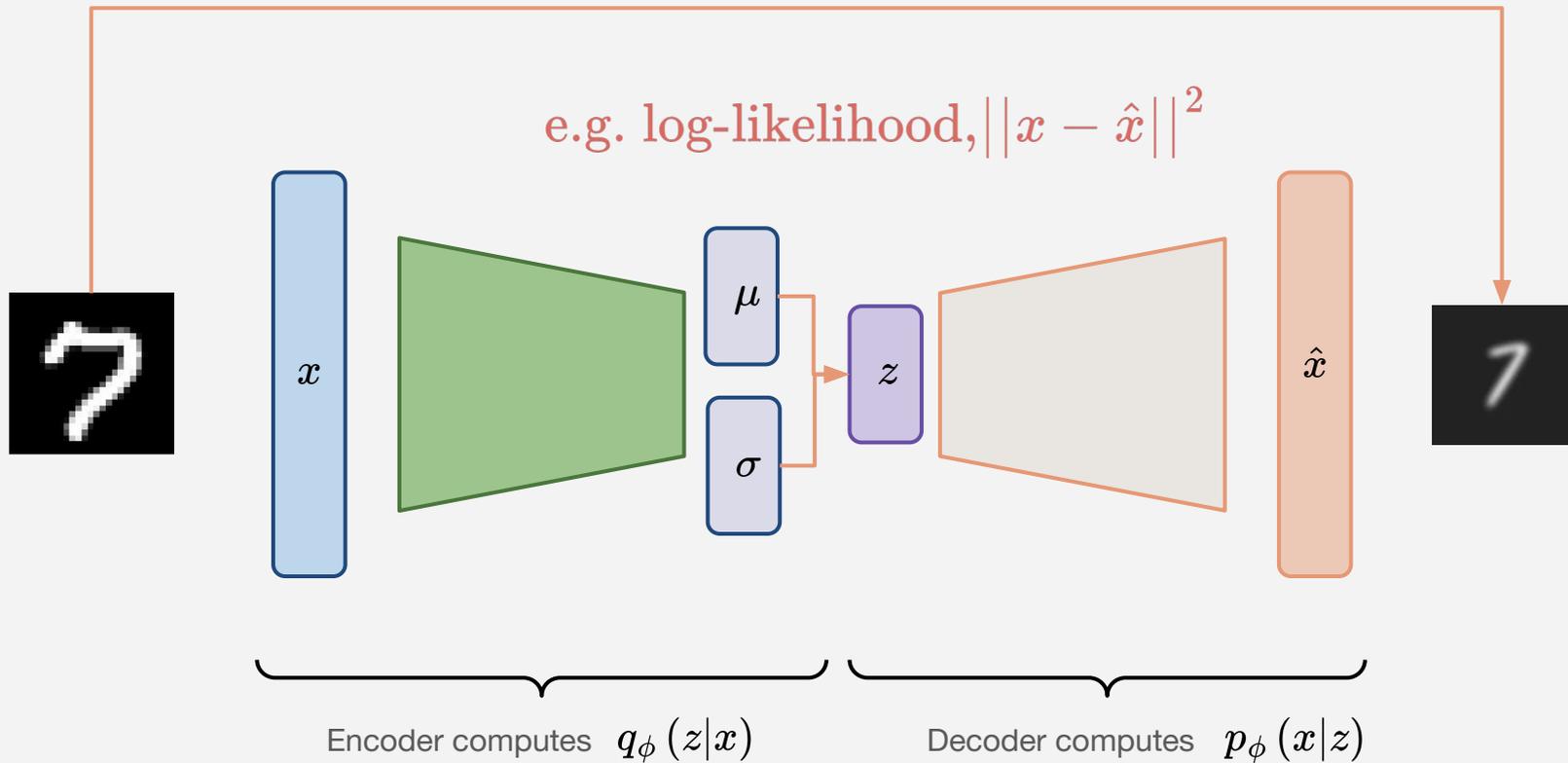


VAE Optimization



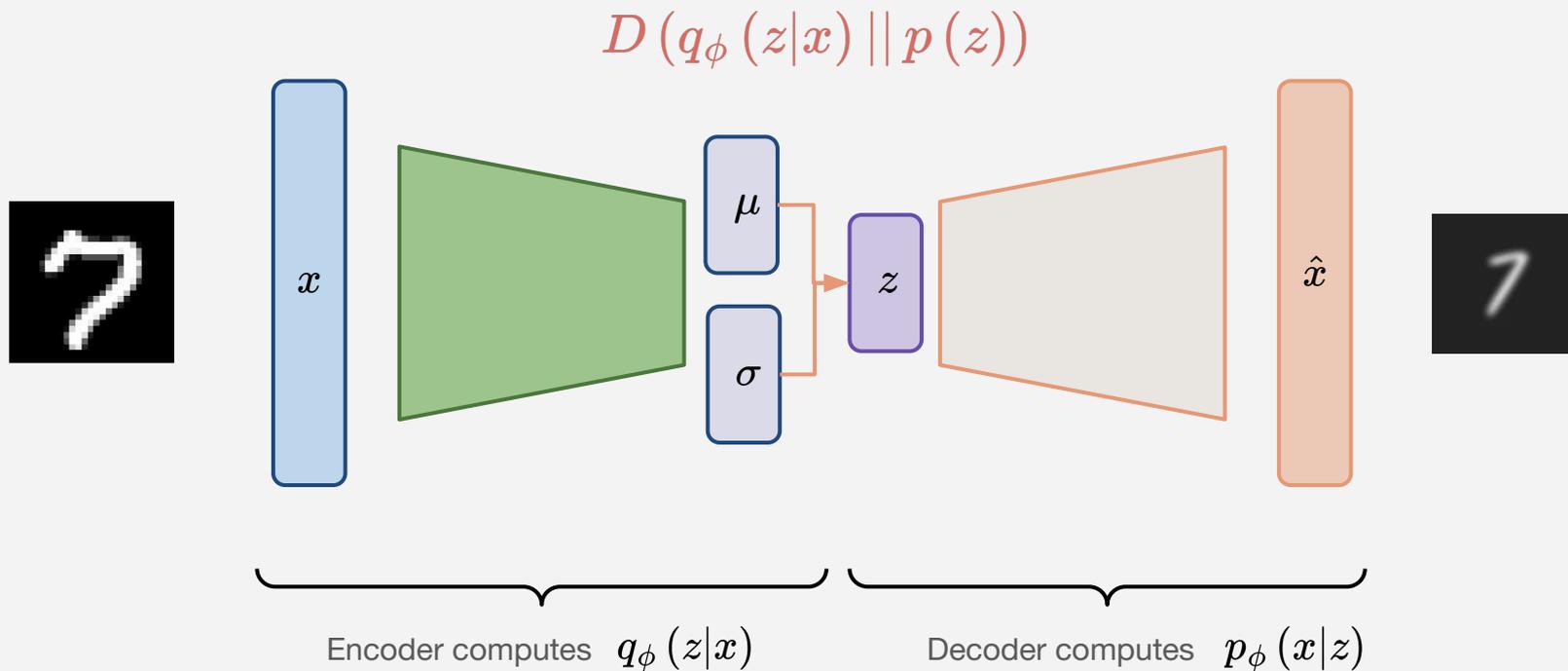
$$\mathcal{L}(\phi, \theta, x) = (\text{reconstruction loss}) + (\text{regularization term})$$

VAE Optimization



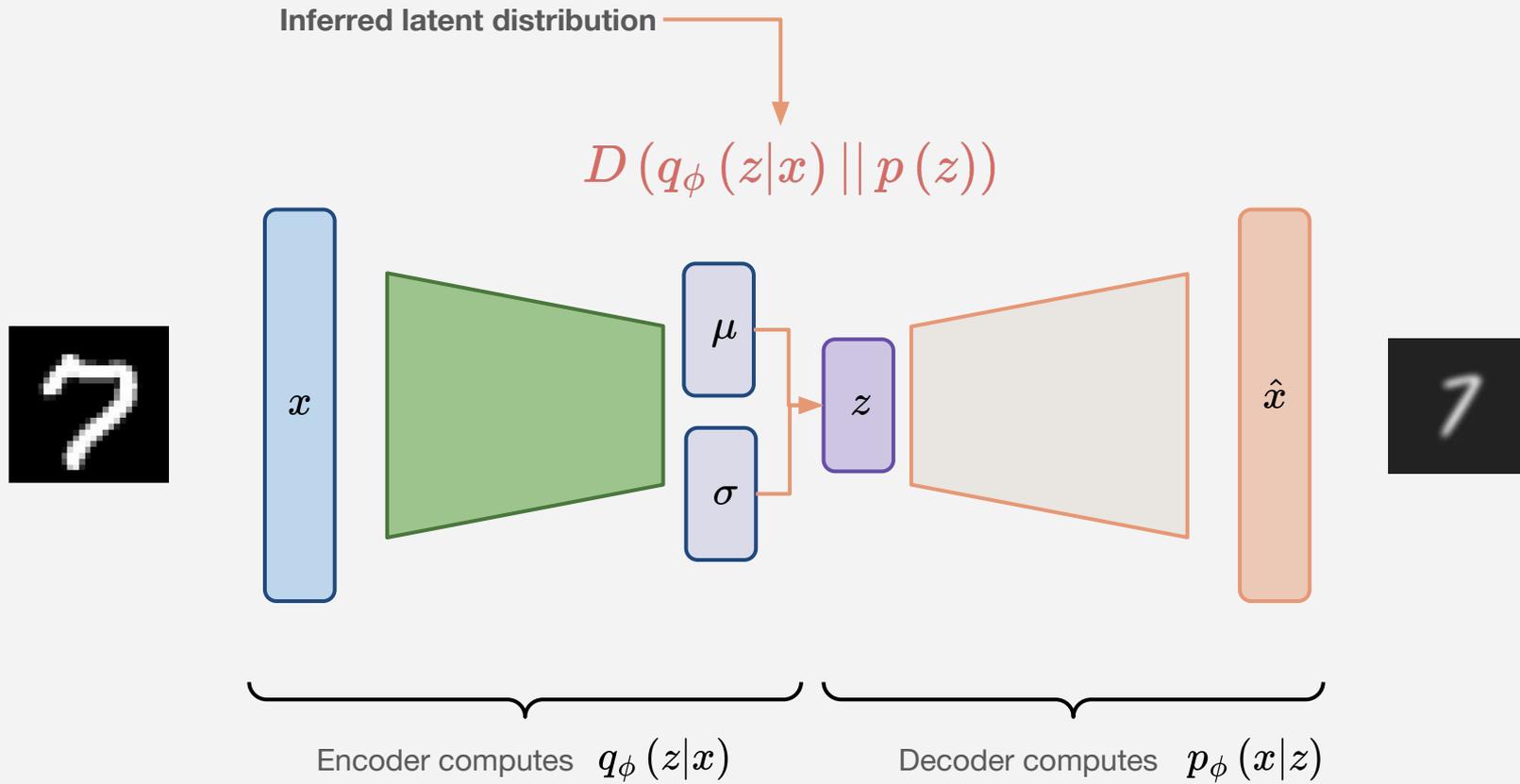
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VAE Optimization



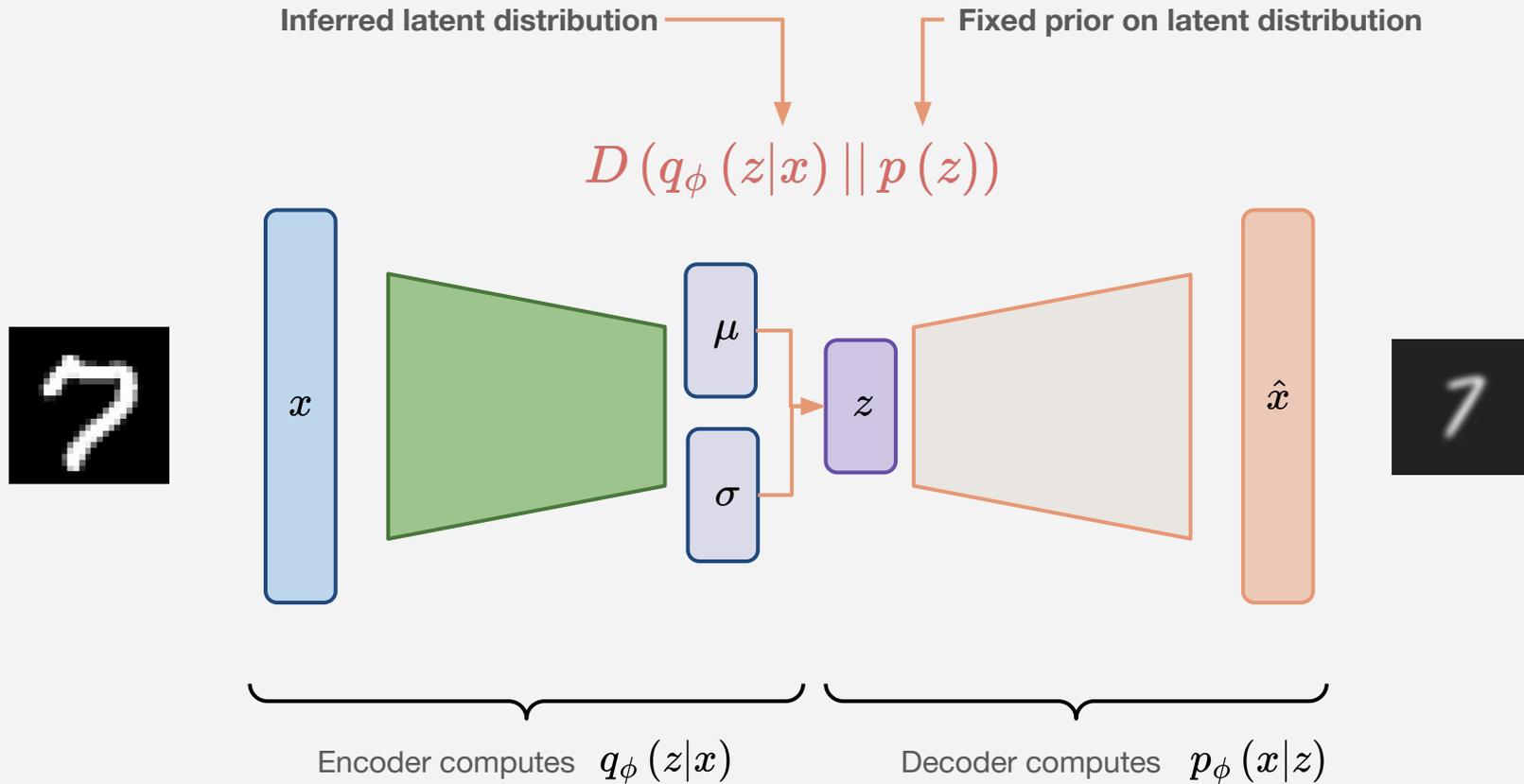
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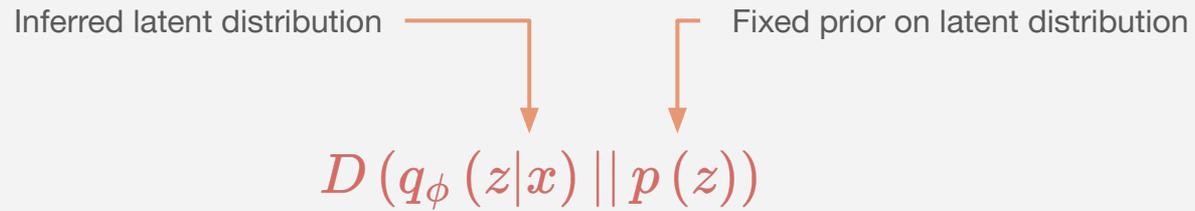
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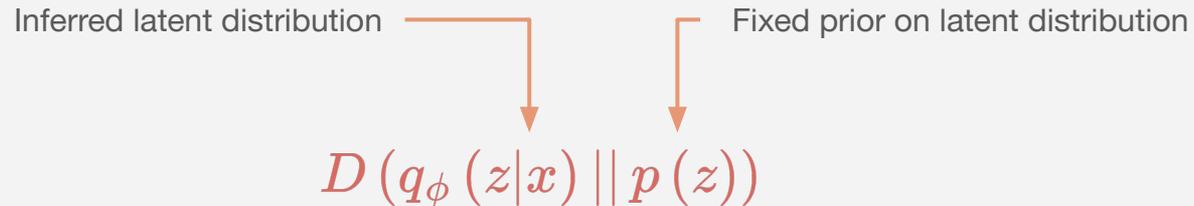


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Priors on Latent Distribution



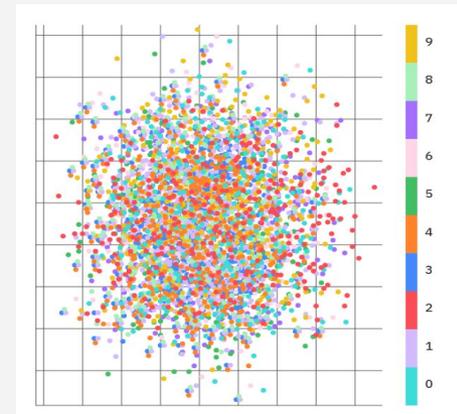
Priors on Latent Distribution



Common Choice of prior: Normal Gaussian

$$p(z) = \mathcal{N}(\mu = 0, \sigma^2 = 1)$$

- Encourages distribution of encodings evenly around the center of the latent space
- Penalize the network when it tries to “cheat” by clustering points in specific regions (memorizing the data)



Priors on Latent Distribution

Inferred latent distribution

Fixed prior on latent distribution

$$D(q_\phi(z|x) || p(z))$$

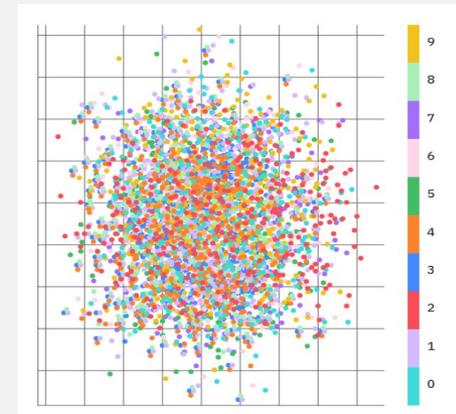
KL-divergence between the two distributions

$$= -\frac{1}{2} \sum_{j=0}^{k-1} (\sigma_j + \mu_j^2 - 1 - \log \sigma_j)$$

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$$p(z) = \mathcal{N}(\mu = 0, \sigma^2 = 1)$$

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Regularization

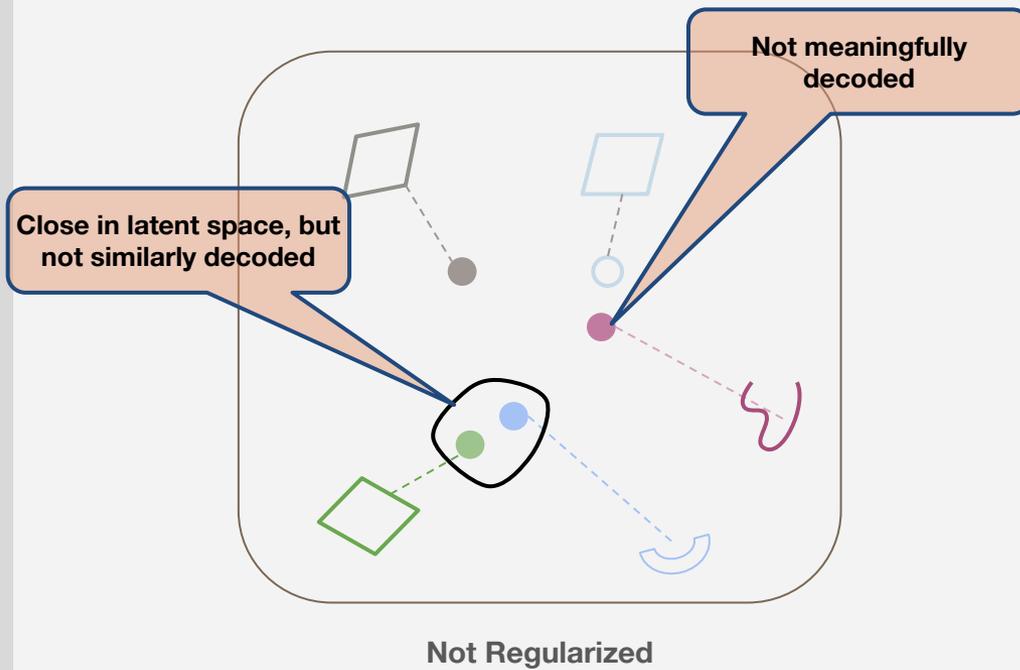
- **Continuity:** points close in the latent space → similar content after decoding

Regularization

- **Continuity:** points close in the latent space → similar content after decoding
- **Completeness:** sampling from the latent space → “meaningful” content after decoding

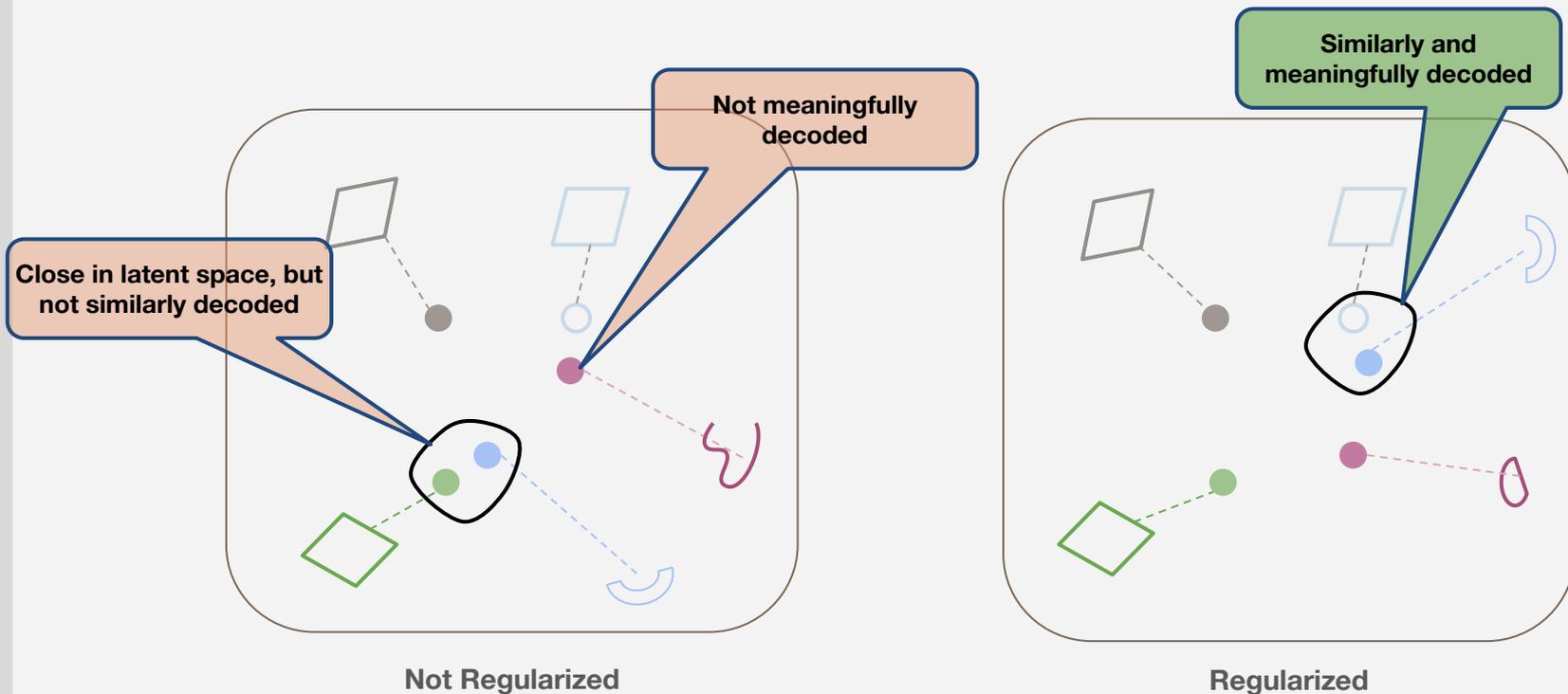
Regularization

- **Continuity:** points close in the latent space → similar content after decoding
- **Completeness:** sampling from the latent space → “meaningful” content after decoding



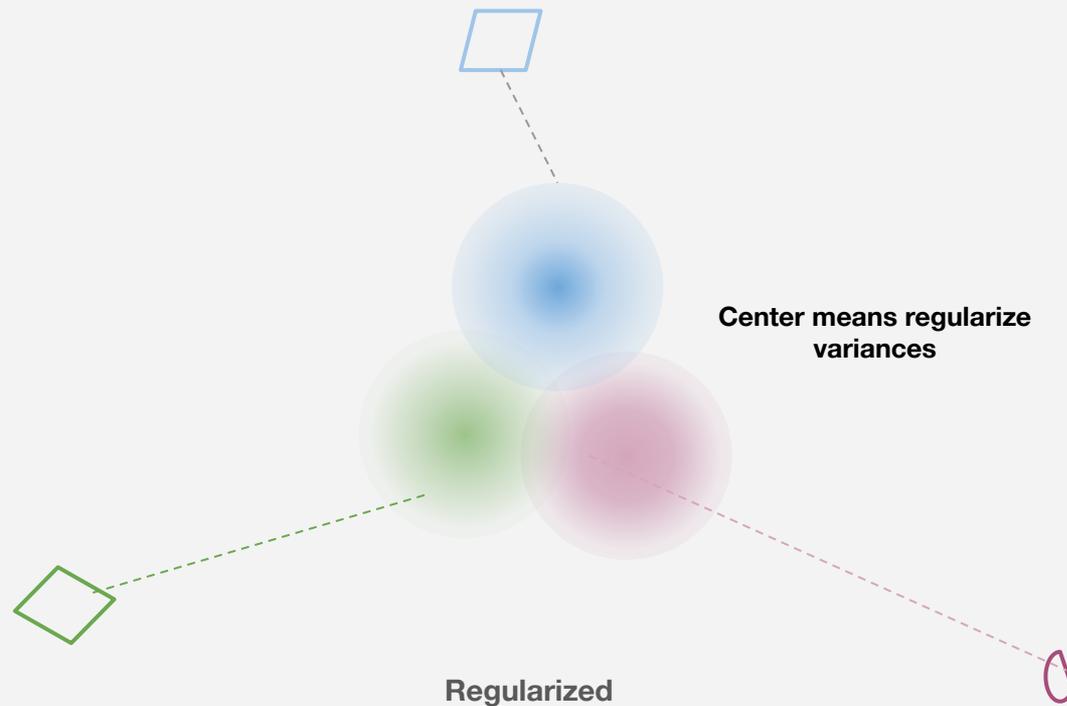
Regularization

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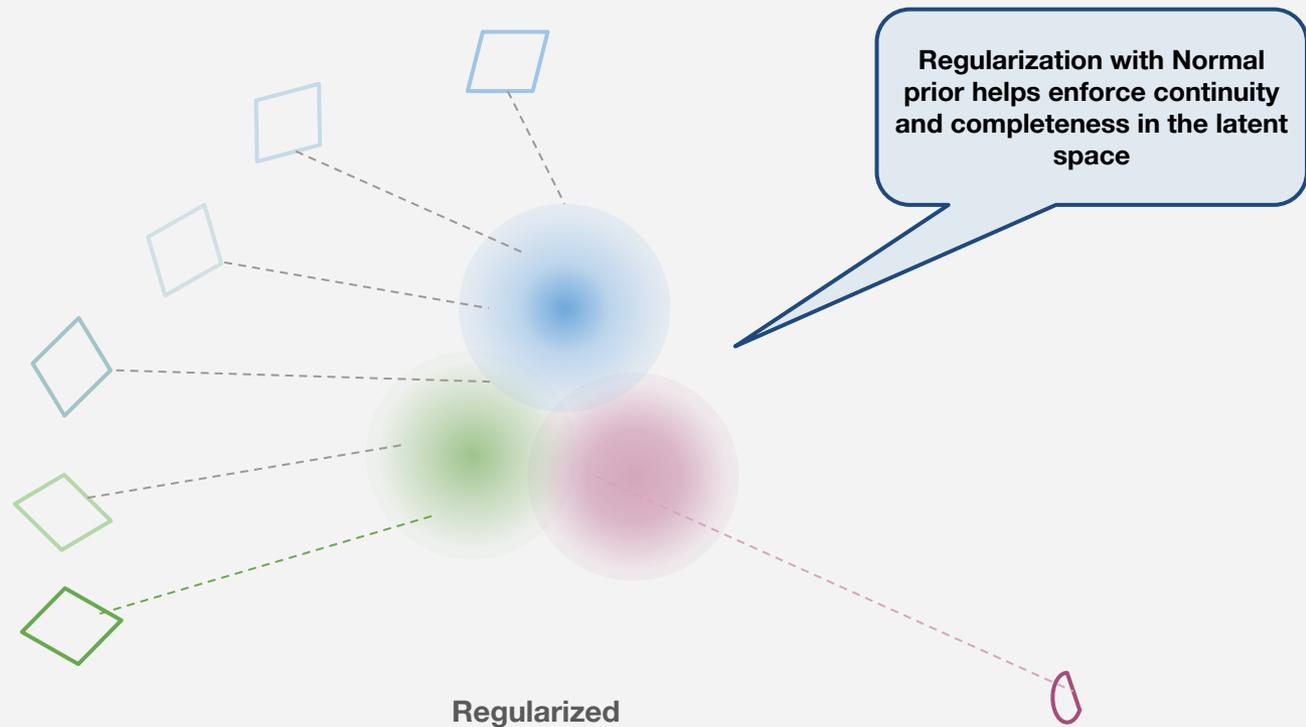
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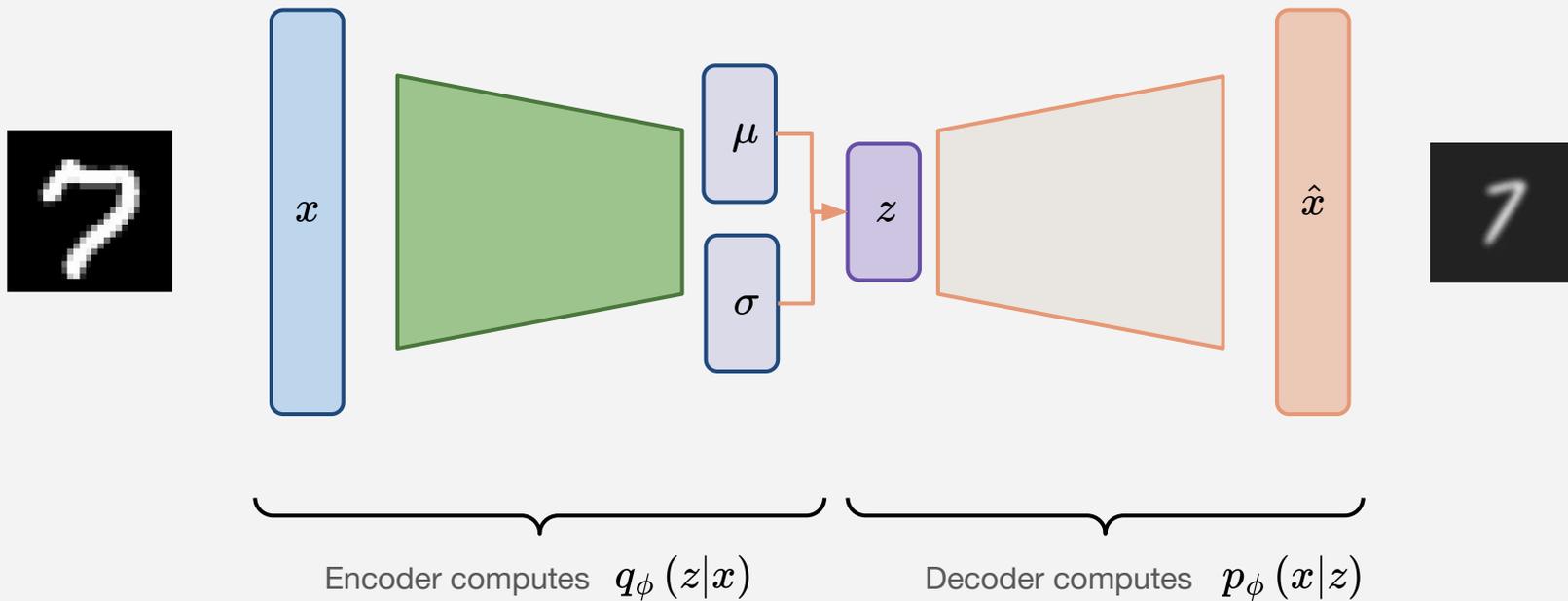


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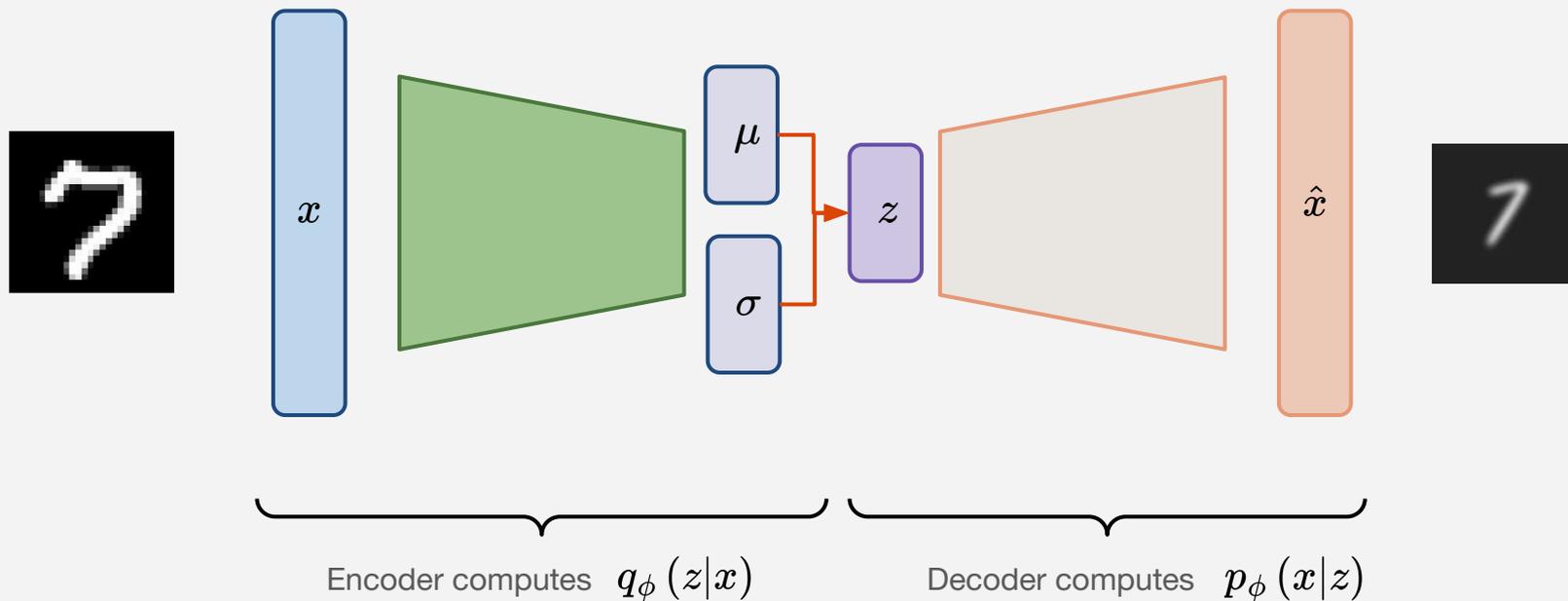
VAE



$$\mathcal{L}(\phi, \theta, x) = (\text{reconstruction loss}) + (\text{regularization term})$$

VAE

Problem: We cannot backpropagate gradients through sampling layers!

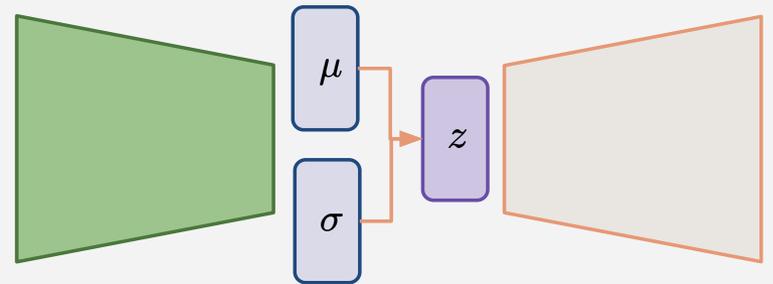


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Reparametrizing the Sampling Layer

Key Idea:

$$z \sim \mathcal{N}(\mu, \sigma^2)$$

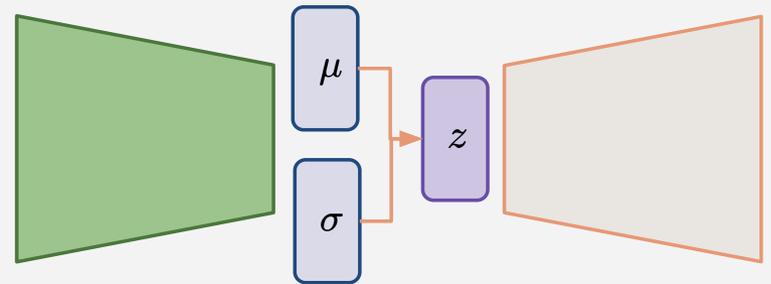


Reparametrizing the Sampling Layer

Key Idea:

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Consider the sampled latent vector z as a sum of:



Reparametrizing the Sampling Layer

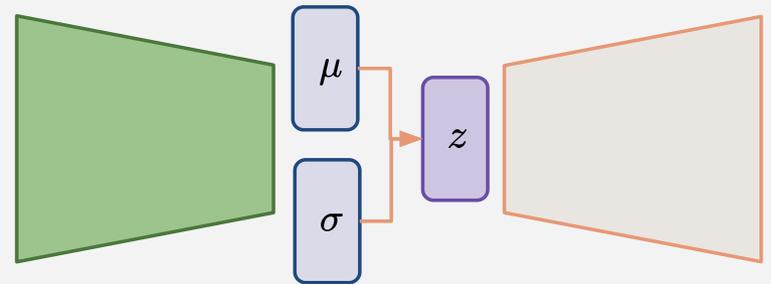
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- A fixed vector μ

$$z = \mu +$$



Reparametrizing the Sampling Layer

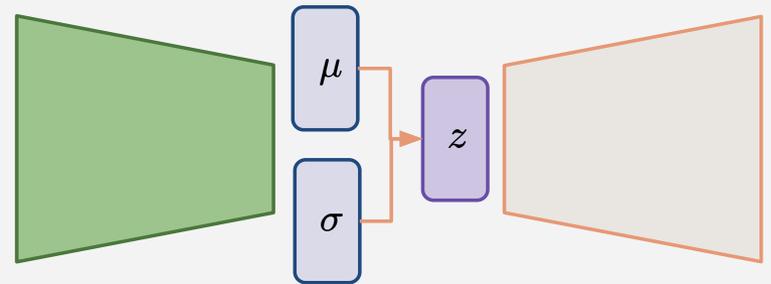
Key Idea:

$$z \sim \mathcal{N}(\mu, \sigma^2)$$

Consider the sampled latent vector z as a sum of:

- A fixed vector μ
- and a fixed vector σ

$$z = \mu + \sigma$$



Reparametrizing the Sampling Layer

Key Idea:

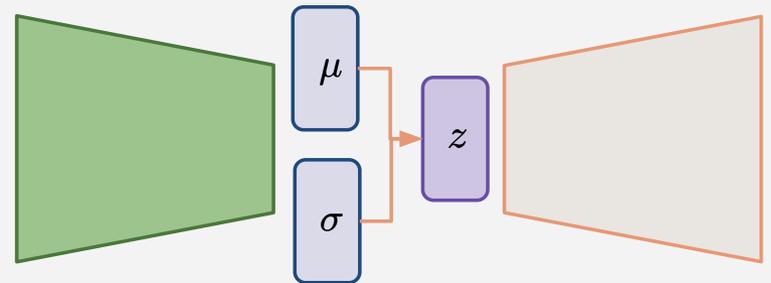
$$z \sim \mathcal{N}(\mu, \sigma^2)$$

Consider the sampled latent vector z as a sum of:

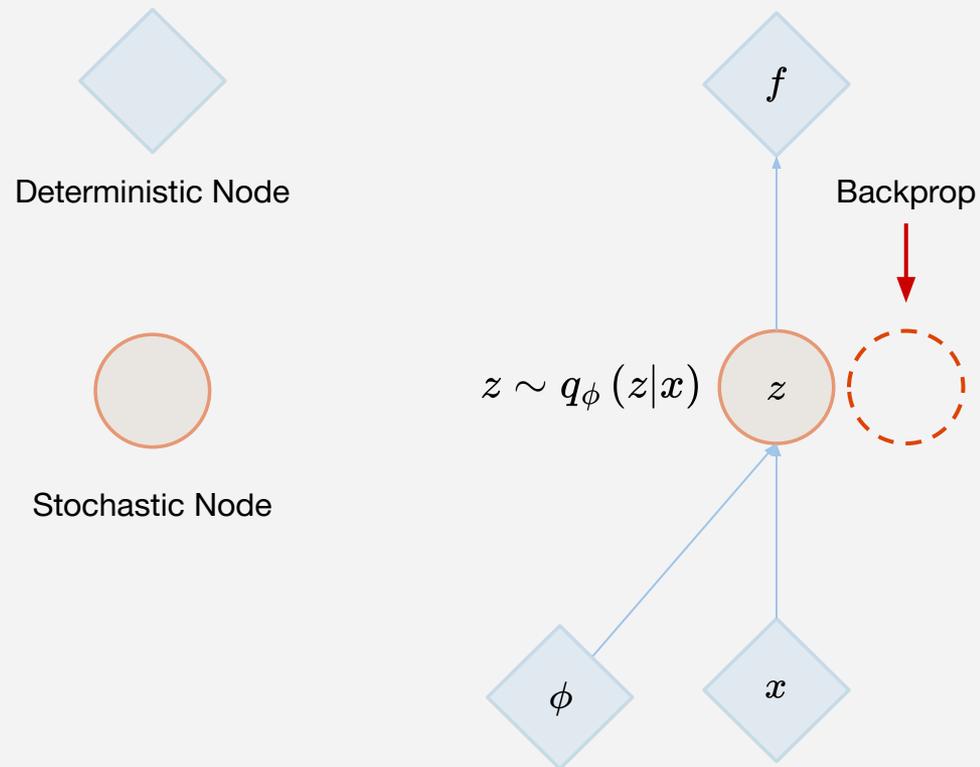
- A fixed vector μ
- and a fixed vector σ scaled by random constant drawn from the prior distribution

$$z = \mu + \sigma \odot \epsilon$$

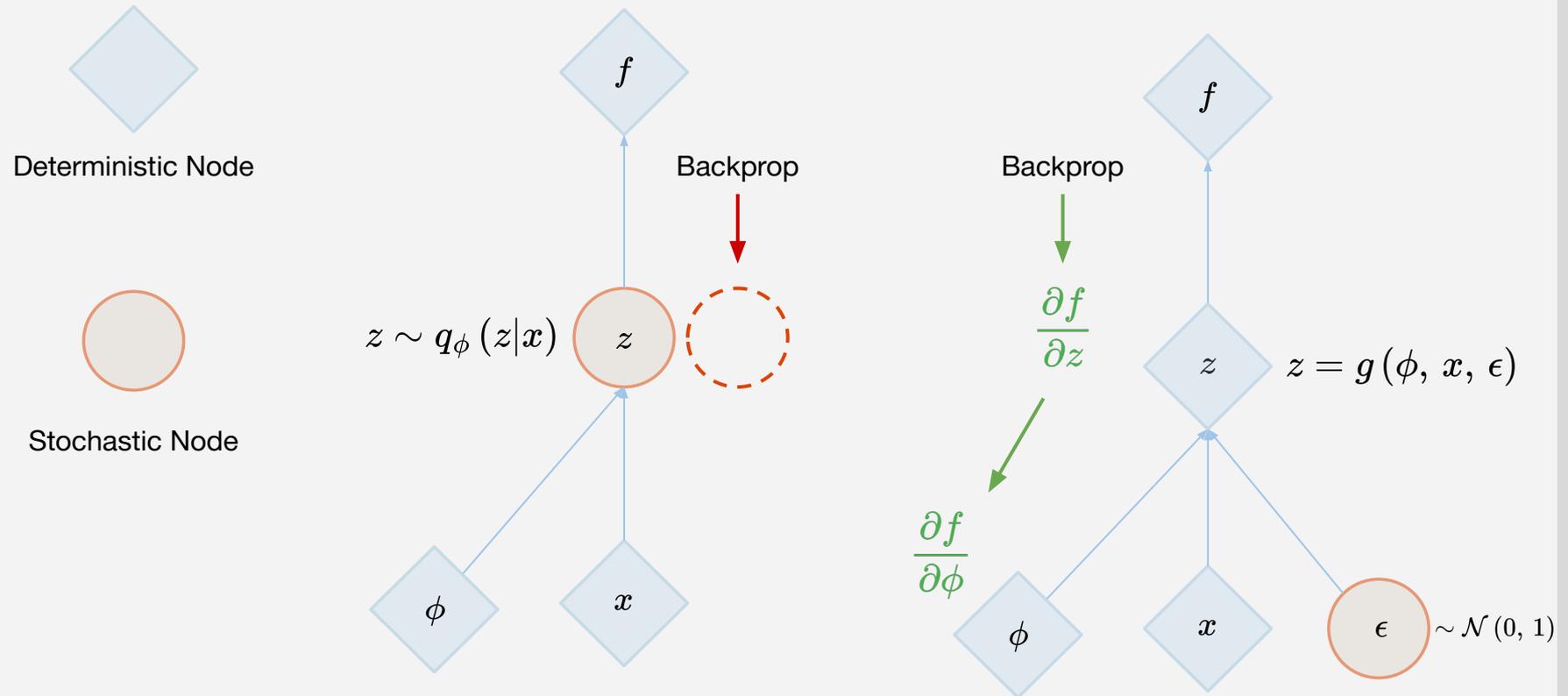
where $\epsilon \sim \mathcal{N}(0, 1)$



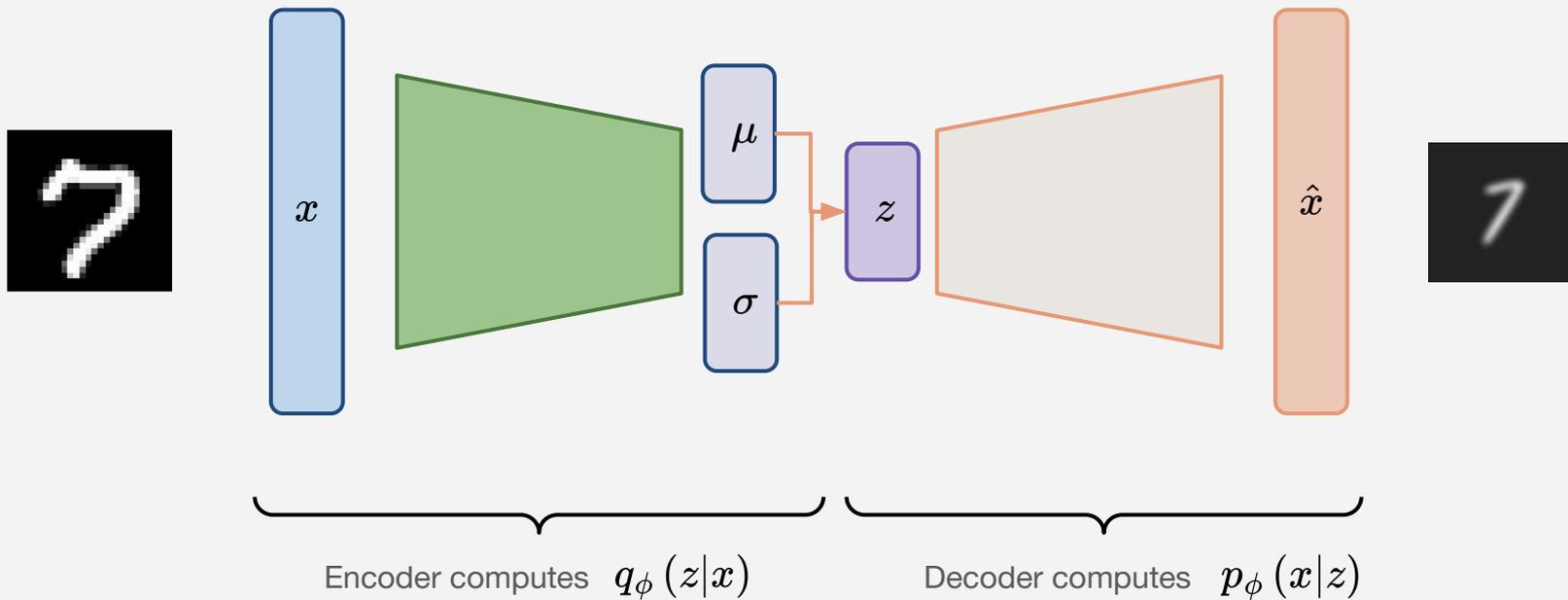
Reparametrizing the Sampling Layer



Reparametrizing the Sampling Layer



VAE



$$\mathcal{L}(\phi, \theta, x) = (\text{reconstruction loss}) + (\text{regularization term})$$

VAE Latent Perturbation

Gradually change **a single latent variable**

Keep all other variables fixed



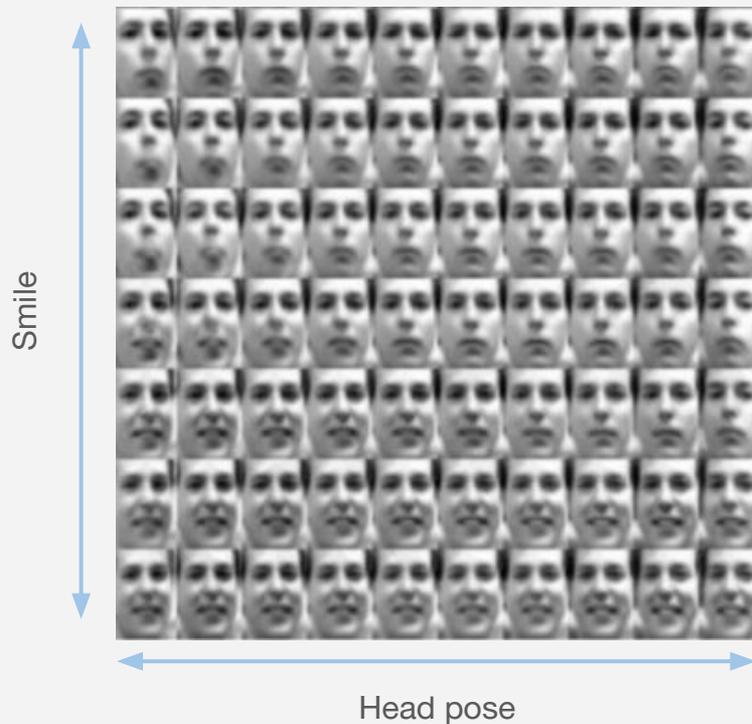
Head pose

Different dimensions of z encodes **different interpretable latent features**

VAE Latent Perturbation

Gradually change **a single latent variable**

Keep all other variables fixed

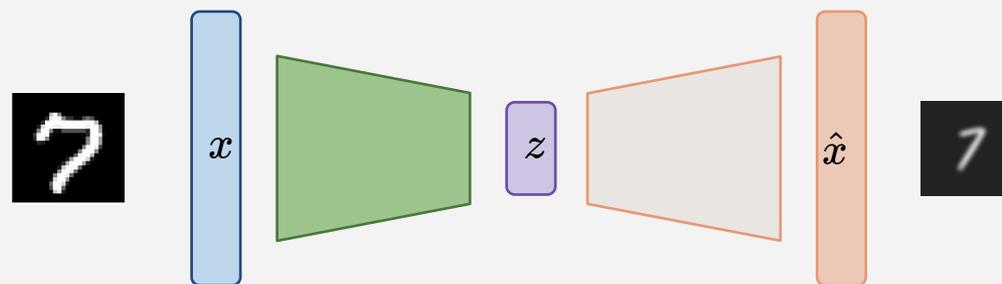


Disentanglement

- We want latent variables that are uncorrelated with each other
- Enforce diagonal prior on the latent variables to encourage independence

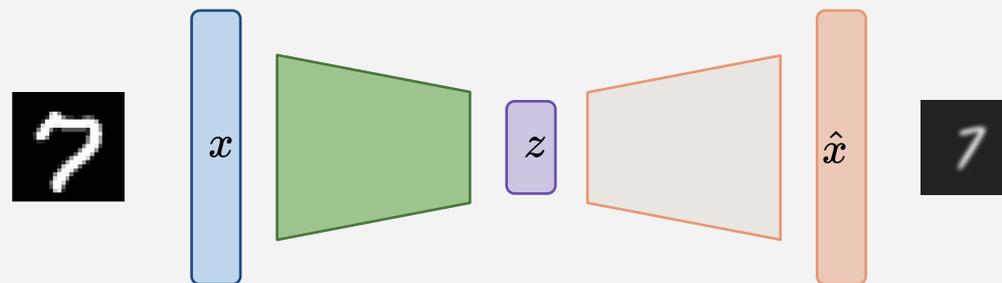
VAE Summary

1. Compress representation of world to something we can use to learn



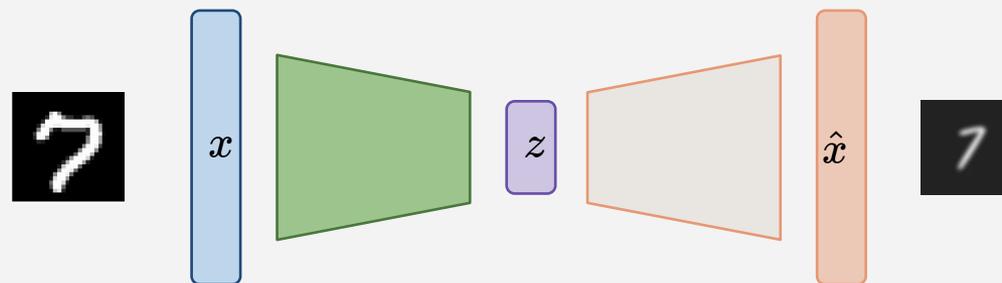
VAE Summary

1. Compress representation of world to something we can use to learn
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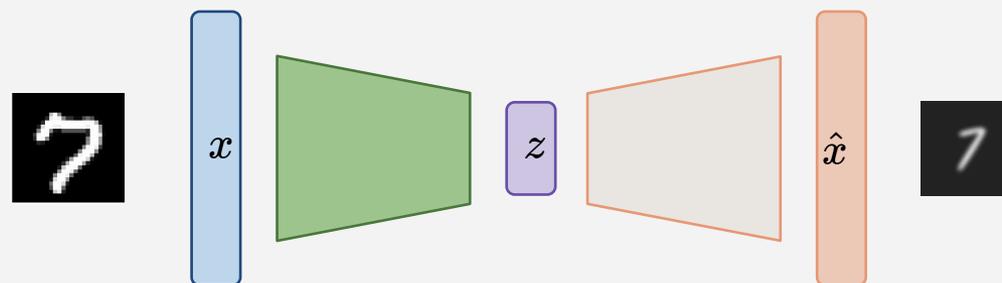
VAE Summary

1. Compress representation of world to something we can use to learn
2. Reconstruction allows for unsupervised learning (no labels)
3. Reparameterization trick to train with gradients



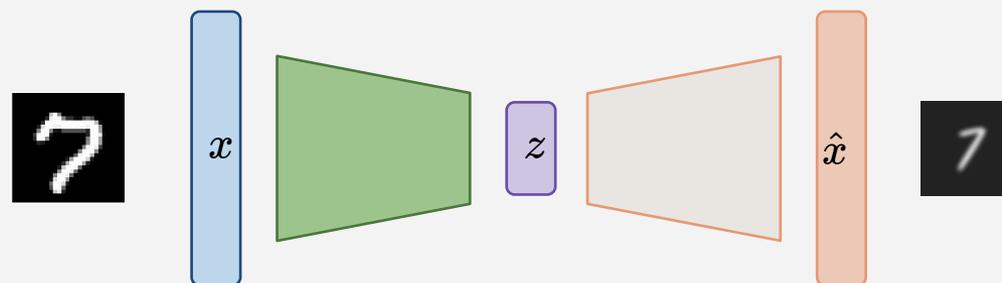
VAE Summary

1. Compress representation of world to something we can use to learn
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VAE Summary

1. Compress representation of world to something we can use to learn
2. Reconstruction allows for unsupervised learning (no labels)
3. Reparameterization trick to train with gradients
4. Interpret hidden latent variables using perturbation
5. Generation new examples



Generative Adversarial Networks (GANs)

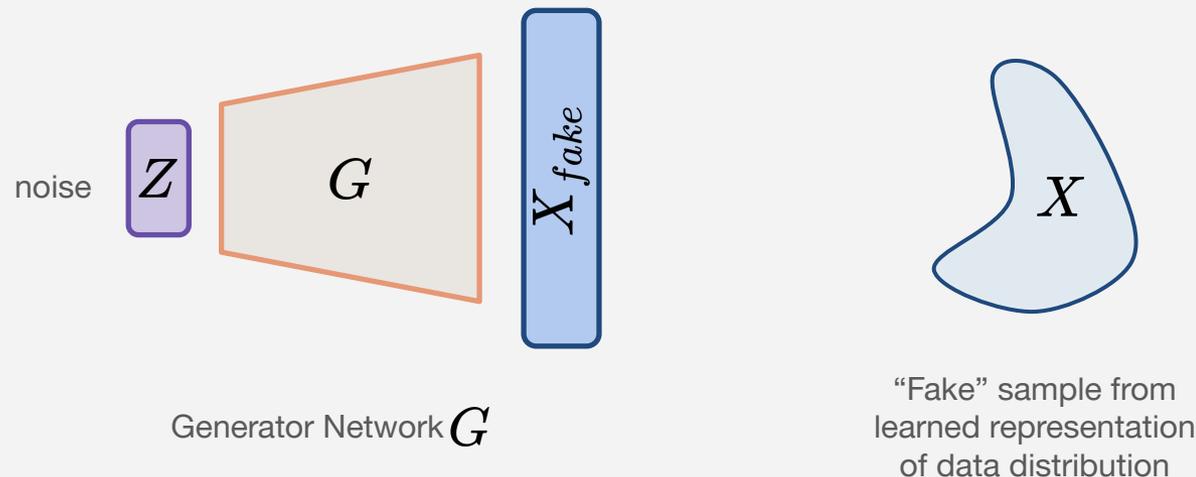
Generative Adversarial Networks (GANs)

Idea: Don't explicitly model density. Instead, just sample to generate new instances.

Problem: Want to sample from a complex distribution? Can't do this directly.

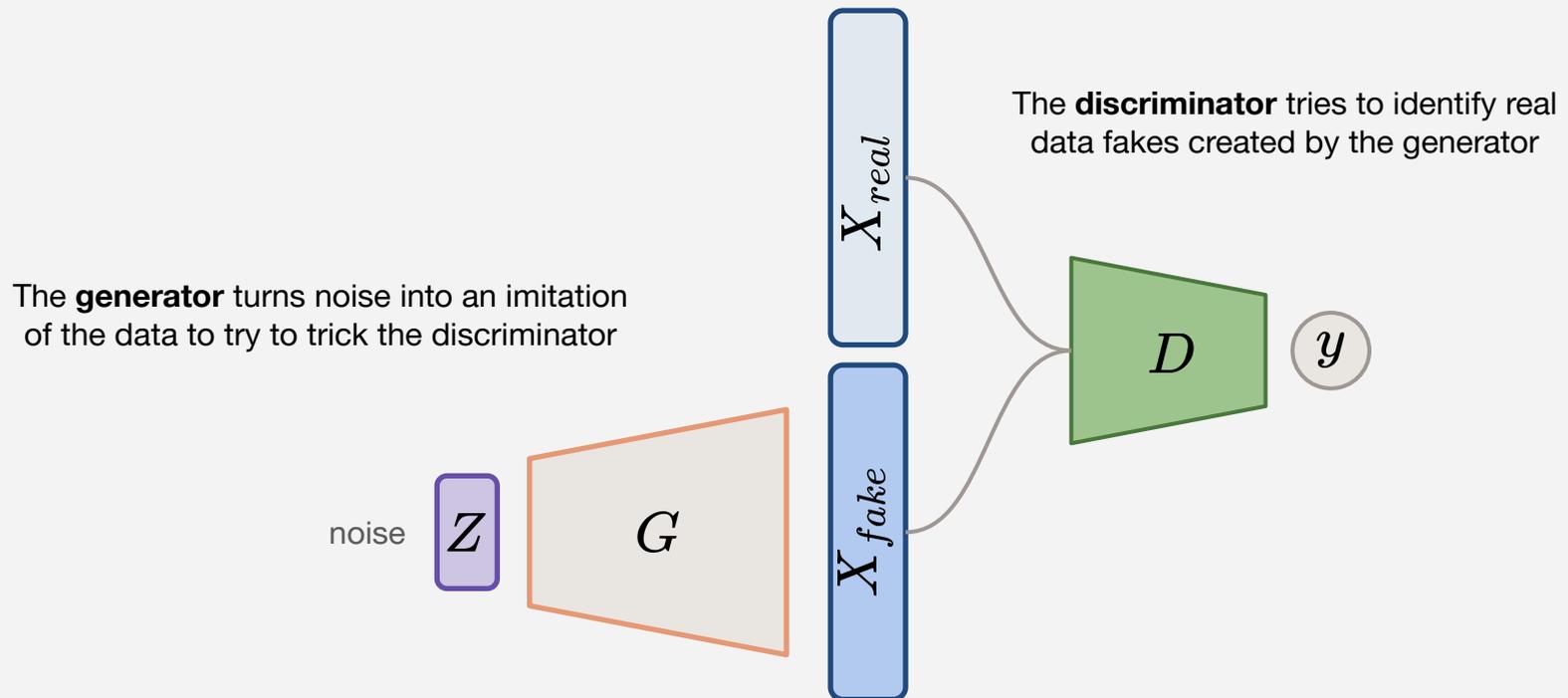
Strategy:

- Sample from something simple (noise?)
- Learn a transformation to the data distribution.



Generative Adversarial Networks (GANs)

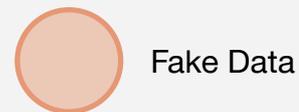
Generative Adversarial Networks (GANs) are a way to make a generative model by having two neural networks compete with each other.



GAN Intuition

Generator starts from noise to try to create an imitation of the data

Generator

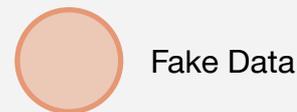


GAN Intuition

Discriminator looks at both real data and fake data created by the generator

Discriminator

Generator



GAN Intuition

Discriminator looks at both real data and fake data created by the generator

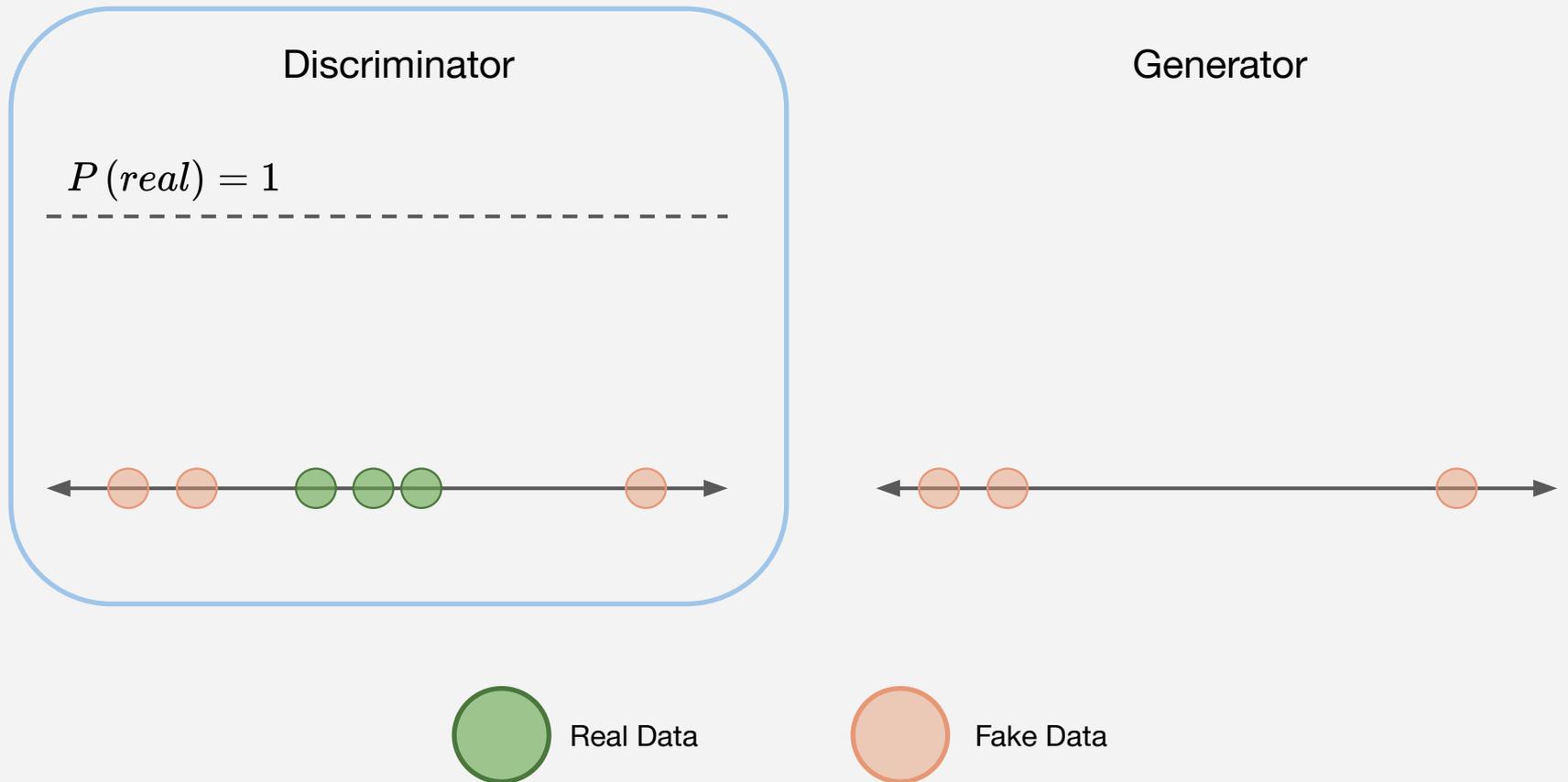
Discriminator

Generator



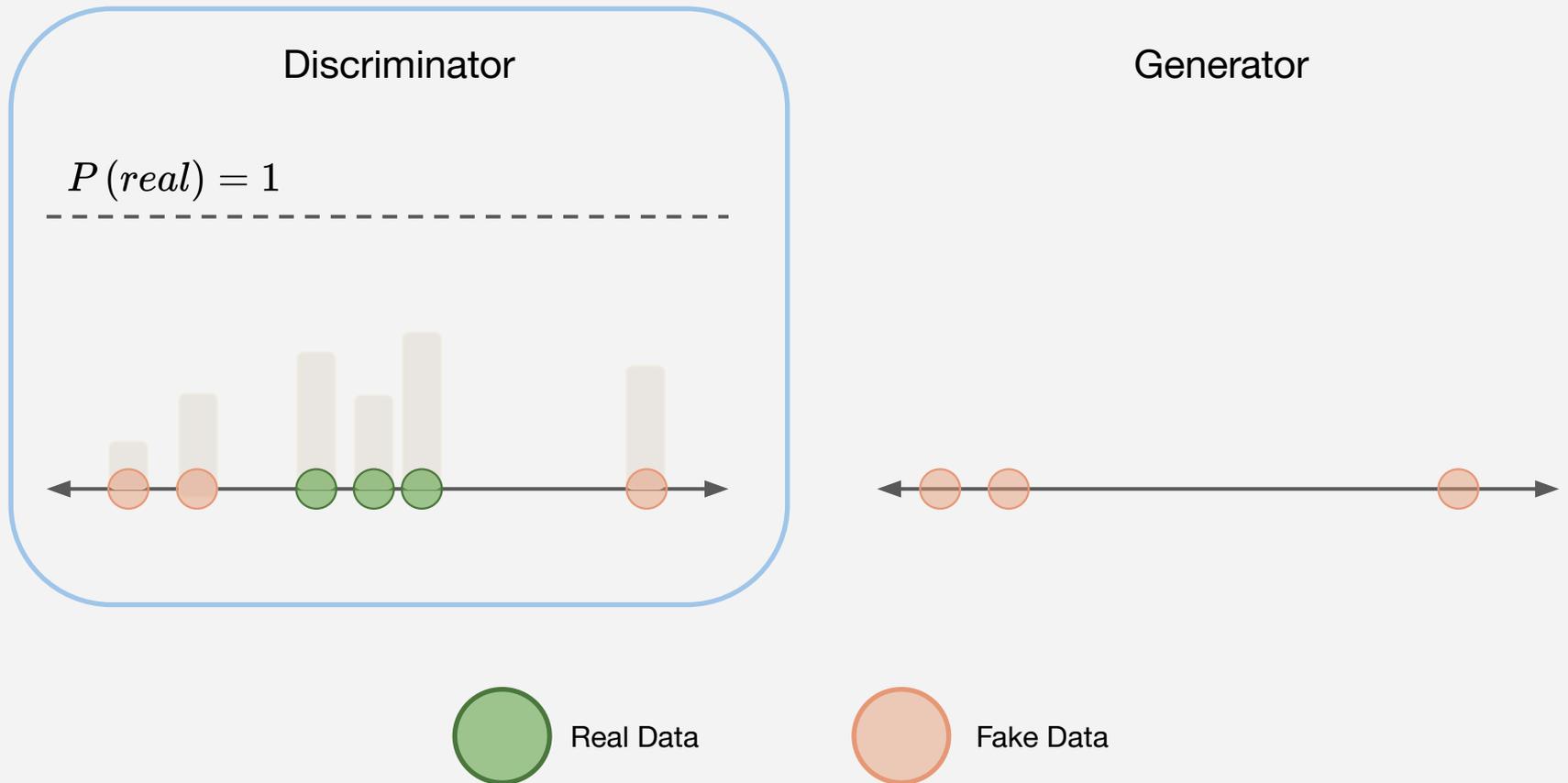
GAN Intuition

Discriminator tries to predict what's real and what's fake



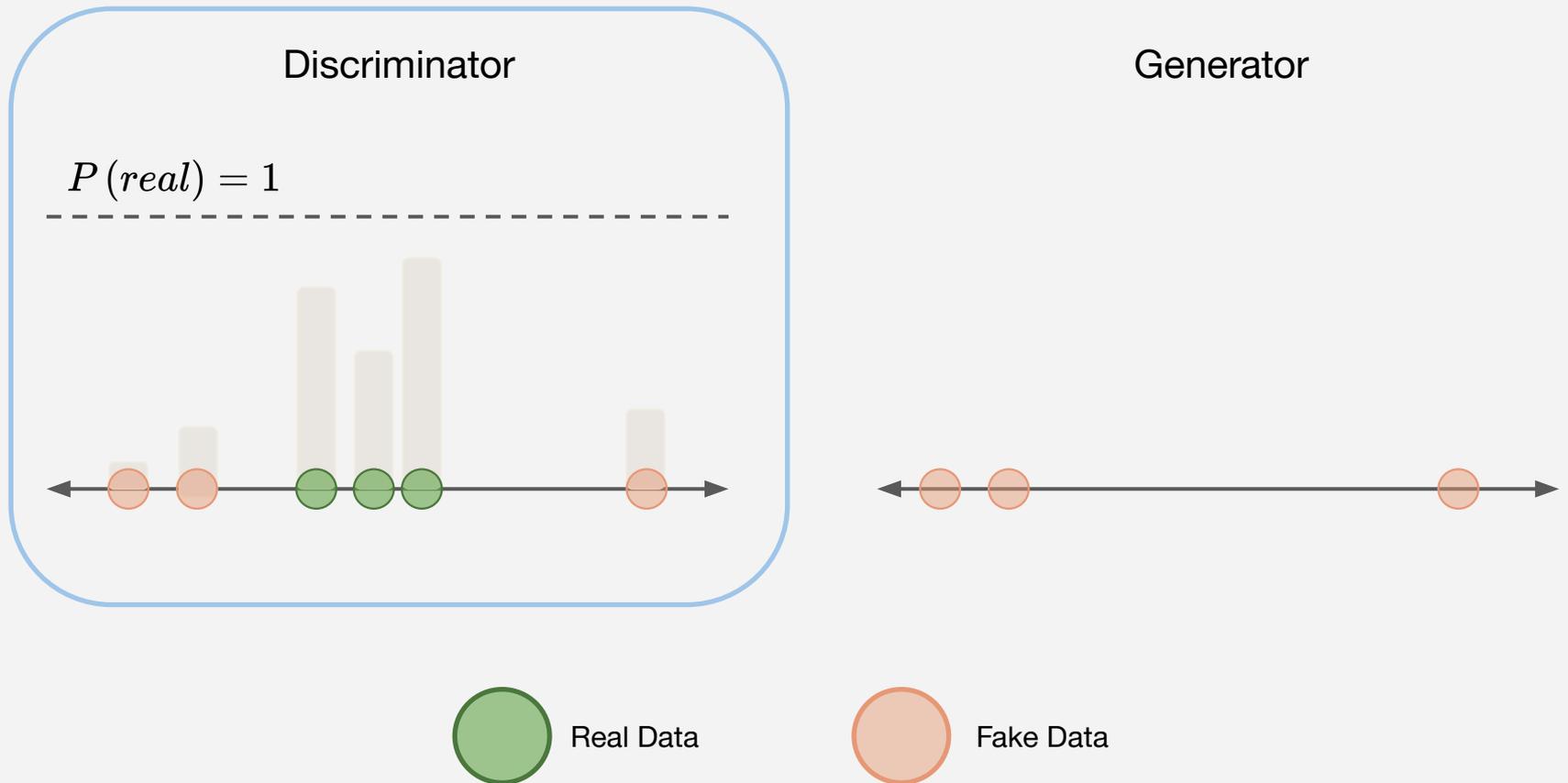
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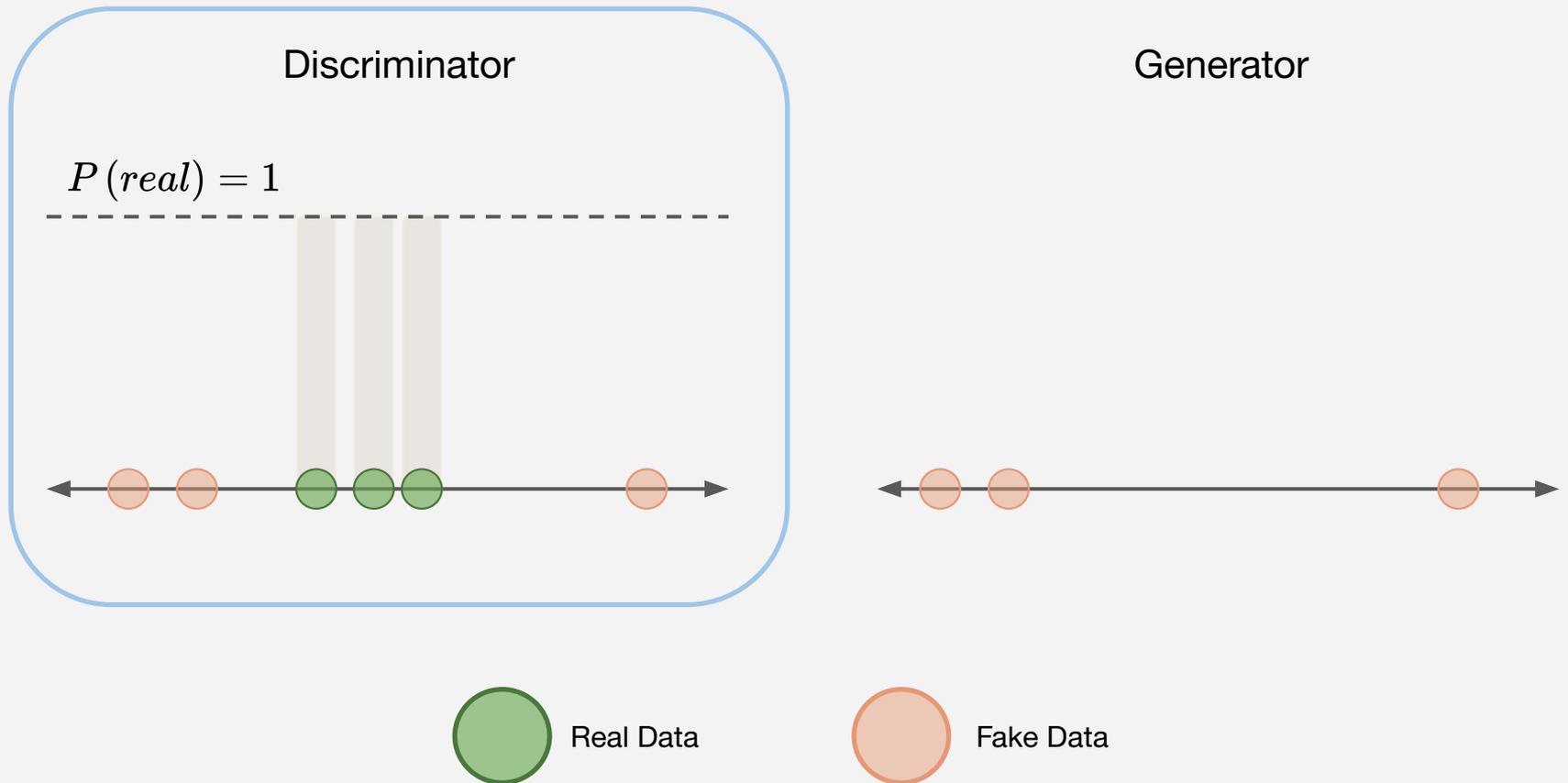
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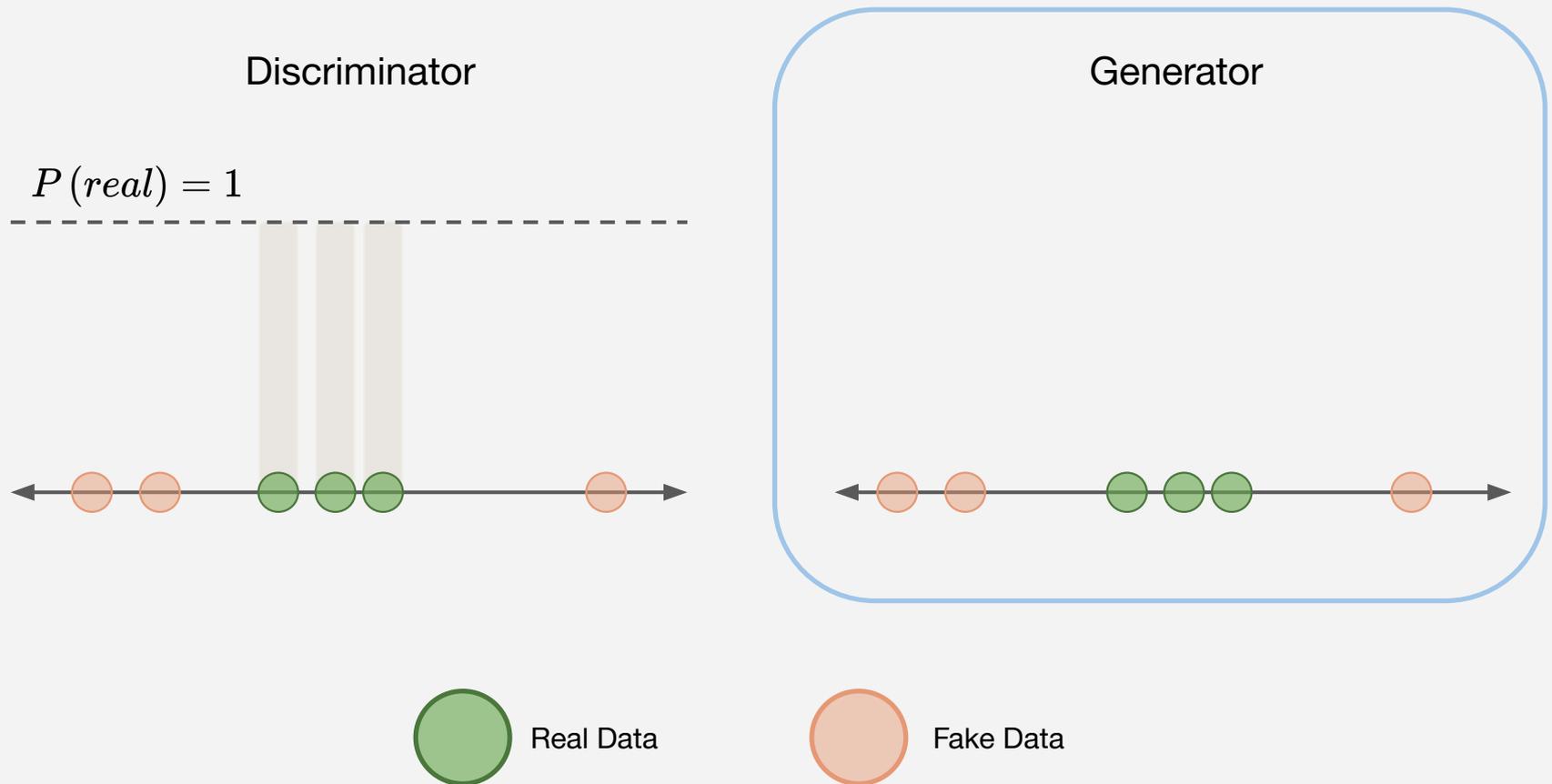
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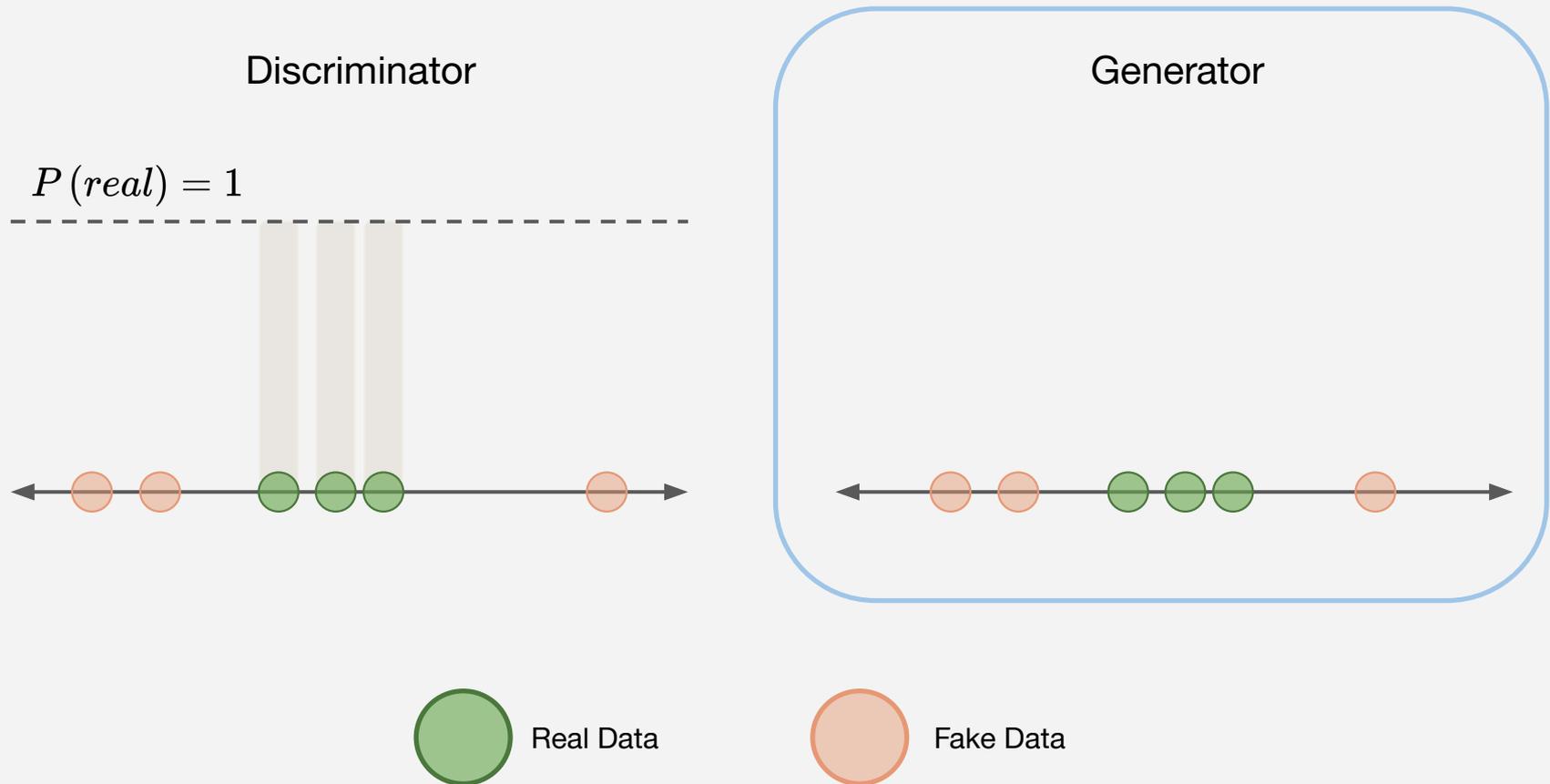
GAN Intuition

Generator tries to improve its imitation of the data



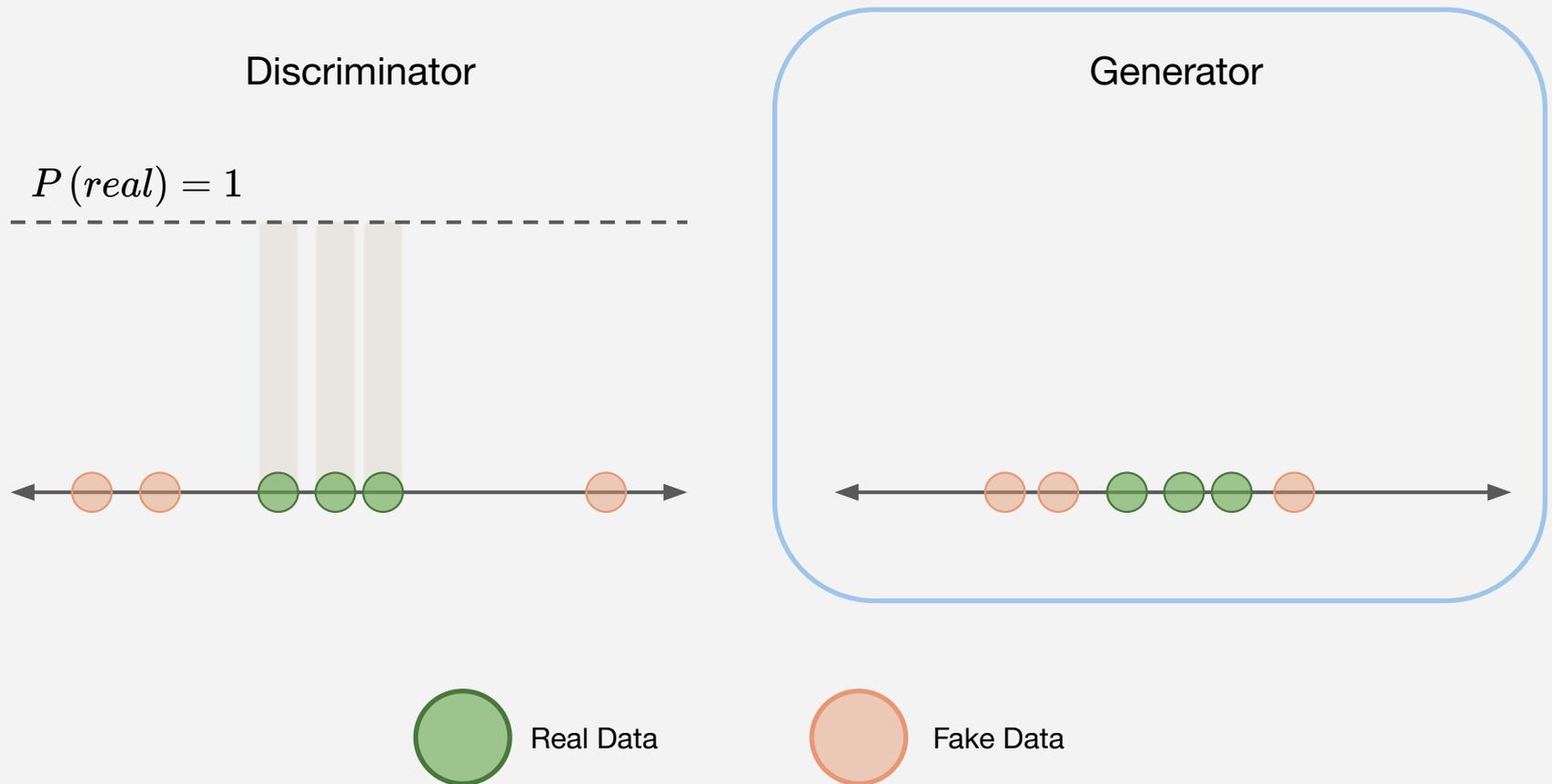
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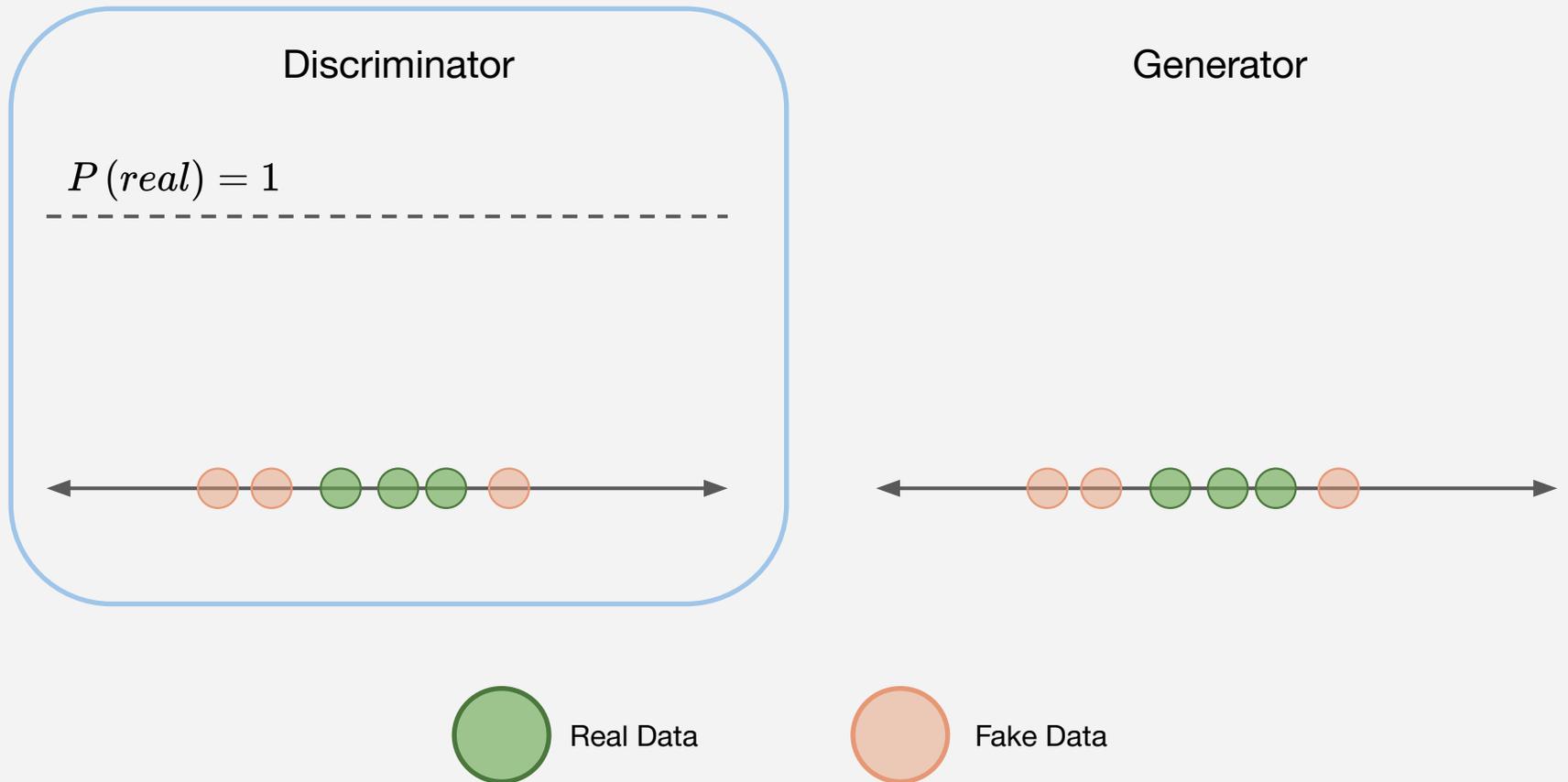
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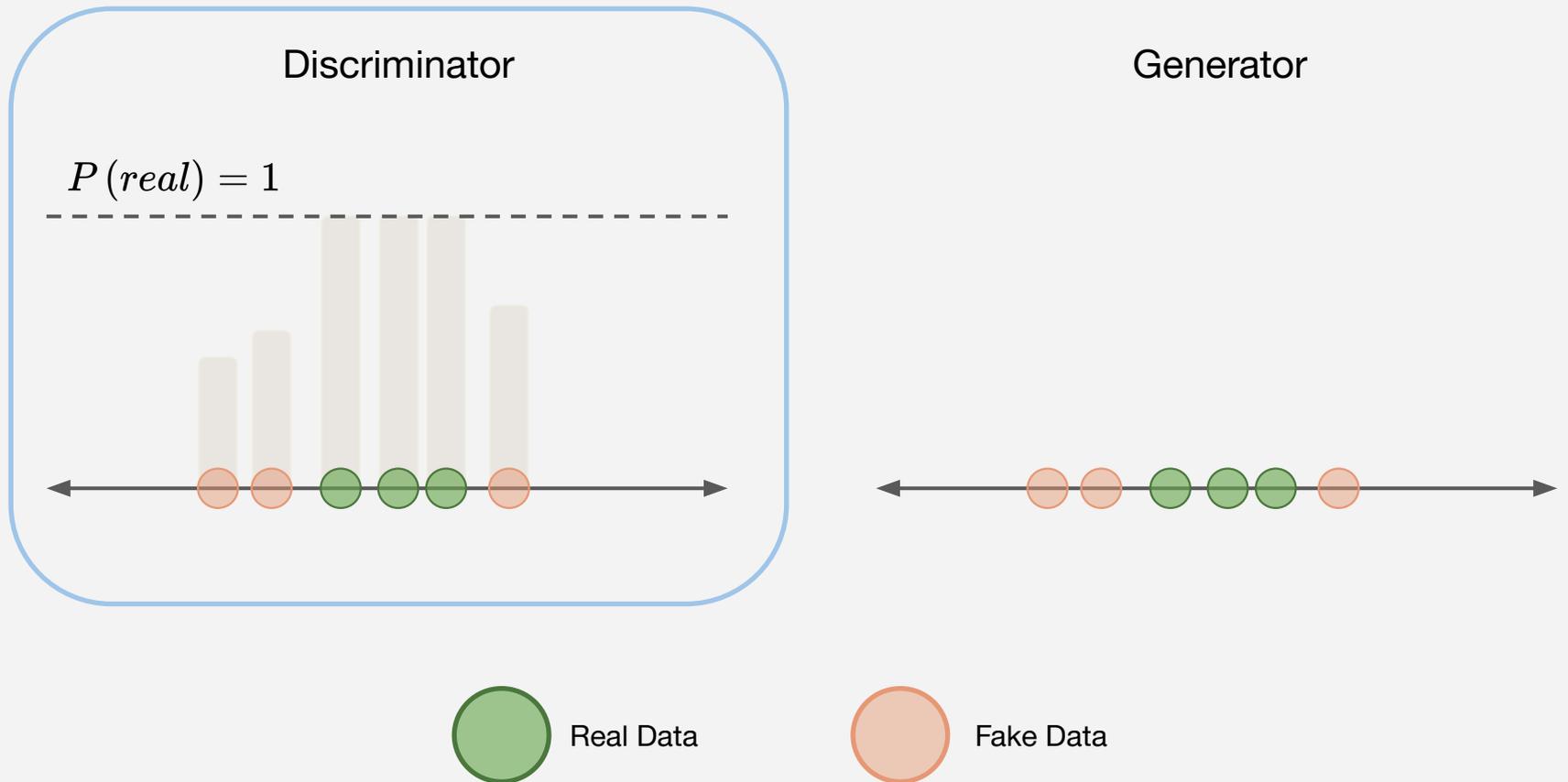
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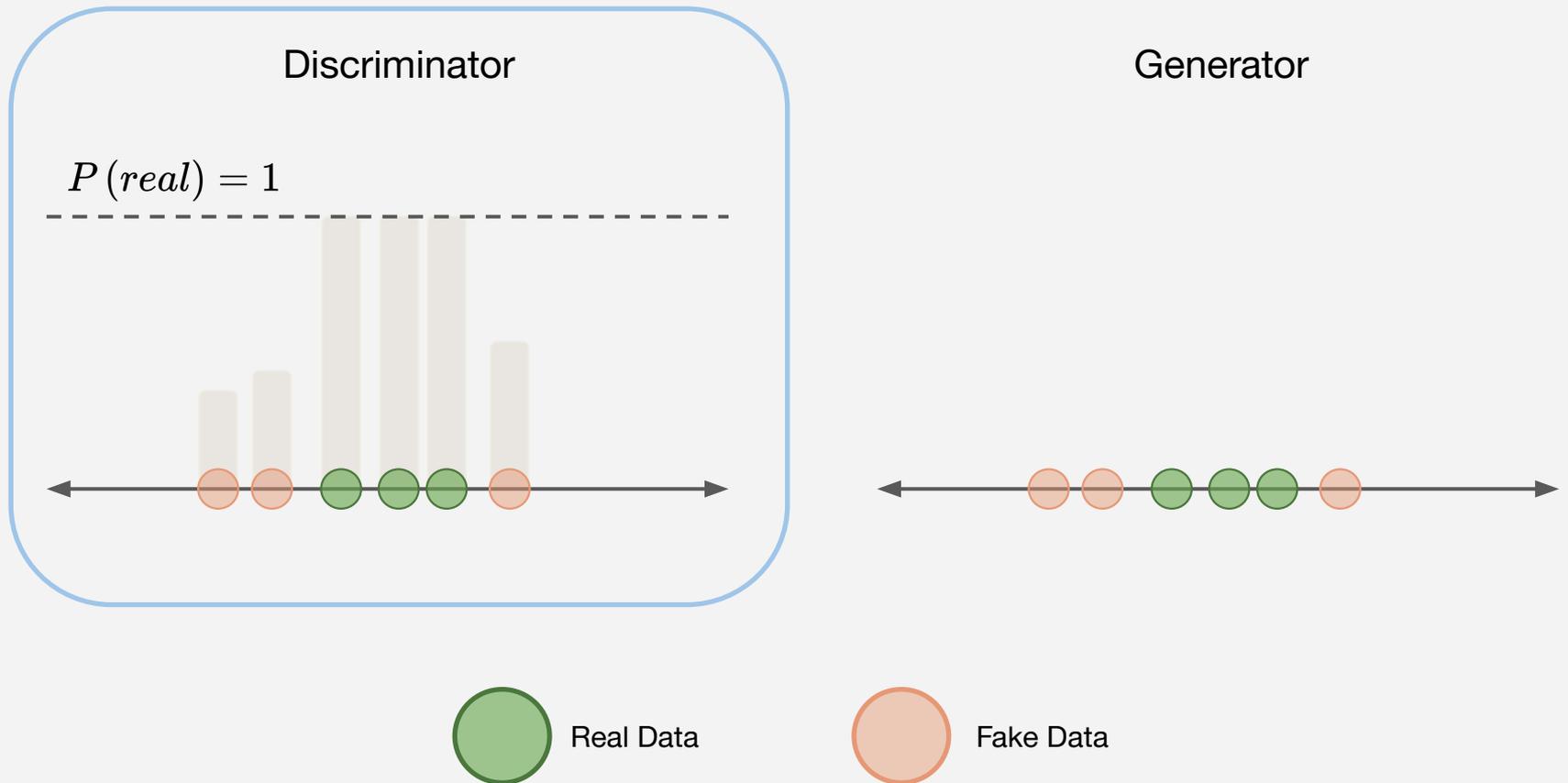
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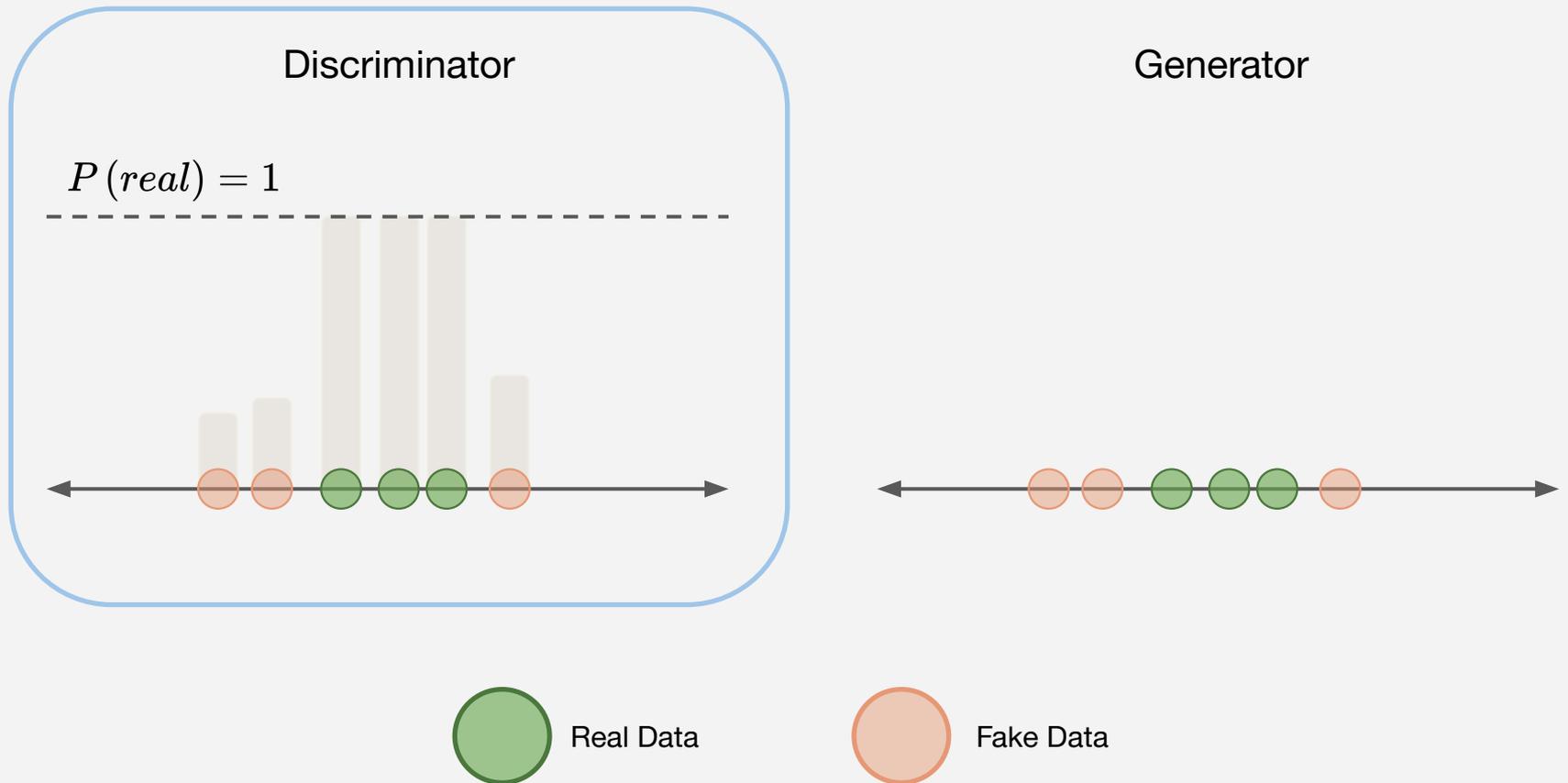
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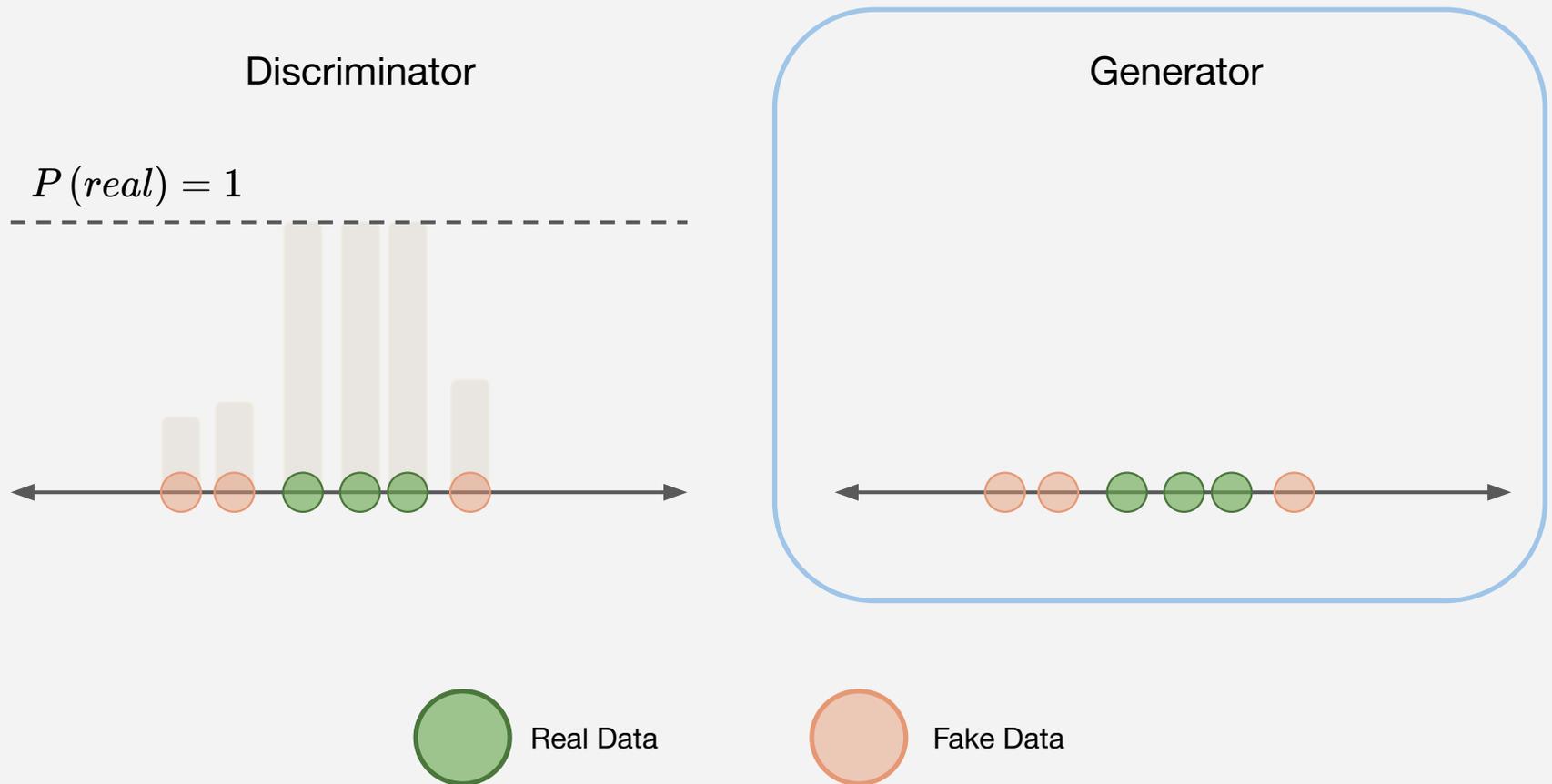
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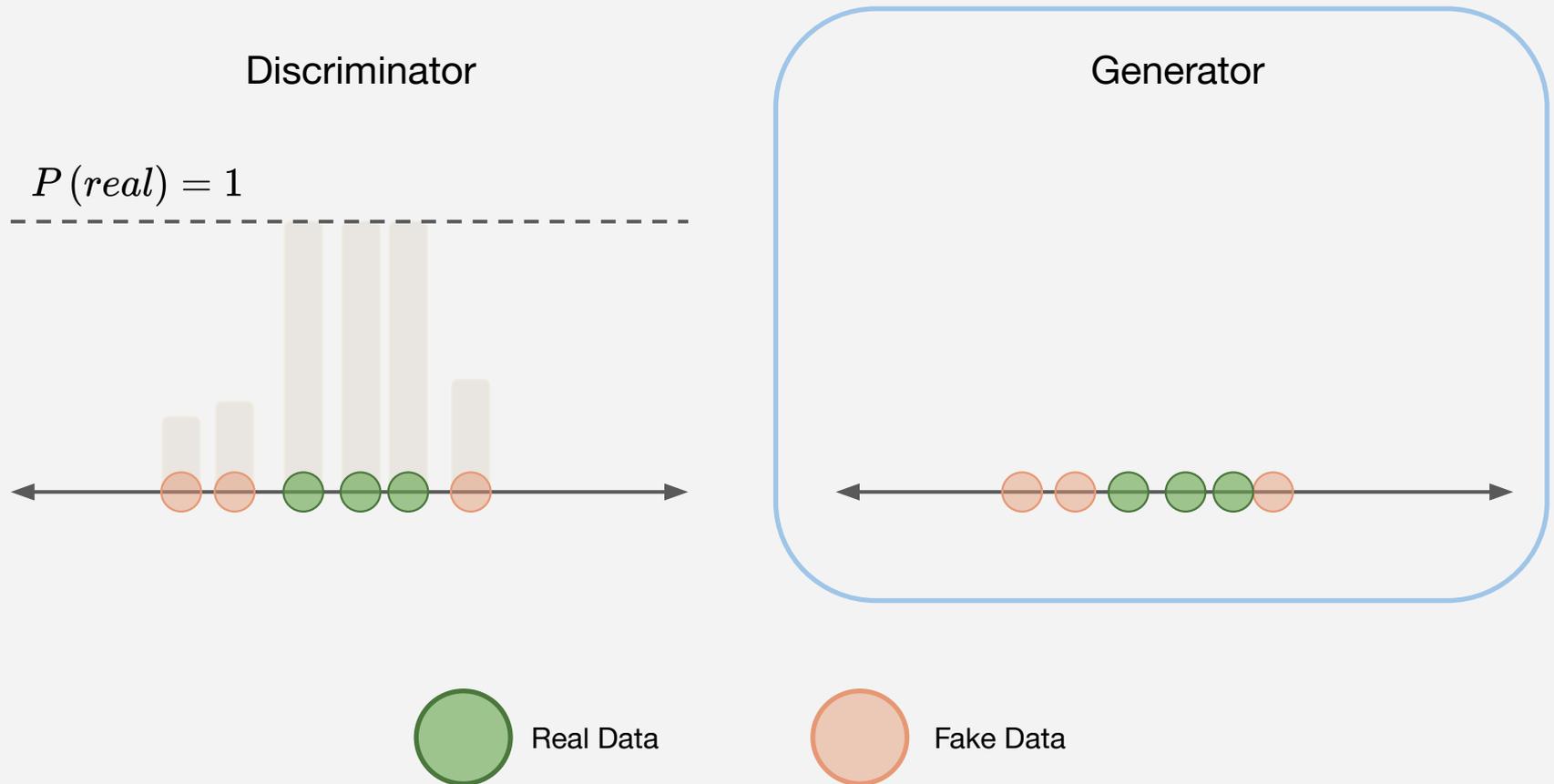
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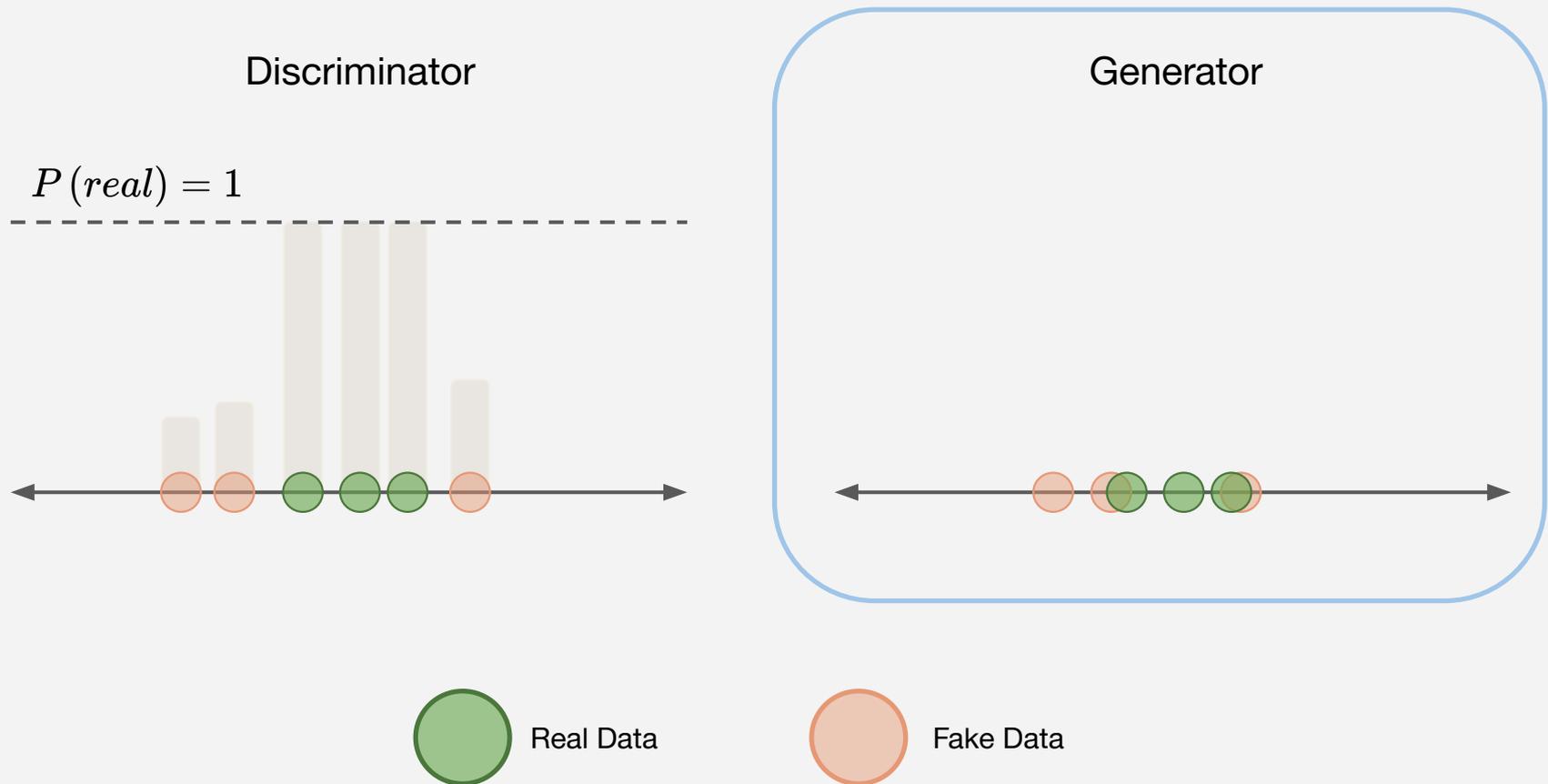
GAN Intuition

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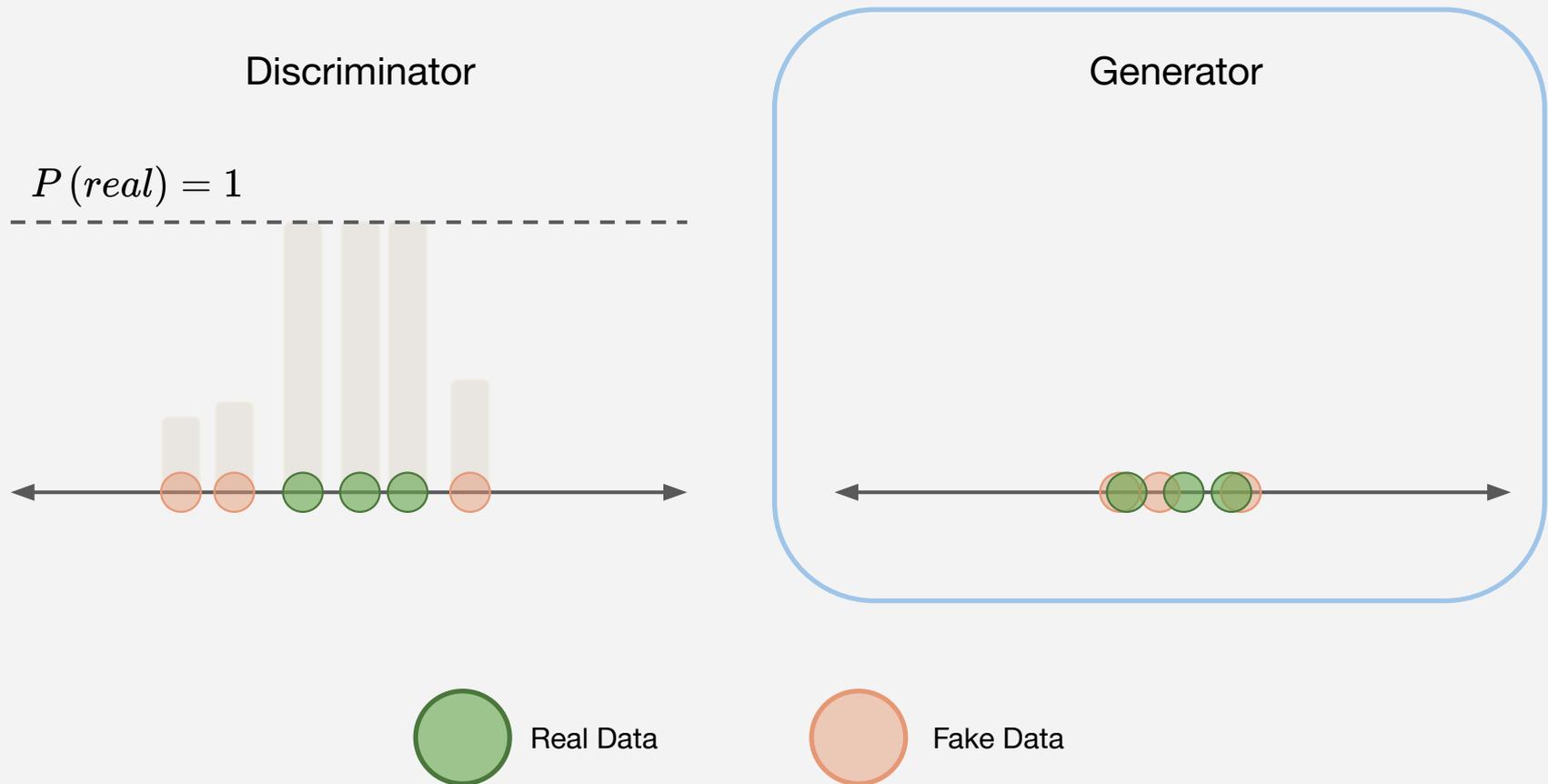
GAN Intuition

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GAN Intuition

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GAN Intuition

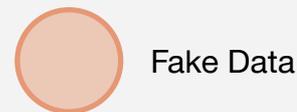
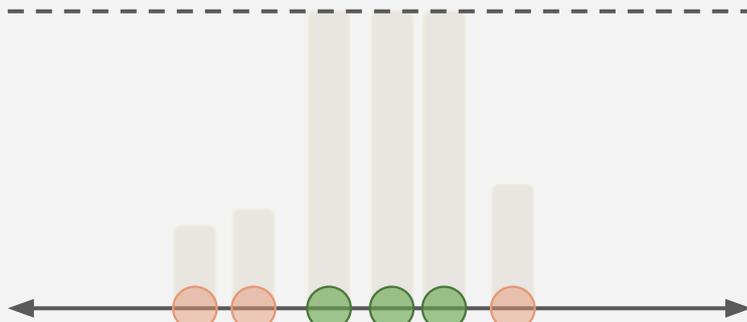
Discriminator tries to identify real data from fakes created by the generator

Generator tries to create imitations of data to trick the discriminator

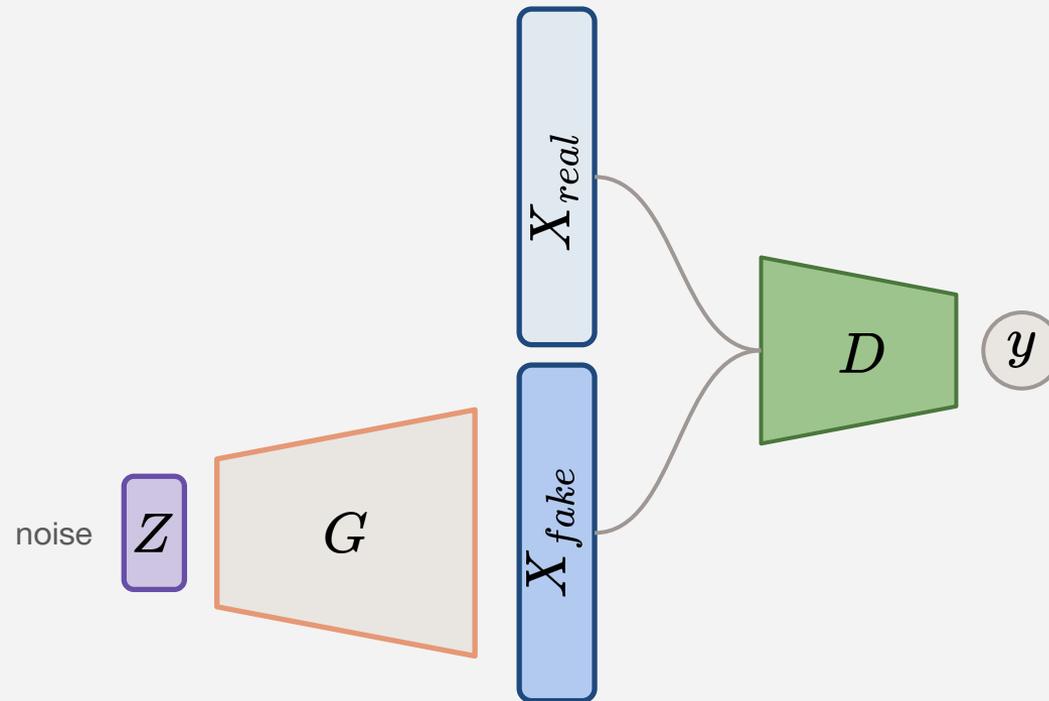
Discriminator

Generator

$$P(\text{real}) = 1$$

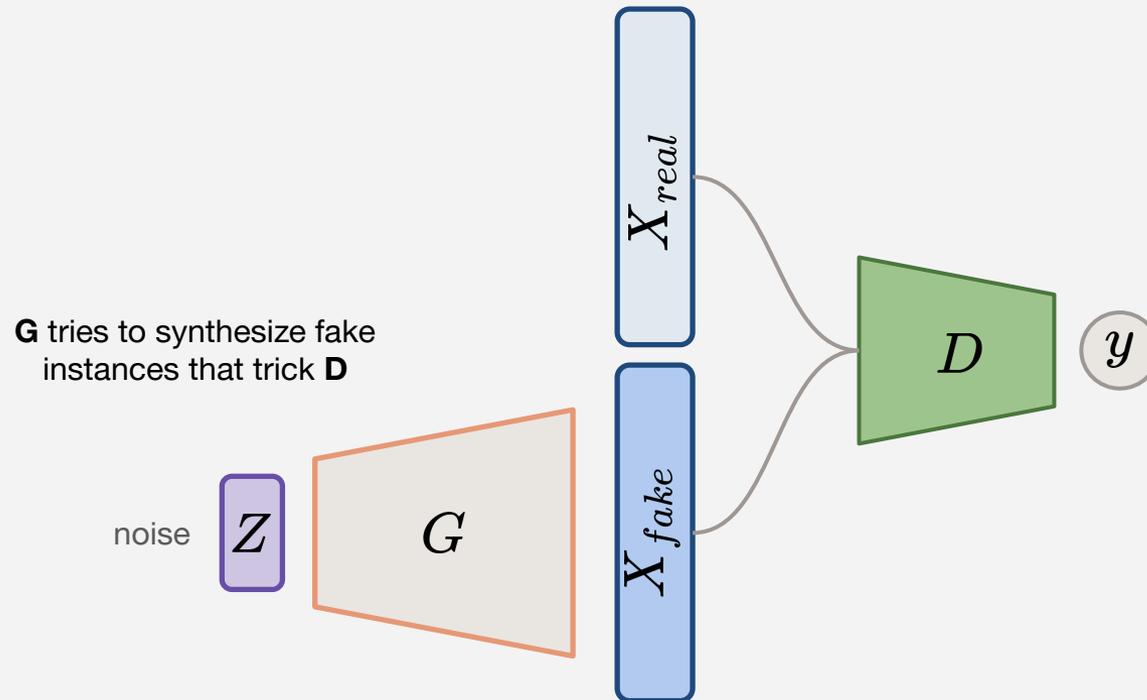


Training GANs



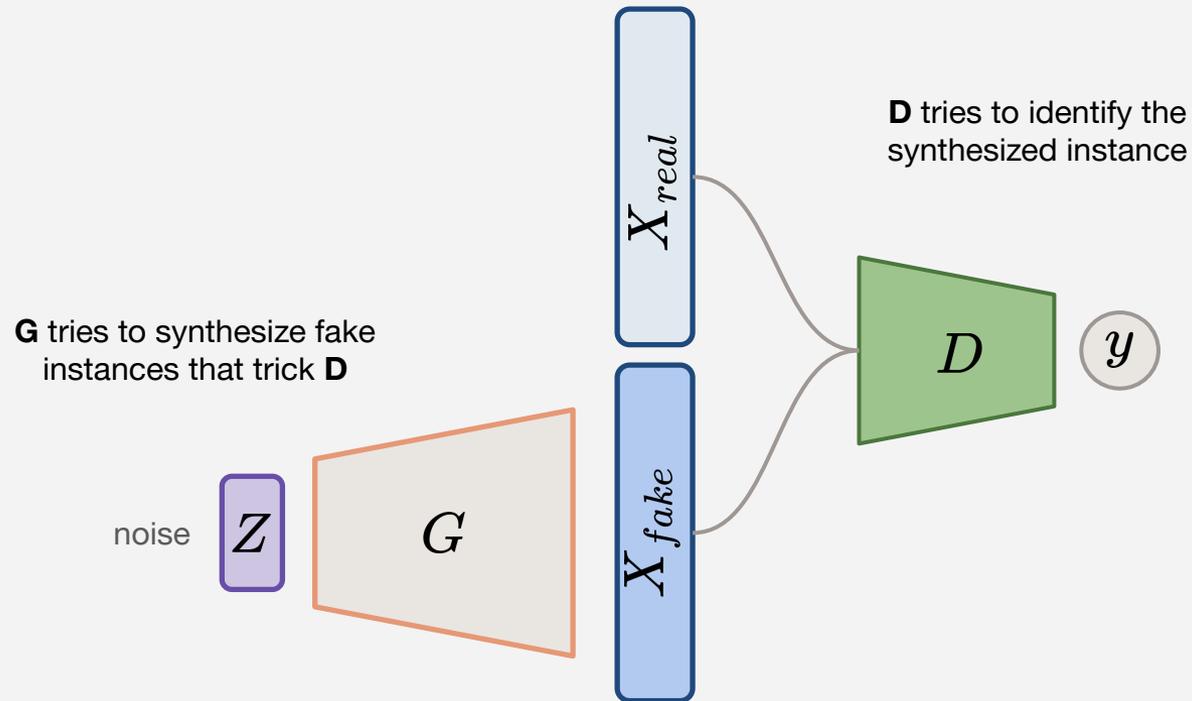
Training: adversarial objectives for **D** and **G**
Optimum: **G** reproduces the true data distribution

Training GANs



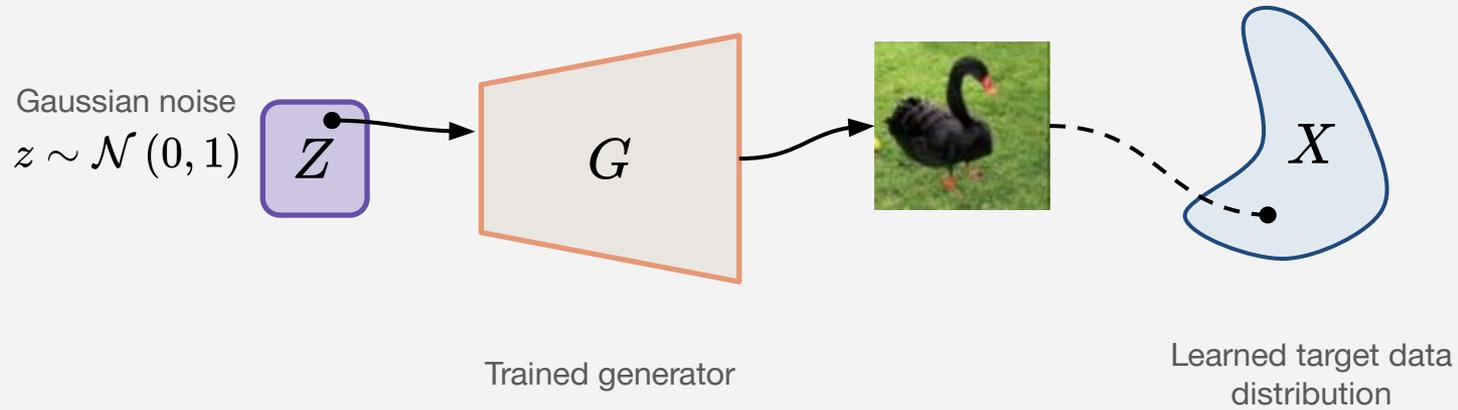
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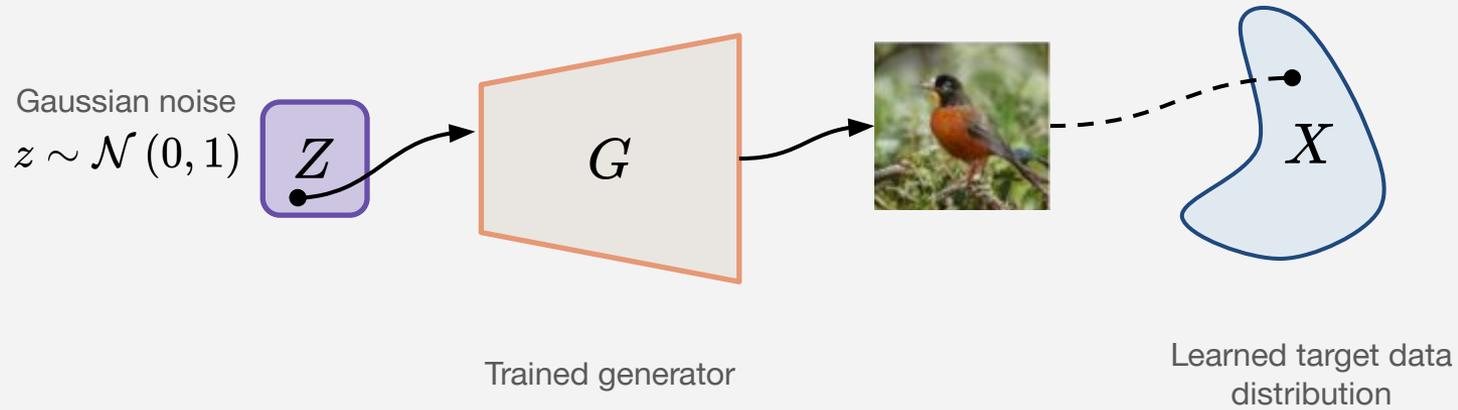


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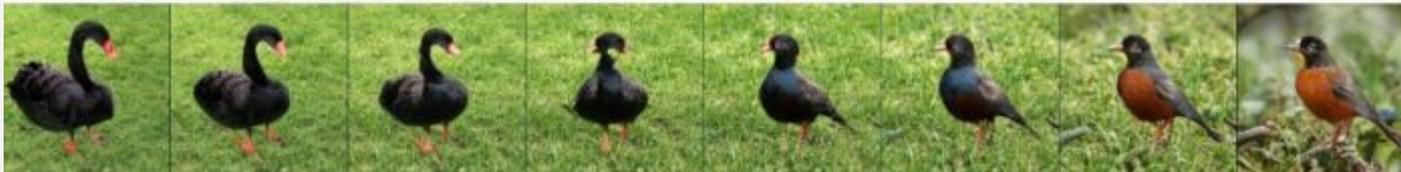
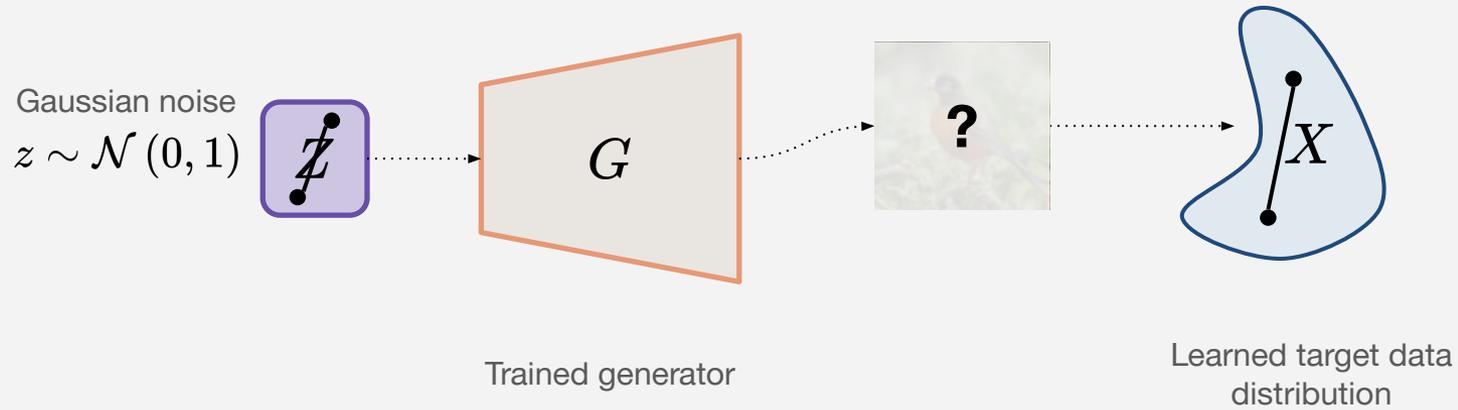
GANs: Distribution Transformers



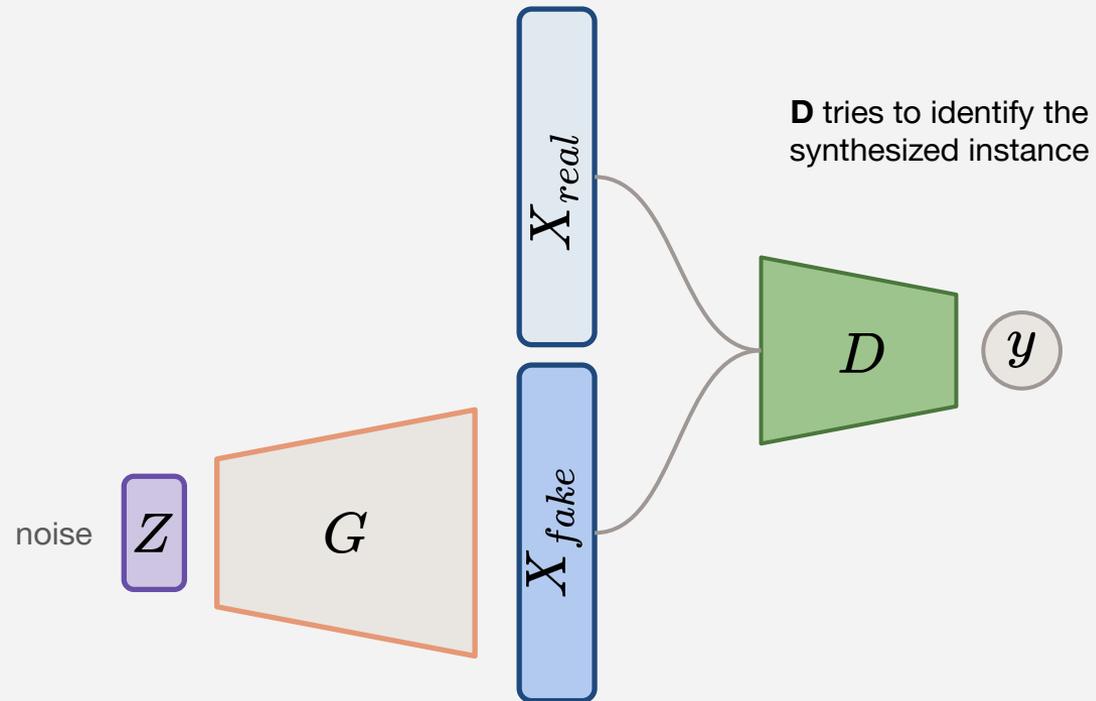
GANs: Distribution Transformers



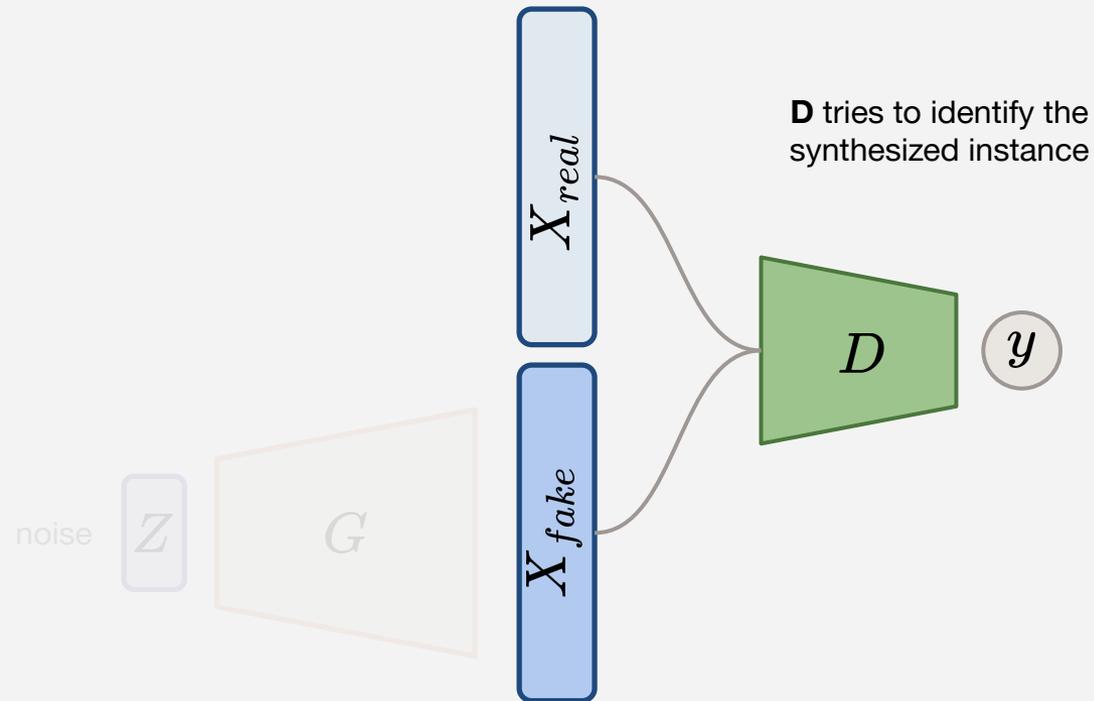
GANs: Distribution Transformers



Training GANs : Loss Function



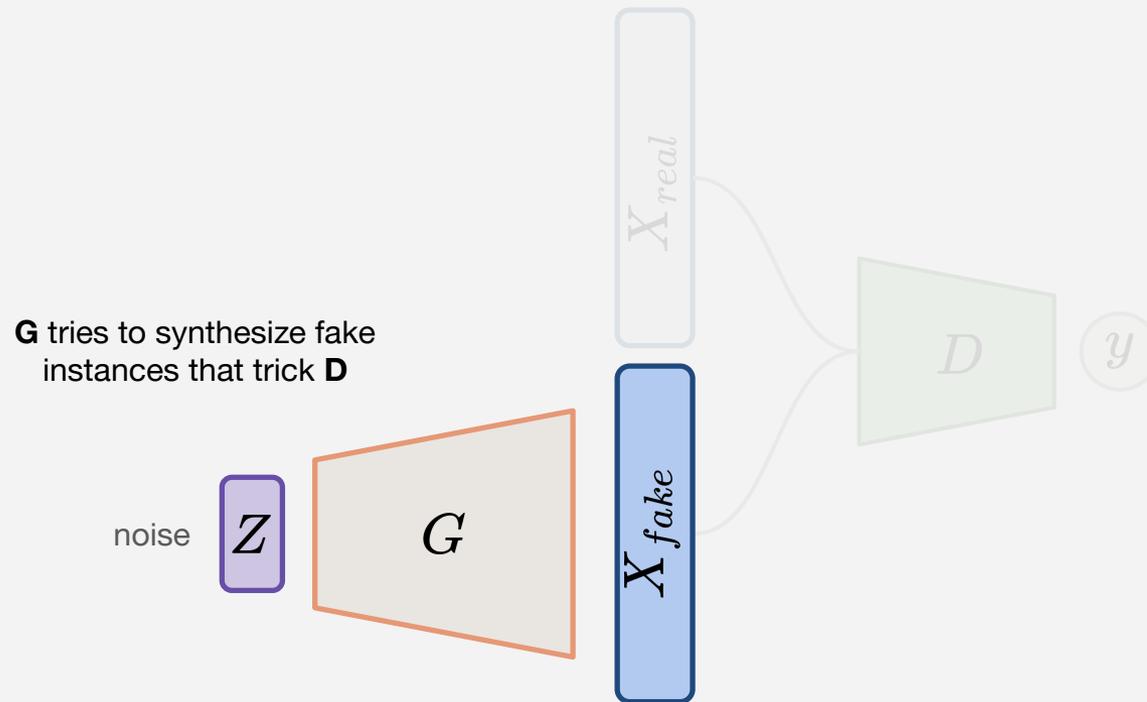
Training GANs : Loss Function



$$\arg \max_D \mathbb{E}_{Z, X} [\log D(G(Z)) + \log (1 - D(X))]$$

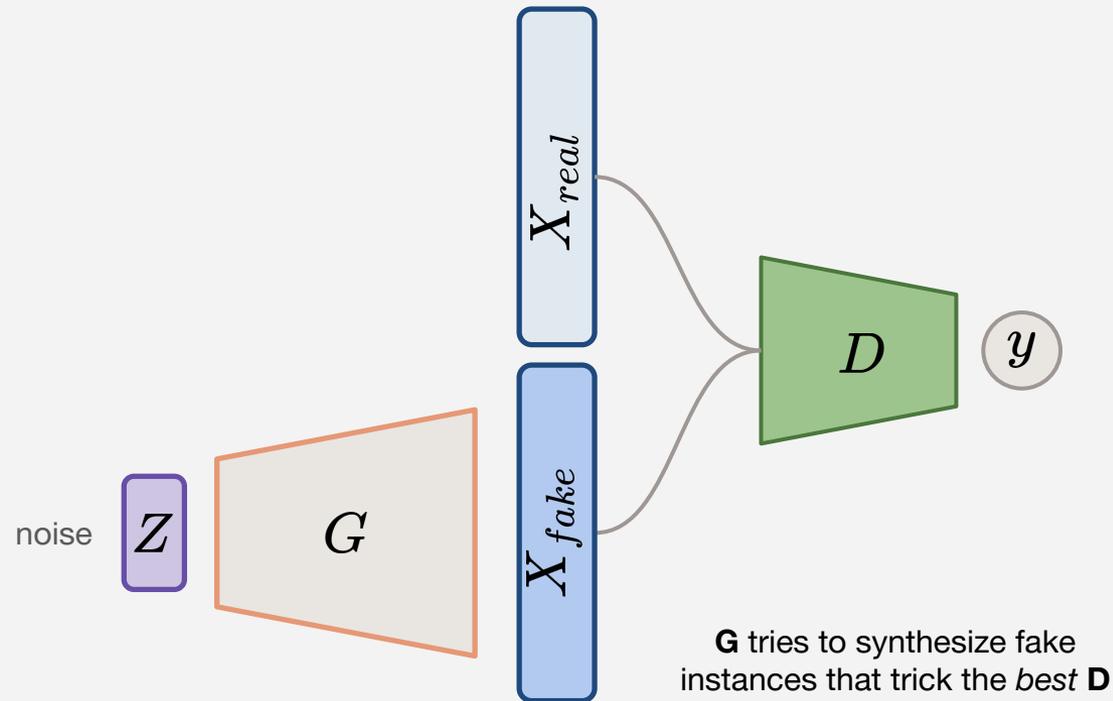
Fake Real

Training GANs : Loss Function



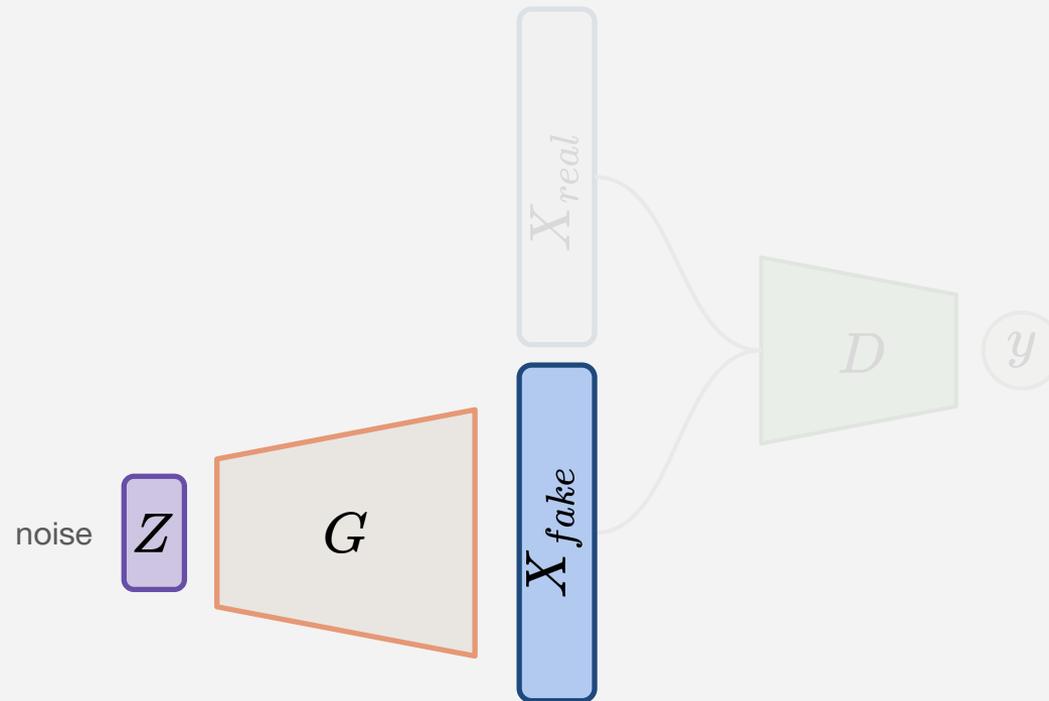
$$\arg \min_G \mathbb{E}_{Z, X} [\log D(G(Z)) + \log(1 - D(X))]$$

Training GANs : Loss Function



$$\arg \min_G \max_D \mathbb{E}_{Z, X} [\log D(G(Z)) + \log(1 - D(X))]$$

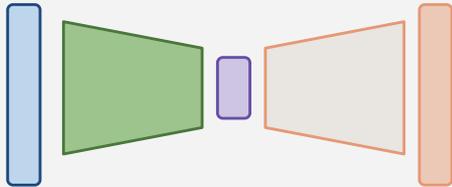
Generating New Data



After training, use generator network to create **new data** that's never been seen before

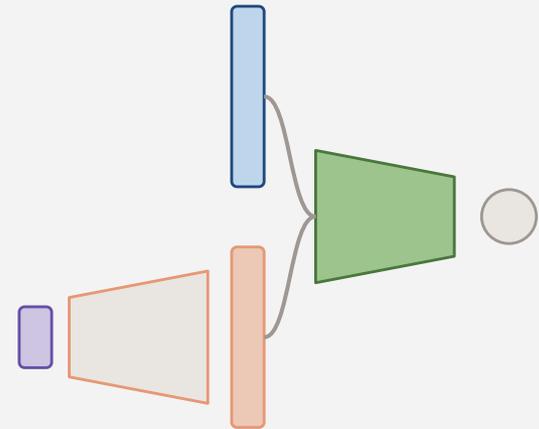
Generative Modeling

Learn lower-dimensional **latent space** and **sample** to generate input reconstructions



Autoencoders and Variational Autoencoders (VAEs)

Competing **generator** and **discriminator** networks



Generative Adversarial Networks (GANs)